

ELECTRICAL MEASUREMENTS & INSTRUMENTATION

(Diploma 4TH SEM)



Education for a World Stage

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Measuring Instruments

Some terms according to measuring instruments.,

① Accuracy :- It is the degree of closeness of measure value to the true value.

→ Accuracy is the conformity to the truth.

② Precision :- It is the reproducibility of the same result or value again and again.

→ Precision sure consistency of the result.

→ Accuracy can be improved by recalibrating instruments.

→ highly precision instruments may not sure accuracy but for having higher accuracy the instrument must be precision.

③ Sensitivity :- It is the smallest amount of difference in electrical quantities that will

Change an instrument reading.

(or)

It is the characterisation of instruments for change in output with change in input.

If for a finite change in the input the change in output is more then the instrument is highly sensitive.

④ Resolution

It is the smallest unit of measurement that can be indicated by an instrument.

→ If the resolution = $\frac{1}{1000}$ then the instrument can be read upto 3 value after decimal.

⑤ Error :- It is the deviation of measure value from actual value.

→ The main reason for ^{error} is the inability of the system to track in proper manner.

→ Error is fundamentally classified into 2 types.

① Absolute error :- It is defined as the difference of measure value to the standard value.

$$\boxed{S_A = A_m - A}$$

where, S_A = Absolute error

A_m = Measure value

A = Standard value

⑤ Relative error when the absolute error is represented in percentage then it is called as relative error.

$$\% S_A = E_r = \frac{S_A}{A} \times 100$$

⑥ Tolerance It refers to the total allowable error within an instrument.

→ It is specially represented with + or - sign.

Type of measuring instruments

Generally they are two types.

① Absolute instruments.

② Secondary instruments

Absolute instrument

On this instrument the electrical quantity is measured in terms of the instrument constant.

These instrument are used for comparison with other instruments but don't require any previous ~~calibration~~ Calibration with the aid of other instruments.

Bx- Tangent Galvanometer

Here the current is measured in terms of deflection constant.

$$I \propto \tan \theta$$

$$I = K \tan \theta$$

Secondary instruments :- These instruments are required to be calibrated with by comparison with an absolute instrument or any other secondary instrument which has already been calibrated against absolute instrument.

Ex- Ammeter, voltmeter, watt meter etc.

→ Secondary instruments are generally used in practical laboratory.

Classification of Secondary Instrument

The secondary instruments are further classified into 3 groups.

- ① Indicating type
- ② Recording type
- ③ Integrating type

① Indicating type :-

This is the instruments in which electrical quantity is measured by deflection of a pointer over a calibrated scale.

→ This instrument indicates the instantaneous value of the measurement quantities.

⇒ Ex - Volt meter, Ammeter, etc.

② Recording Instrument :-

These instruments gives a continuous record of the variation of electrical quantities being measured over a time interval.

→ here a extra ^{recording} mechanism is attach in the instrument.

→ generally a pen is attach to the moving system which traces the magnitude of quantity measured on a sheet of paper.

→ These instrument records daily ~~and~~ ^{or} annual use of power, power factor, load curve.

EX - ~~Energy meter~~.

③ Integrating type :-

On this instrument the electrical quantities are added up or integrated over the period of measured and then recorded.

EX - Energy meter.

Torque associated with indicating type instrument :-

- ① Deflecting torque (T_d)
- ② Controlling torque (T_c)
- ③ Damping torque (T_{dmp})

① Deflecting torque (T_d)

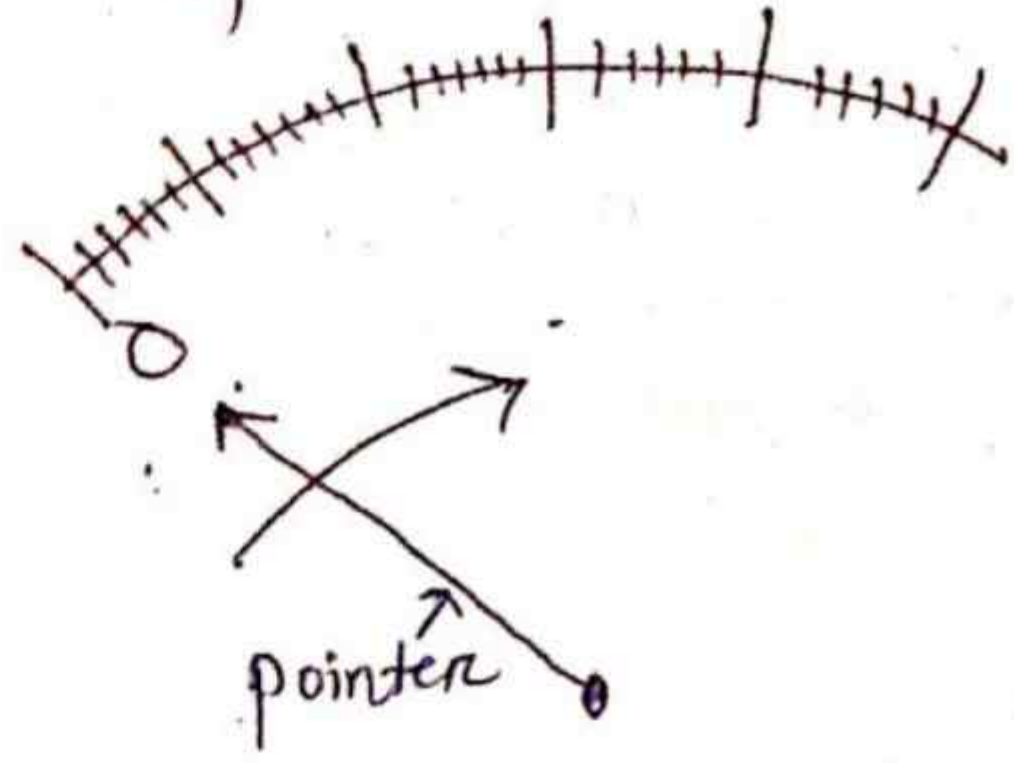
The purpose of deflecting torque is to deflect the pointer from its initial position.

→ It is represented by (T_d).

→ The direction of this ~~type~~ torque is in forward direction.

Date - 7/2/20

→ This torque can be produced by the utilisation of any one of the following effect produced by current or voltage.



- (i) Magnetic effect
- (ii) Electro dynamic effect
- (iii) Electro magnetic effect
- (iv) chemical effect
- (v) Thermal effect
- (vi) Electro static effect

② Controlling torque (T_c)

→ The purpose of control torque is -

- (i) It opposes the deflecting torque or it deflects the pointer proportional to the magnitude of supply voltage or current.
- (ii) It brings ~~at~~ the pointer to initial position when the supply gets disconnected from instrument.
- (iii) The direction of controlling torque is backward direction.

→ There are two mechanism to produce control torque.

- (i) Spring control mechanism.

② Gravity control mechanism,

① Spring control mechanism

In this mechanism two springs made up of ~~phosphor~~ phosphor bronze wire are used.

→ one spring is placed above and other is placed below the spindle of instrument.

→ Both are oppositely twisted,

→ The material used for making Springs should be non magnetic, low specific resistance, low temp. coefficient of resistance,

→ when the instrument is not in use the springs are in their condition and the control torque is zero,

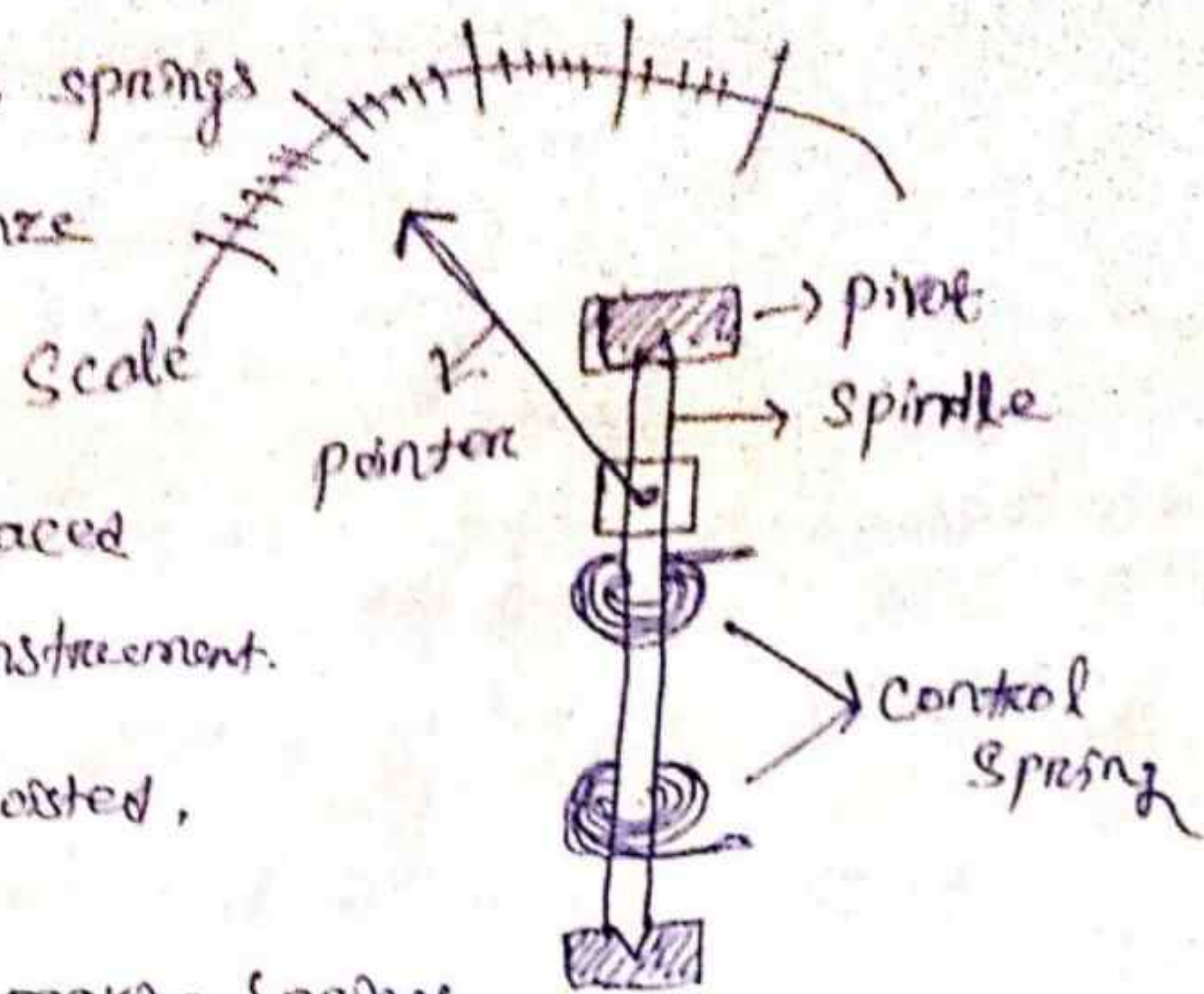
→ when the instrument is connected to the circuit then deflecting torque is produced and the pointer moves on the scale. so one of the spring get twisted and other spring get untwisted. the resultant twist produces the controlling torque.

→ The position when $T_d = T_c$, the pointer stops at that position.

→ Hence the control torque equation is

$$T_c = \frac{\gamma b t^3 \theta}{12L}$$

$$T_c = K \theta$$



where γ = young's modulus of spring material.
 b = width of spring
 t = thickness of spring
 θ = Deflection of the pointer.
 l = length of the spring.

Advantages of spring control mechanism,

- (i) The instrument can be placed in any position that is vertical or horizontal.
- (ii) This method does not increase the weight of the instrument as the spring is light.
- (iii) Scale is uniform in this method.

dis advantages

- (i) Temp. variation can affect the length and design of the spring so it can change the control torque.
- (ii) The spring get deteriorate with the time and hence accuracy is lost.

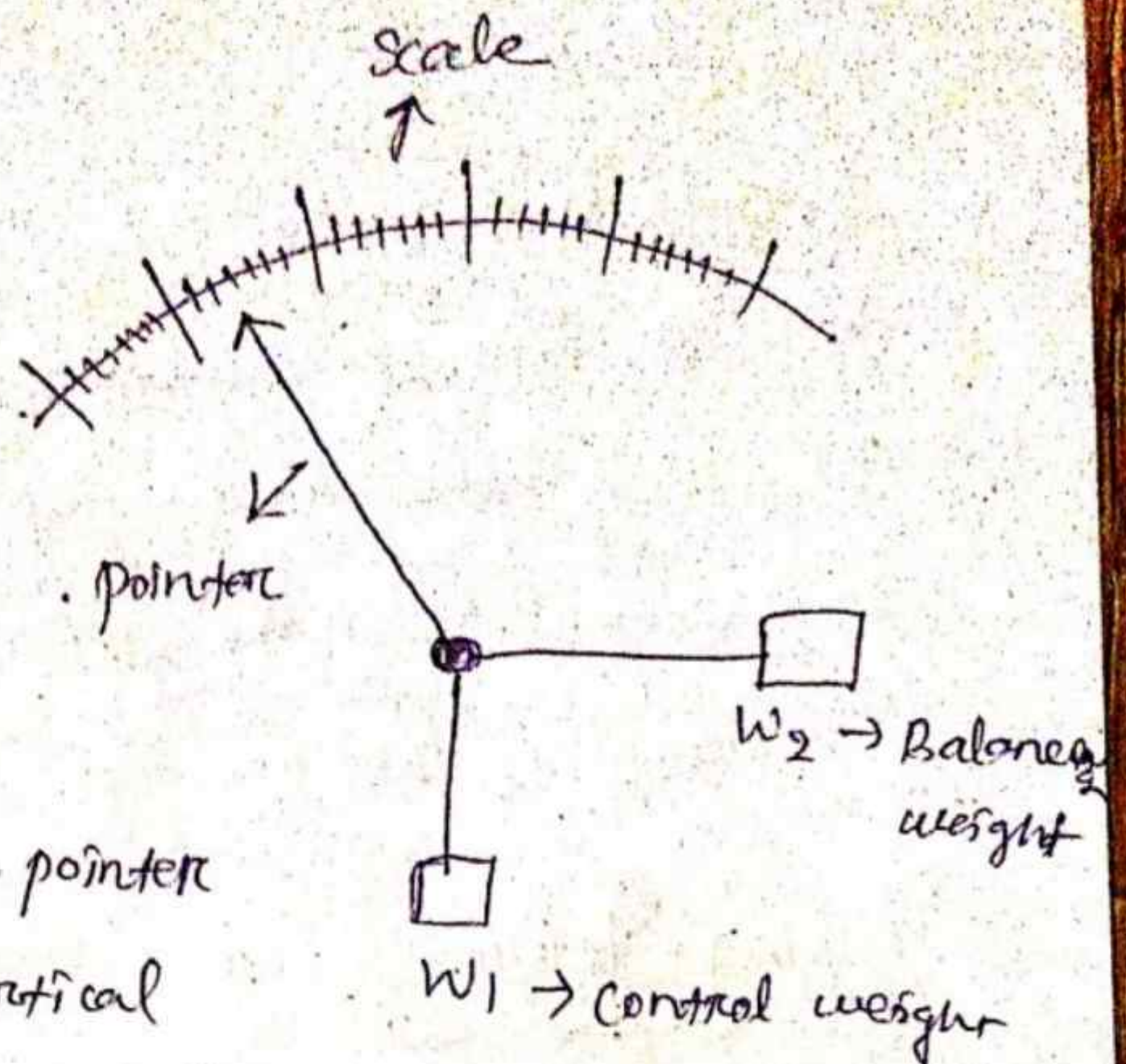
(3) Gravity control mechanism :-

On this method natural downward pole due to gravity is employed.

→ A small weight w_1 is attach to the moving system and a w_2 is attached for balancing the w_1 .

$$T_c = W_1 l \sin \theta$$

$$T_c \propto \sin \theta$$



→ At '0' position of the pointer

the control weight is in vertical position and therefore no control torque is produced.

→ when the instrument is connected to the circuit deflecting torque produced and the pointer is deflected by an angle θ from its initial position.

~~But due to the gravity the control weight try to~~
~~and~~ and the control weight also deflects by an angle θ . But due to the gravity W_1 try to come back to its original vertical position hence ~~reverse~~ control torque is produced.

→ There are two components $W_1 \sin \theta$, $W_1 \cos \theta$, only $W_1 \sin \theta$ will produce the control torque. hence ^{component} of the control torque is $W_1 \sin \theta$.

Advantages

- ① It is simple and cheap method.
- ② It is not affected by temp. variation.

Disadvantages

- (i) Scale is non uniform so the reading become difficult.
- (ii) This method increases the weight of the instrument.
- (iii) This instrument should be placed always in vertical position. otherwise it may produce error in the reading.

Date-14/1/20

Damping torque T_D

It is the torque which is required to damp the oscillation of the pointer.

→ It helps to take the reading.

→ It provided by some mechanism that are,

- (1) air friction damping -
- (2) fluid friction damping
- (3) Eddy current damping

(1) Air friction damping

In this system the moving system (pointer) is attach with a piston which is placed in a air chamber. The piston is made up of aluminium.

The air chamber is covered at the top,

→ The oscillation of pointer is damp by the movement of piston in air chamber.

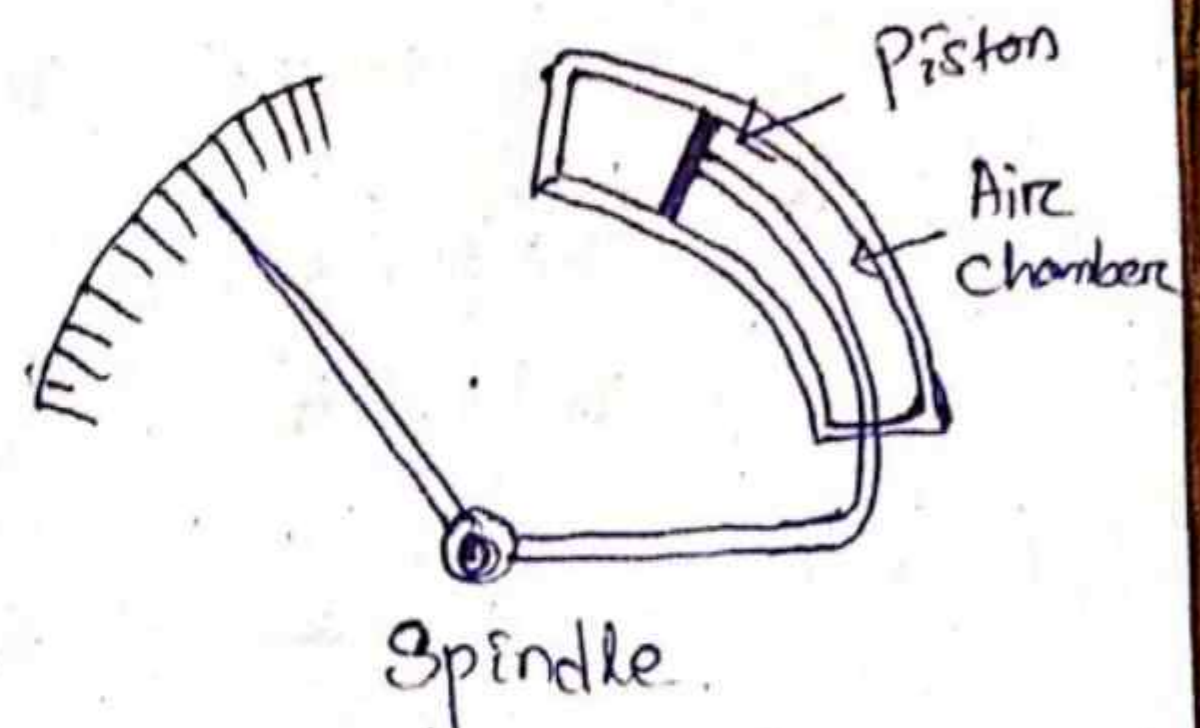
→ It is run by compression and expansion of the air.

→ It is observed that in forward oscillation the piston moves inside the chamber and the air gets compressed and for backward oscillation piston moves outside the chamber so the air gets expanded.

→ This system is used in MI instruments and electro dynamometer type instruments.

→ Air friction damping is preferred where low value of magnetic field is used.

Fluid friction damping :-



(Fluid friction damping)

(Air friction damping)

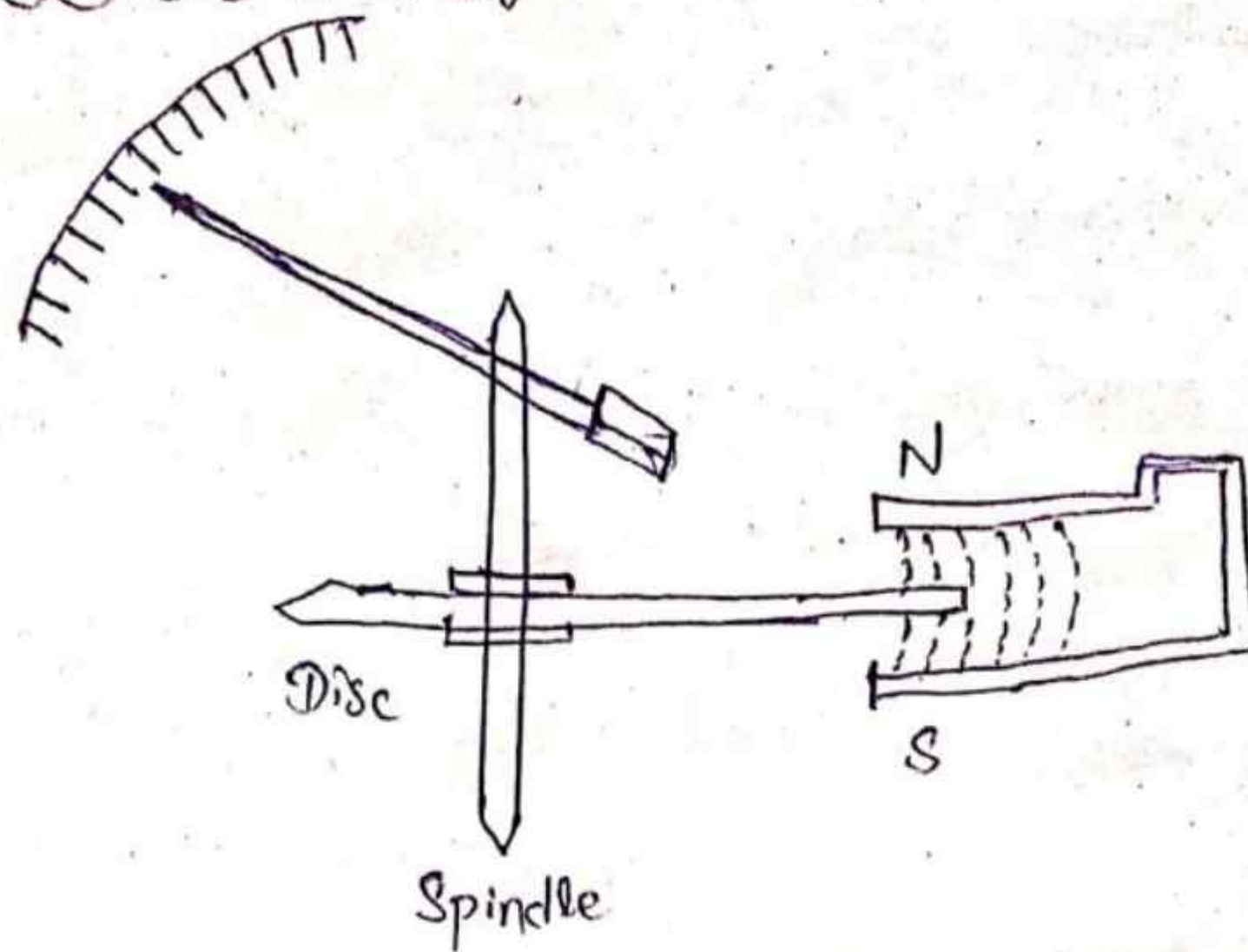
In this method a light aluminium vane (or) piston is attached to the moving system and made to dip into a viscous liquid.

→ Generally damping oil is used as liquid.

→ When pointer starts oscillate spindle gets rotated and the aluminium vane also starts rotating against the viscosity of fluid.

The opposition offered by the fluid provides damping to the oscillation.

Eddy current damping :-



→ In this mechanism a copper or aluminium disc is attached to the spindle as shown above the figure.

→ When the ~~rest~~ pointer starts to oscillate the spindle gets rotated by which the aluminium disc also starts rotating. As we see that the aluminium disc is rotating inside a magnetic field, so an emf is induced in the aluminium disc.

→ By which a current flows through the aluminium disc which is known as eddy current. This eddy current opposes the cause that generates it.

That is oscillation, so the damp is provided.

→ In this permanent magnet is used.

Fluid friction damping used in electro static type instruments.

Eddy current damping is the most efficient damping.

~~PMMC Type Instruments~~ Classification of Instrument

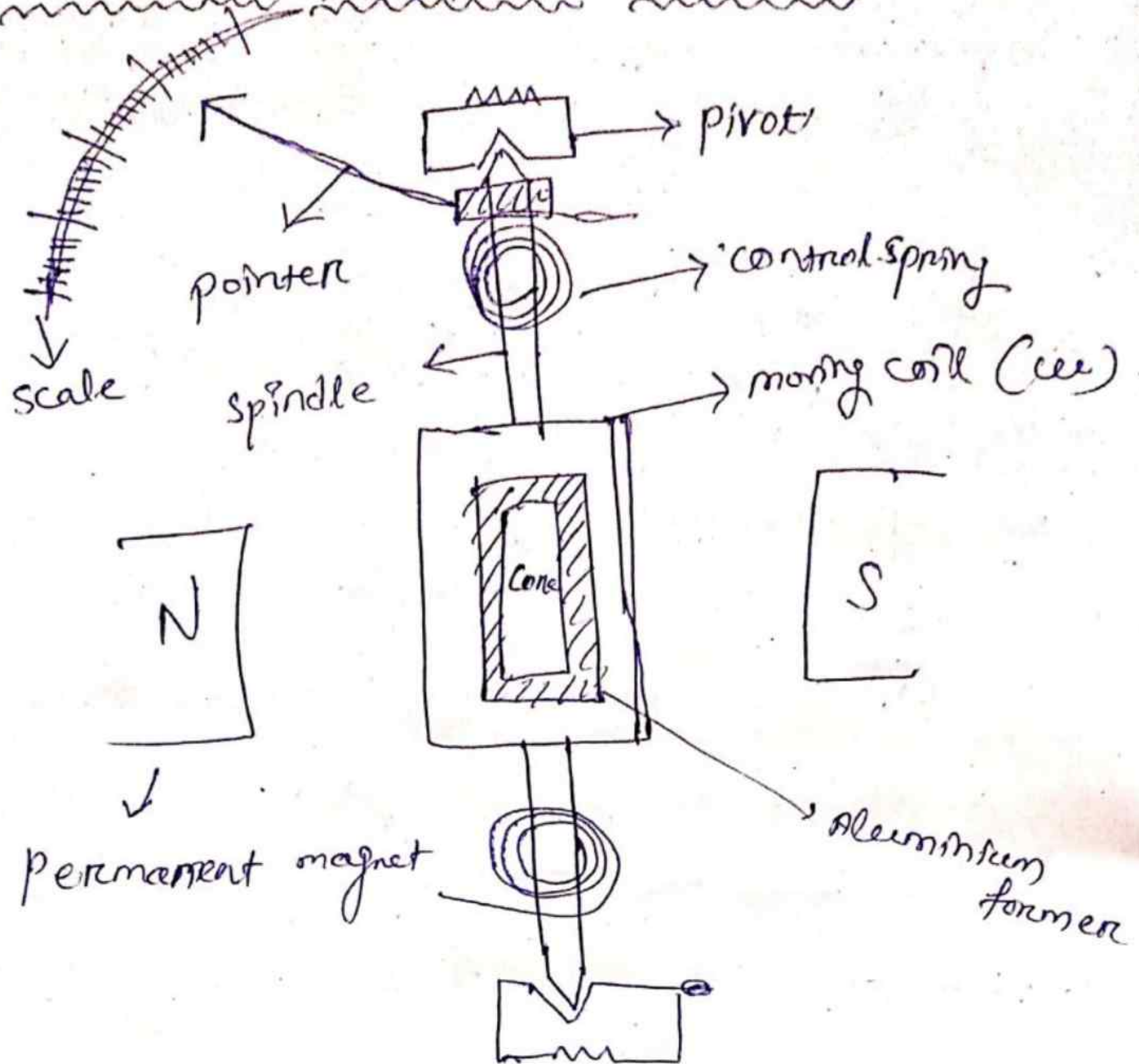
① According to measurement,

- ① Voltmeters and ammeters (V, I)
- ② Wattmeters and energy meter (P, E)
- ③ Phase and frequency meters ~~(ϕ, f)~~
- ④ D.C. and A.C. Bridges
- ⑤ Instrument transformer

② According to construction and operating principle,

- ① Permanent magnet moving coil instrument (PMMC)
- ② Moving Iron Instrument. (MI)
- ③ Electro dynamometer type instrument.
- ④ Electro static type instruments.
- ⑤ Induction type instrument.
- ⑥ Electro thermic instrument.

Construction of PMMC instrument



A PMMC instrument consist of two main parts moving coil and a permanent magnet along with other parts,

① Magnet system (or) Permanent magnet :-

On this instrument the necessary magnetic field is obtained by permanent magnet.

and hence the name.

→ In earlier days horseshoe magnets were used but the disadvantages with this is it has more weight so the torque by weight ratio decreases. For better accuracy torque/weight must be greater than 1.

→ Now a days Permanent magnet with high intensity and high coercive forces with U-shaped are used. These are generally made up of alcomax, alnico, ferrites etc.

(II) Moving coil :-

It is one of the main component of PMMC instrument. It is made up of ccc-coil which is wound on a rectangular block placed betⁿ the magnetic poles.

→ The rectangular block is made up of aluminium, and it is called aluminium former, which is pivoted to the Jewel bearing for free rotation through spindle.

→ Supply or connection is given to the moving coil.

(III) Control system :-

Here, Spring control mechanism is used for providing control torque.

→ Two ~~thin~~ hair springs made up of phosphorous bronze are wound on the spindle of the instrument.

④ Damping System:-

In this instrument eddy current damping is used. It is done by the movement of aluminium plate in the magnetic field.

⑤ Scale and pointer:-

The pointer is attached to the spindle which moves over a calibrated scale.

→ pointer is made up of aluminium because it is the lighter material having lesser inertia. So it can deflect for small deflecting force.

→ pointer is in the shape of needle (or) arrow.

Principle:-

It works on the principle of DC motor i.e. whenever a current carrying conductor is placed inside a magnetic field it will experience a rotating force or torque.

When the supply is given to the moving coil it develops electromagnetic torque by which coil starts deflecting. This deflection of coil is carried to the pointer through spindle, and pointer deflects on the scale.

The deflecting torque can be estimated as,

$$T_d = B L N d$$

where B = magnetic flux density

I = current to the scale

l = length of the coil

N = no of turns of coil

d = diameter of coil.

Once the construction is completed, l, N, d are constant and since the magnet is permanent magnet, ' B ' also remains constant. So now the ' T_d ' becomes.

$$\therefore T_d = G I \quad \therefore \boxed{T_d \propto I}$$

$$\Rightarrow \boxed{G = B l N d} \quad \text{--- (1)}$$

~~So~~

here the control torque is provided by the spring
so it can be expressed as

$$\boxed{T_c = K \theta} \quad \text{--- (2)}$$

where K is the spring constant.

θ = the angle of deflection.

~~So in this instrument the damping torque is provided to damp the oscillation.~~

as we know that the pointer remains in steady position when, $T_d = T_c$.

So by equating eqⁿ ① and ②, we found that

$$\Rightarrow G\theta = K\theta$$

$$\Rightarrow \theta = \frac{K}{G\theta}$$

$$\text{or } \theta = \frac{G\theta}{K}$$

$$\text{So } \boxed{\theta \propto I}$$

→ From this eqⁿ it can be concluded that the scale is uniform.

→ In this instrument the damping torque is provided to damp the oscillation.

Application:-

① This instrument is used as ammeter, ~~and~~ voltmeters.

② ~~It is~~ it is ~~exclusively~~ exclusively used for D.C. measurement i.e. DC voltage (or) DC current.

Advantages:-

- High torque by weight ratio
- Uniform scale.
- Less power consumption
- No hysteresis loss
- ~~less~~ affected by stray magnetic field.

→ Can be used as ammeter, voltmeter and watt meter.

Disadvantages :-

- These are only used for DC measurement.
- It is costly than other instrument.

Date-29/01/20

Extension range of PMMC type instrument :-

The PMMC instrument fundamentally developed is of very much lower rating, so it can't be suitable for measurement of higher range. So ^{to} enable the instrument to match the practical requirements small electrical modification are made to the basic instrument that is called as Extension range of PMMC instrument.

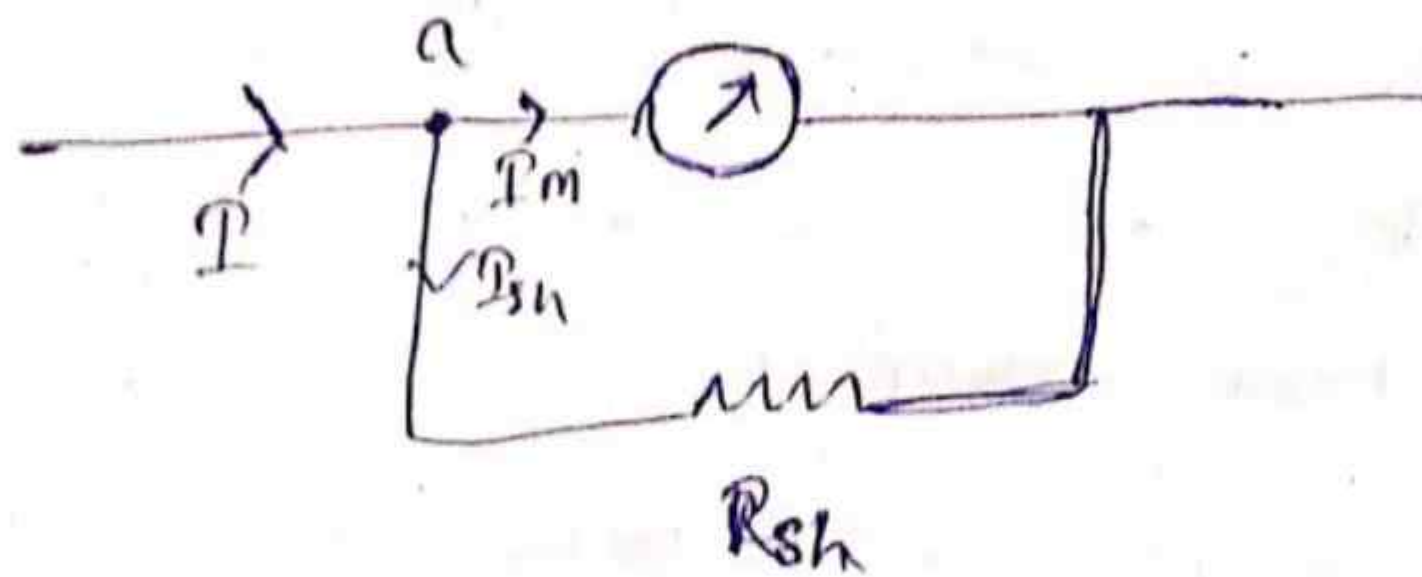
→ It is the small modification made to the instrument to measure the high range of voltage and current.

PMMC instrument as an ammeter :-

The current rating in general can be increase by decreasing ~~of~~ the effective resistances. The decrement of resistance is possible by providing some path, there by the range of ammeter can be extended by providing a shunt resistance to the existing instrument.

Let's consider a prime ammeter as shown in the figure. Where I_m through is the current through the meter, R_m is the resistance of the meter.

We have to extend the value upto 'I' ampere, hence we have to provide a shunt path having resistance R_{sh} .



$R_{sh} \rightarrow$ It is the shunt resistance connected ~~to the~~ parallel to the instrument.

Derivation:-

The voltage drop in meter path and shunt path remains constant;

$$\text{i.e. } I_m R_m = I_{sh} \cdot R_{sh}$$

$$\Rightarrow R_{sh} = \left(\frac{I_m R_m}{I_{sh}} \right) \quad \text{--- (1)}$$

Putting K_{EL} at node 'a'.

$$I = I_m + I_{sh}$$

$$\Rightarrow I_{sh} = I - I_m$$

putting value of I_{sh} in eq (1)

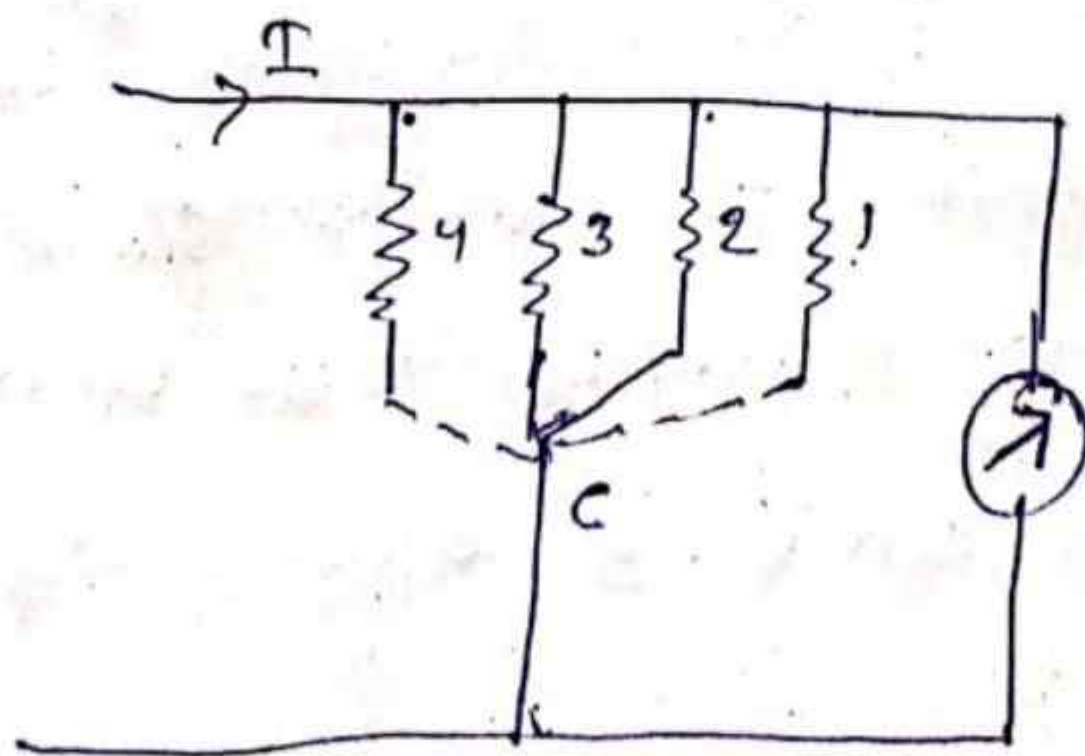
$$\Rightarrow R_{sh} = \left(\frac{I_m}{I - I_m} \right) \cdot R_m$$

$$\Rightarrow R_{sh} = \left(\frac{1}{\frac{I}{I_m} - 1} \right) \cdot R_m$$

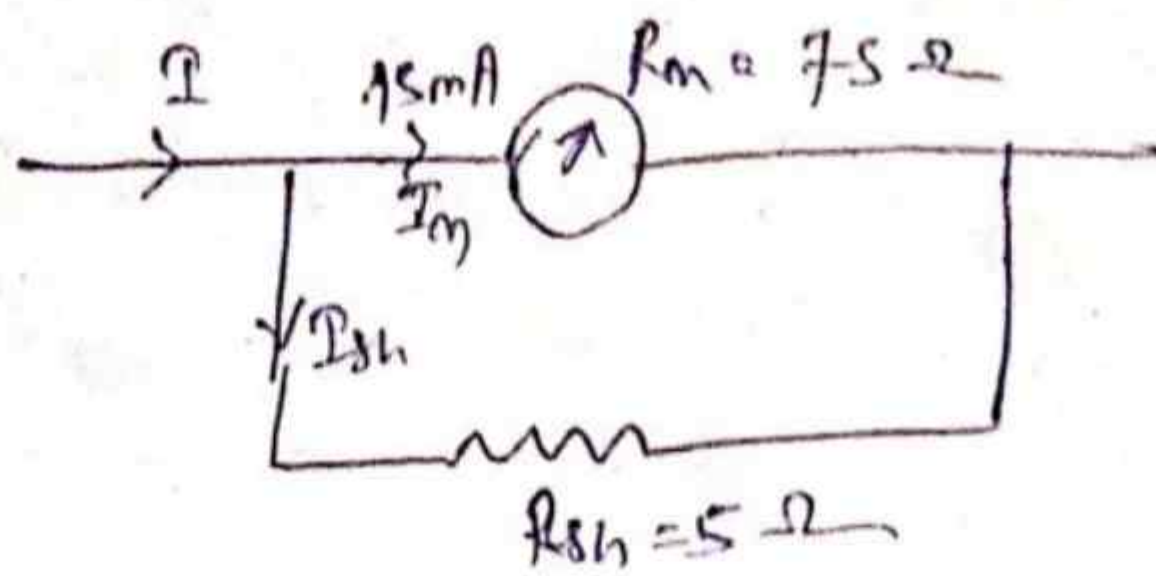
$$\Rightarrow R_{sh} = \frac{R_m}{(N-1)} \text{ or } \frac{R_m}{(m-1)}$$

where $N = m = \frac{I}{I_m} = \text{constant or multiplication factor}$

when no. of shunts are connected to the ammeter its value can be extended to the different ranges. It can be shown in the figure.



- ① The prime instrument of rating 15 mA , 75Ω , which shunted with a resistance of 5Ω , then find out the overall rating of the instrument.



$$\therefore R_{sh} = \frac{15 \times 75}{I_{sh}}$$

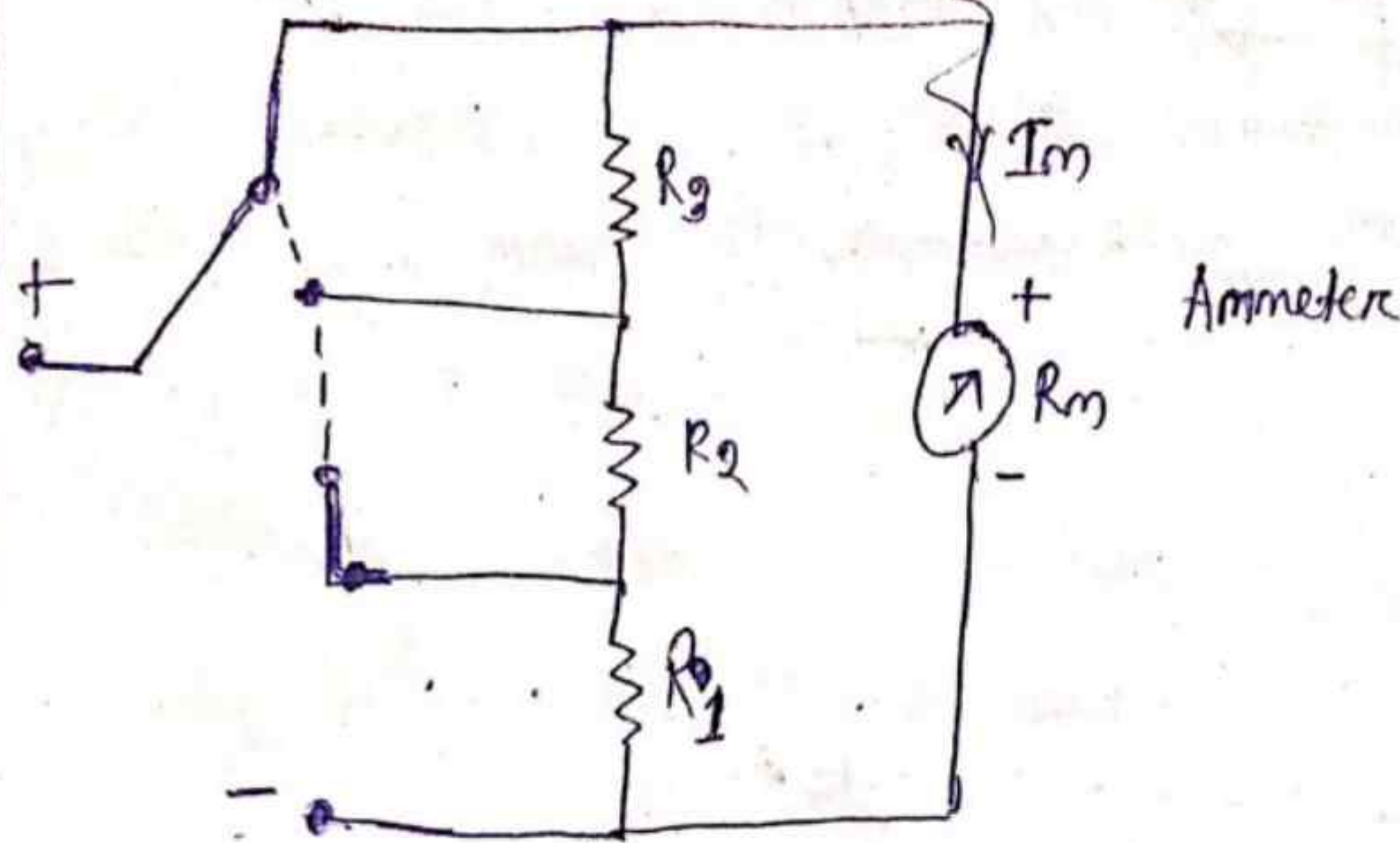
$$\therefore 5 = \frac{15 \times 75}{I_{sh}}$$

$$\Rightarrow I_{sh} = \frac{15 \times 75}{5} = 225 \text{ mAmp}$$

$$\therefore I = I_m + I_{sh} = 15 + 225 = 240 \text{ mAmp}$$

② A moving coil ammeter has full scale deflection of ~~150 mA~~ 15 mA and a coil resistance 1000Ω . Then what will be the value of shunt resistance required for the instrument to be converted to read a full scale deflection of 1 amp.

③ The full scale deflection current of an ammeter 1 mA and its internal resistance is 100Ω . If this meter is to have scale deflection at 5 amp what is the value of shunt resistance to be used.

Universal Shunt :-Calculation

- I_m, R_m are the meter ~~res~~ current and resistance.
- R_1, R_2, R_3 are the resistances connected in parallel with the ammeter.
- when the switch is in position '3', R_1, R_2, R_3 are in series and attached shunt to the meter, so ^{effective} resistances are minimum maximum ~~at~~ current flows to the meter.

The voltage drop across two parallel branches are given by

$$I_{sh} \cdot R_{sh} = I_m \cdot R_m$$

$$R_{sh} = R_1 + R_2 + R_3 \Rightarrow I_{sh}(R_1 + R_2 + R_3) = I_m R_m$$

- when the switch is in position '1' R_1 is parallel to $R_2 + R_3 + R_m$ and here the voltage drop eqⁿ is

$$I_1 R_1 = I_m (R_2 + R_3 + R_m)$$

→ when the switch is in position '2' $R_1 + R_2$ is in parallel with $R_3 + R_m$, and voltage eqⁿ becomes,

$$I_2 (R_2 + R_1) = I_m (R_3 + R_m)$$

Q. Design a universal shunt / Ayrton shunt to provide an ammeter with the current first 1amp, 5amp, 10 amp. The basic meter resistance is 50Ω , and full scale ~~meter~~ ^{current} reflection is 1mA .

~~Ques~~ Solⁿ

Given that, $I_1 = 1\text{amp}$, $I_2 = 5\text{Amp}$, $I_3 = 10\text{Amp}$.

$$R_m = 50\Omega, \quad I_m = 1\text{mA} = 1 \times 10^{-3}\text{Amp}$$

when the switch is in position - 1

$$1 \times R_1 = 1 \times 10^{-3} (R_2 + R_3 + 50)$$

$$\Rightarrow R_1 - R_2 \times 10^{-3} - R_3 \times 10^{-3} = 50 \times 10^{-3} \quad \text{--- (1)}$$

when the switch is in position - 2

$$5 \times (R_2 + R_1) = 1 \times 10^{-3} (R_3 + 50)$$

$$\Rightarrow 5R_1 + 5R_2 - R_3 \times 10^{-3} = 50 \times 10^{-3} \quad \text{--- (2)}$$

when the switch is in position - 3

$$10 \times (R_1 + R_2 + R_3) = 1 \times 10^{-3} \times 50$$

$$\Rightarrow 10R_1 + 10R_2 + 10R_3 = 50 \times 10^{-3} \quad \text{--- (3)}$$

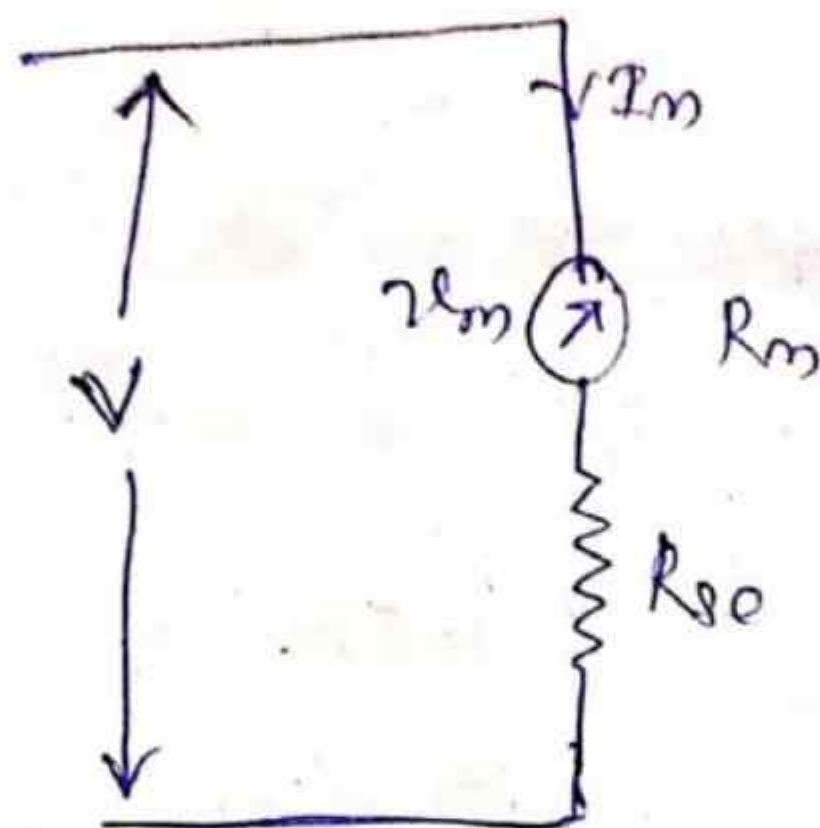
$$\therefore R_1 = 0.04, \quad R_2 = -0.039, \quad R_3 = -4.99$$

Extension range of prime volt meter :-

The voltmeter is extended by increasing the resistance of the ext. SO to increase the rating of voltmeter series resistances are connected with the Volt meter.

The series resistance connected with the voltmeter are called as multiplier.

Let's consider a prime volt meter as shown in the figure.



$I_m, R_m \rightarrow$ meter
current & resistance
respectively.

I_{fs} = full scale
(or) deflection
current
 $I_m =$

R_{se} = series resistance (or) multiplier

V_m = voltage across meter

V = extended voltage

$$\therefore V_m = I_m R_m \quad \text{--- (1)}$$

$$V = I_m (R_m + R_{se}) \quad \text{--- (2)}$$

Dividing eqⁿ (2) by eqⁿ (1)

$$\frac{V}{V_m} = \frac{R_m + R_{se}}{R_m}$$

$$\Rightarrow \frac{V}{V_m} = \frac{1 + R_{se}}{R_m}$$

$$\Rightarrow R_{se} = \left(\frac{V}{V_m} - 1 \right) R_m$$

$$R_{se} = (N - 1) R_m$$

where N = multiplying factor

$$\Rightarrow N = \frac{R_{se} + 1}{R_m}$$

Q- A voltmeter has rating 0.25 V . If we want to extend its range, ~~what~~^{what} will be the multiplying factor, upto 10 V .

What will be the series resistances to be connected if

$$R_m = 25 \Omega$$

$$\Rightarrow 40 = \frac{R_{se}}{25} + 1$$

$$\Rightarrow 40 = 25 + R_{se}$$

$$\Rightarrow 40 \times 25 = 25 + R_{se}$$

$$\Rightarrow R_{se} = 40 \times 25 - 25$$

$$= 975 \Omega$$

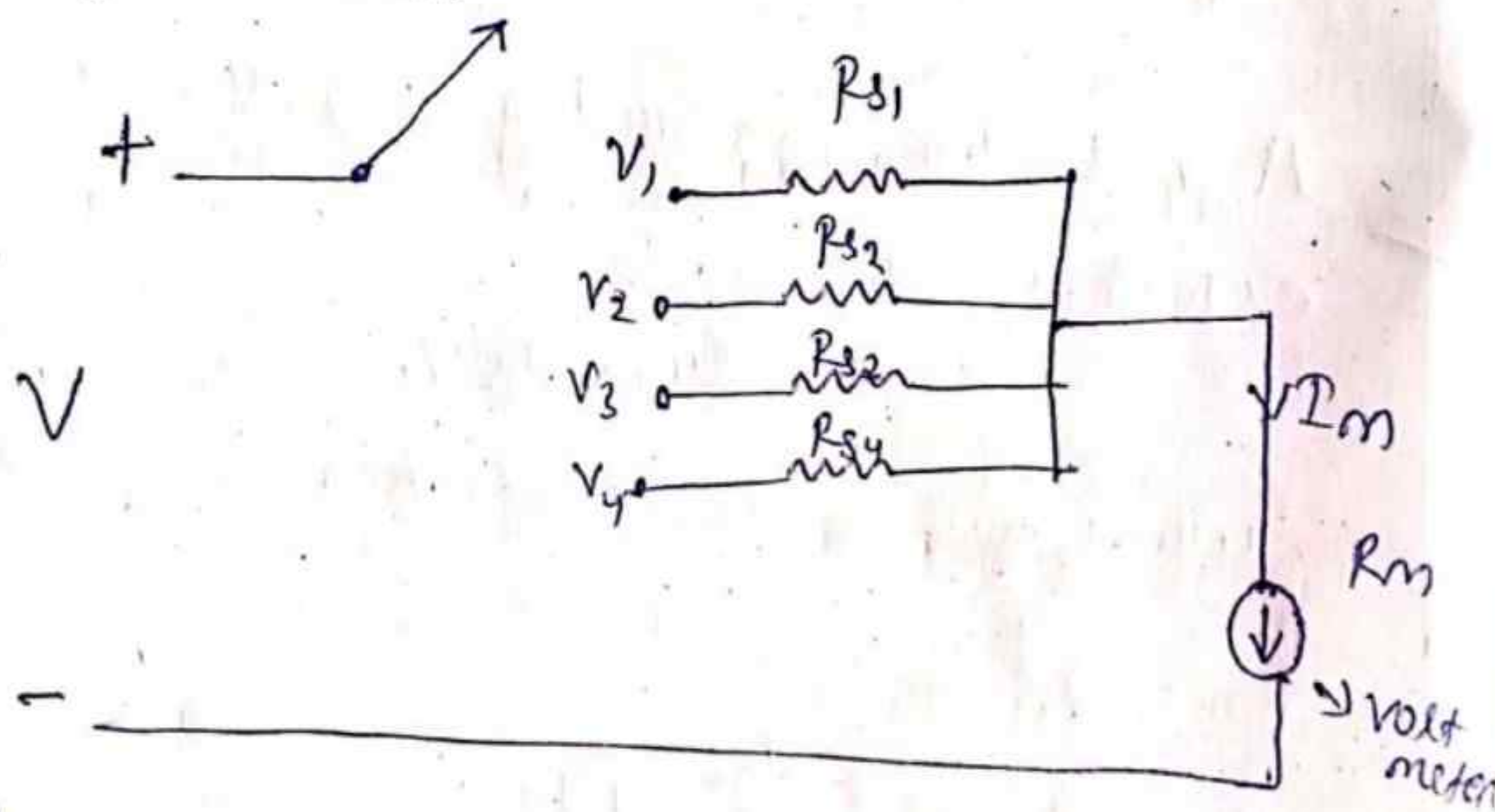
Material for voltmeter multiplier :-

- Their resistance should not change with time.
- Change in their resistance with temp. should be small.
- normally the material used for multiplier is Mn, constantan (alloy of Cu, Ni).



Extension range of voltmeter

Multirange volt meter



Multiplying factor,

$$N_1 = \frac{V_1}{V_m}, N_2 = \frac{V_2}{V_m}, N_3 = \frac{V_3}{V_m}, N_4 = \frac{V_4}{V_m}$$

$$R_{s1} = R_m (N_1 - 1)$$

$$R_{s2} = R_m (N_2 - 1)$$

$$R_{s3} = R_m (N_3 - 1)$$

$$R_{s4} = R_m (N_4 - 1)$$



Voltmeter extension potential division method :-

$$R_1 = R_m (N_1 - 1)$$

$$N_1 = \frac{V_1}{V_m}$$

$$R = 9, \quad \frac{V_2}{I_m} = R_1 + R_m + R_2$$

$$\Rightarrow \frac{V_2}{I_m} = R_m (N_1 - 1) + R_m + R_2$$

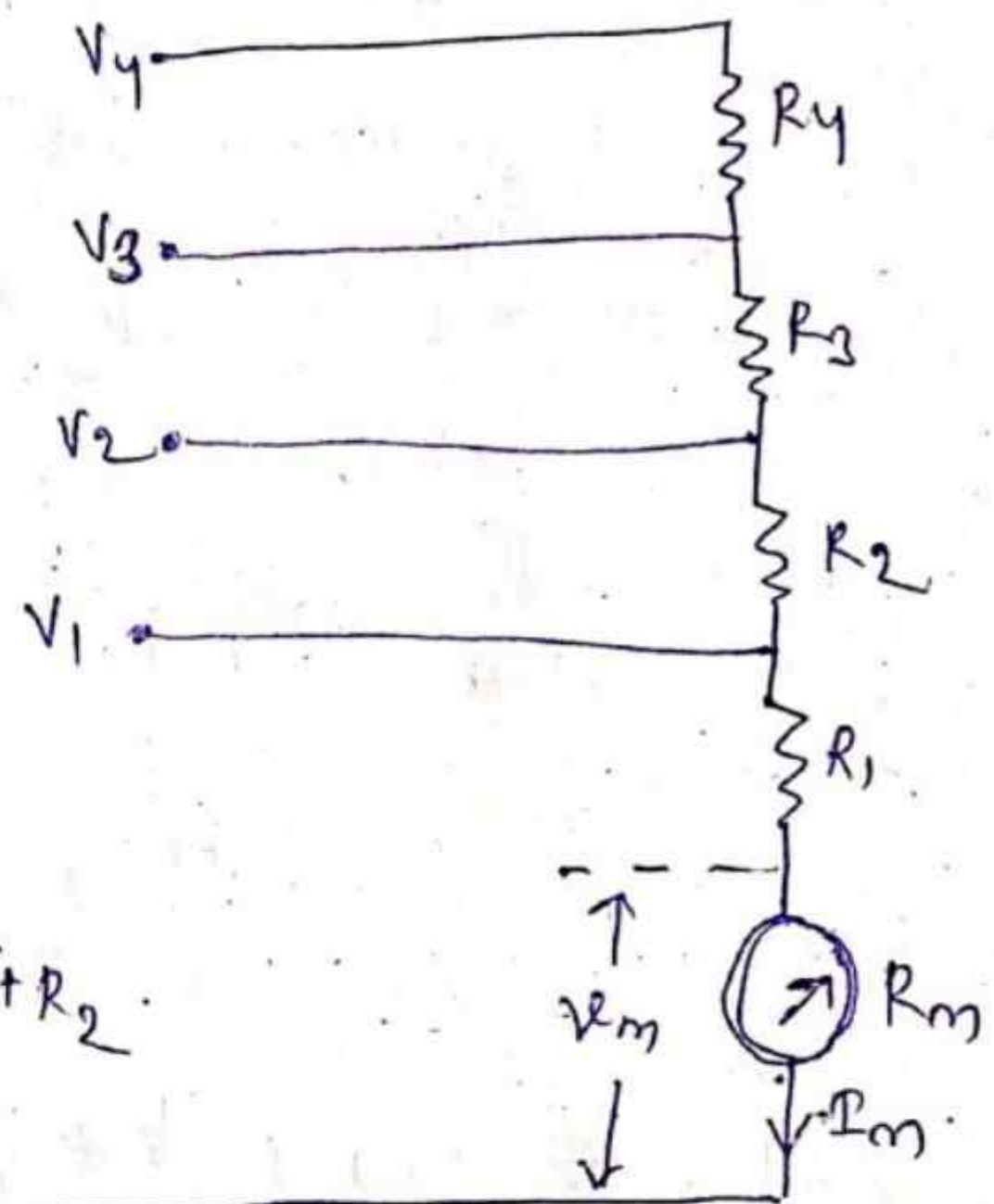
$$\Rightarrow \frac{V_2}{I_m} = R_m N_1 - R_m + R_m + R_2$$

$$\Rightarrow \frac{V_2}{I_m} = R_m N_1 + R_2$$

$$\Rightarrow \frac{V_2}{\left(\frac{V_m}{R_m}\right)} = R_m N_1 + R_2$$

$$\Rightarrow N_2 R_m = R_m N_1 + R_2$$

$$\Rightarrow \boxed{R_m (N_2 - N_1) = R_2}$$



Similarly R_3 and R_4 becomes,

$$R_3 = (N_3 - N_2) R_m \quad N_3 = \frac{V_3}{V_m}$$

$$R_4 = (N_4 - N_3) R_m \quad N_4 = \frac{V_4}{V_m}$$

Q. A PMMC instrument having resistance of $100\ \Omega$, current of 1mA is subjected for the extension of voltage range of 100V , 300V , and 600V , find the individual resistances to be placed in series in potential division extension.

$$R_m = 100\ \Omega, \quad I_m = 1\text{mA} = 10^{-3}\text{A}$$

$$V_1 = 100\text{V}, \quad V_2 = 300\text{V}, \quad V_3 = 600\text{V},$$

$$V_m = I_m \cdot R_m = 100 \times 10^{-3}$$

$$R_{s1} = 100 \left(\frac{100}{100 \times 10^{-3}} - 1 \right) = 999000\ \Omega = 99.90\text{K}\Omega$$

$$R_{s2} = 100 \left(\frac{300}{100 \times 10^{-3}} - 1 \right) = 299900\ \Omega = 29.99\text{K}\Omega$$

$$R_{s3} = 599900\ \Omega = 59.99\text{K}\Omega$$

$$100 \left(\frac{N_2}{N_1} - 1 \right)$$

$$R_1 = R_m (N_1 - 1)$$

$$= 100 \left(\frac{100}{100 \times 10^{-3}} - 1 \right) = 999000 = 99.90\text{K}\Omega$$

$$R_2 = R_m (N_2 - N_1) = 100 \left(\frac{300}{100 \times 10^{-3}} - \frac{100}{100 \times 10^{-3}} \right)$$

$$= 2000000 \text{ K}\Omega$$

$$R_3 = \left(\frac{.600}{100 \times 10^{-3}} - \frac{.300}{100 \times 10^{-3}} \right) 100 = 2000000 \text{ K}\Omega$$

Errors in PMMC instrument &

- (i) Frictional error
 - (ii) Error due to coil
 - (iii) Error due to spring
 - (iv) " " magnet
 - (v) " temperature rise
- (iv) The permanent magnet are aged by heat and vibration treatment. this process results in the loss of initial magnetism but that remains is strongly head.
- The weakening of magnets tends to decrease the deflection for a particular value of current.
- (iii) The weakening of spring with time can be reduced by careful use of material and pre-aging during manufacture.
- The weakening of springs tends to increase the deflection.
- (v) In PMMC instruments, a 1°C increase of temperature reduces the strength of springs by about 0.04% and reduces flux density in the air gap of the

magnet by about 0.02 % . Thus the net effect on the average, is to increase the deflection by about 0.02 % per $^{\circ}\text{C}$.

(ii) The moving coil of a measuring instruments usually wound with copper wire having a temperature coefficient of 0.004/ $^{\circ}\text{C}$.

→ When the instruments used as a micro ammeter or a milli-ammeter and the moving coil is directly connected to the output terminals of the instrument.

→ The indication of the instrument for a constant would decrease by 0.04 percent per $^{\circ}\text{C}$ rise in temperature.

i) The friction of the pivot in the Jewel produces a frictional torque which affects the instruments reading. This error is more serious for sensitive instruments designed for low operating torque .

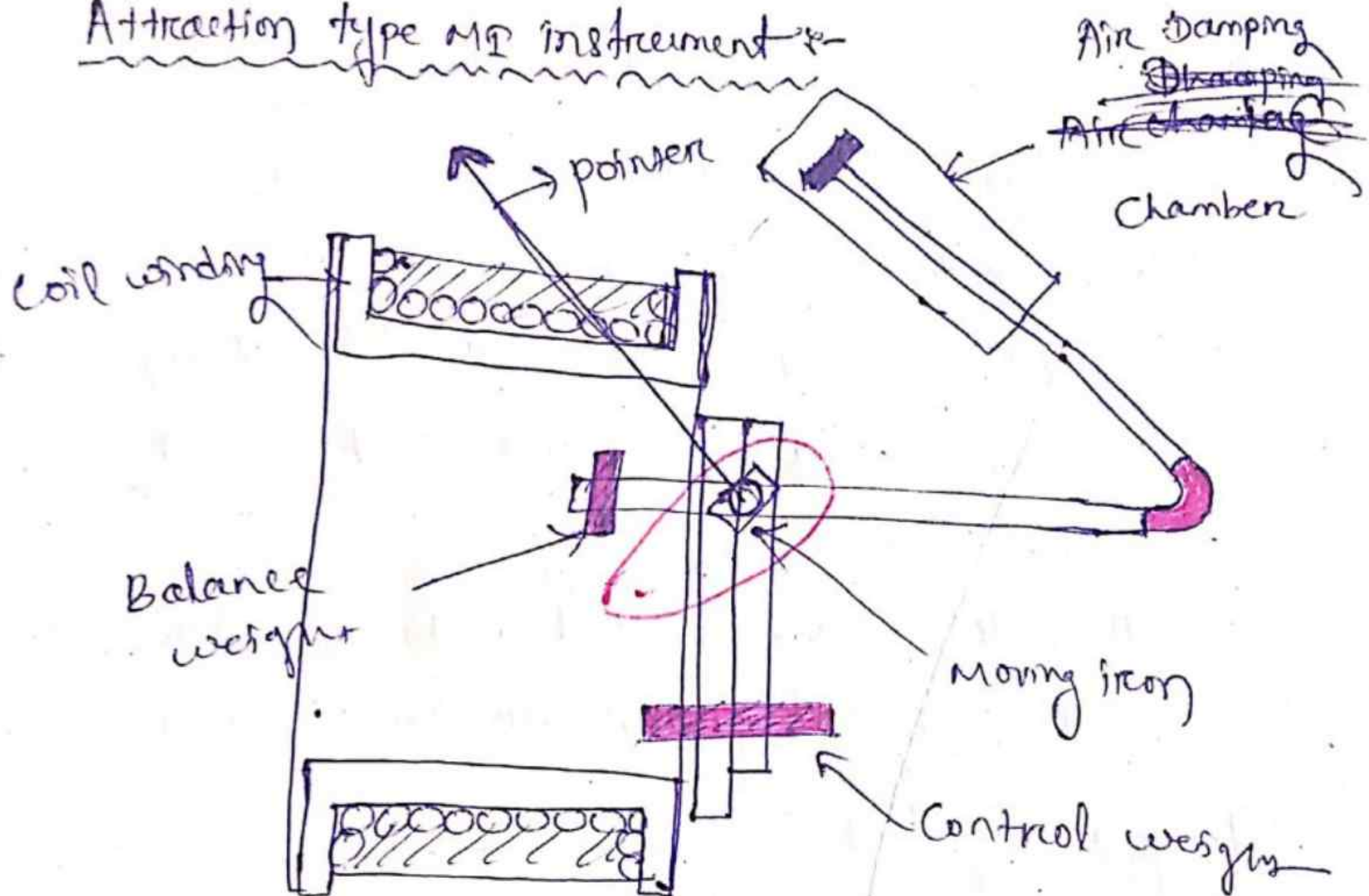
→ These errors may be reduced by adopting a moving system of light construction and large deflecting torque.

(iv) The error owing to weakening of permanent magnet can be reduced by proper attention to ageing and reasonable care in use .

(v) Change of temperature affects the instruments resistance and stiffness of the control spring this is due to heating of the working coil and other resistance coils connected internally in the instrument causing by the operating current.

Moving iron instrument

Attraction type MI instrument



Construction

It consists of a stationary hollow cylindrical coil (Electromagnet), and an oval shaped soft iron piece is mounted ~~centrically~~ to the spindle to which pointer is attached.

→ The controlling torque is provided by gravity control method.

→ The Damping torque is provided by Air friction Damping.

Working Principle

When a soft iron piece is placed in a magnetic field of a current carrying coil, it is

attracted towards the center of the coil or magnetic field.

Working :-

When the instrument is connected to the ckt, the operating current flows through the stationary coil, and a magnetic field is set up by which the soft iron piece is attracted towards the center of the coil.

thus the pointer attached to the spindle gets deflected and moves over the calibrated scale.

Torque equation :-

Deflecting torque :-

$$F \propto mH$$

where m = force act on moving iron.

H = Magnetic field strength produced by the coil.

$$H \propto I$$

$$m \propto H, \quad m \propto I$$

$$F \propto I^2$$

$$\Rightarrow T_d \propto I^2$$

The deflecting torque is expressed as,

$$T_d = \frac{1}{2} I^2 \frac{dL}{d\theta}$$

where

T_d = Deflecting torque

L = self inductance

I = Operating current

θ = Angle of deflection

$\frac{dL}{d\theta}$ = Rate change of self inductance

Date - 01/02/2020

Controlling torque:-

when the control is gravity control,

$$T_c = Wgl \sin \theta$$

and when it is spring control,

$$T_c = K\theta$$

Let's consider spring control is used, then steady state is obtained when $T_d = T_c$

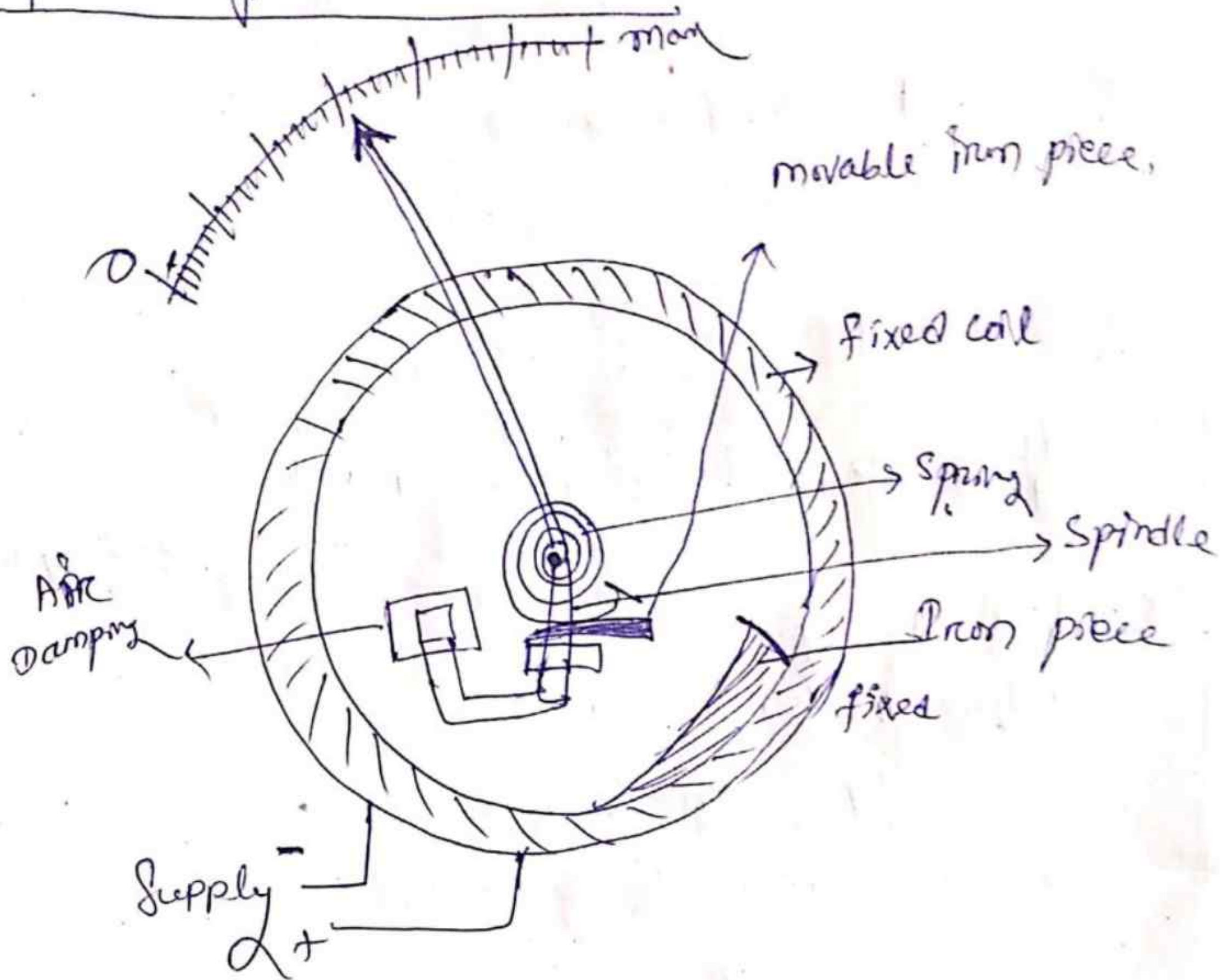
$$\Rightarrow \frac{1}{2} I^2 \frac{dL}{d\theta} = K\theta$$

$$\Rightarrow \theta = \frac{1}{2K} I^2 \frac{dL}{d\theta}$$

$$\Rightarrow \theta \propto I^2$$

from this eqⁿ it is observed the scale is non uniform

Repulsion type MI Instrument



Construction:-

It consists of a fixed cylindrical hollow coil (electromagnet) which carries operating current. Inside the coil two soft iron pieces i.e. rods are placed parallel to each other and along the axis of the coil.

- One iron piece is fixed that is attached to the coil and another one is ~~fixed which is attached~~ movable i.e. attached to the spindle.
- A pointer is attached to the spindle with spring

Control mechanism and air friction damping arrangement,
Working :-

When the instrument is connected to the ckt the operating current flows through the fixed coil. Due to this a magnetic field is setup ~~in~~ along the axis of the coil. This magnetic field magnetised both the iron pieces in the same polarity.

→ Due to this a force of repulsion acts betⁿ two iron pieces. There by the movable iron piece moves away from fixed iron piece, so that the pointer attached to the spindle deflects over the calibrated scale.

Application of MI Instrument :-

- (i) This is used as volt meter, ammeter, wattmeter etc.
- (ii) This is used in both A.C. and D.C.
- (iii) MI Instrument are used up to the frequency of 125 Hz.

Advantages :-

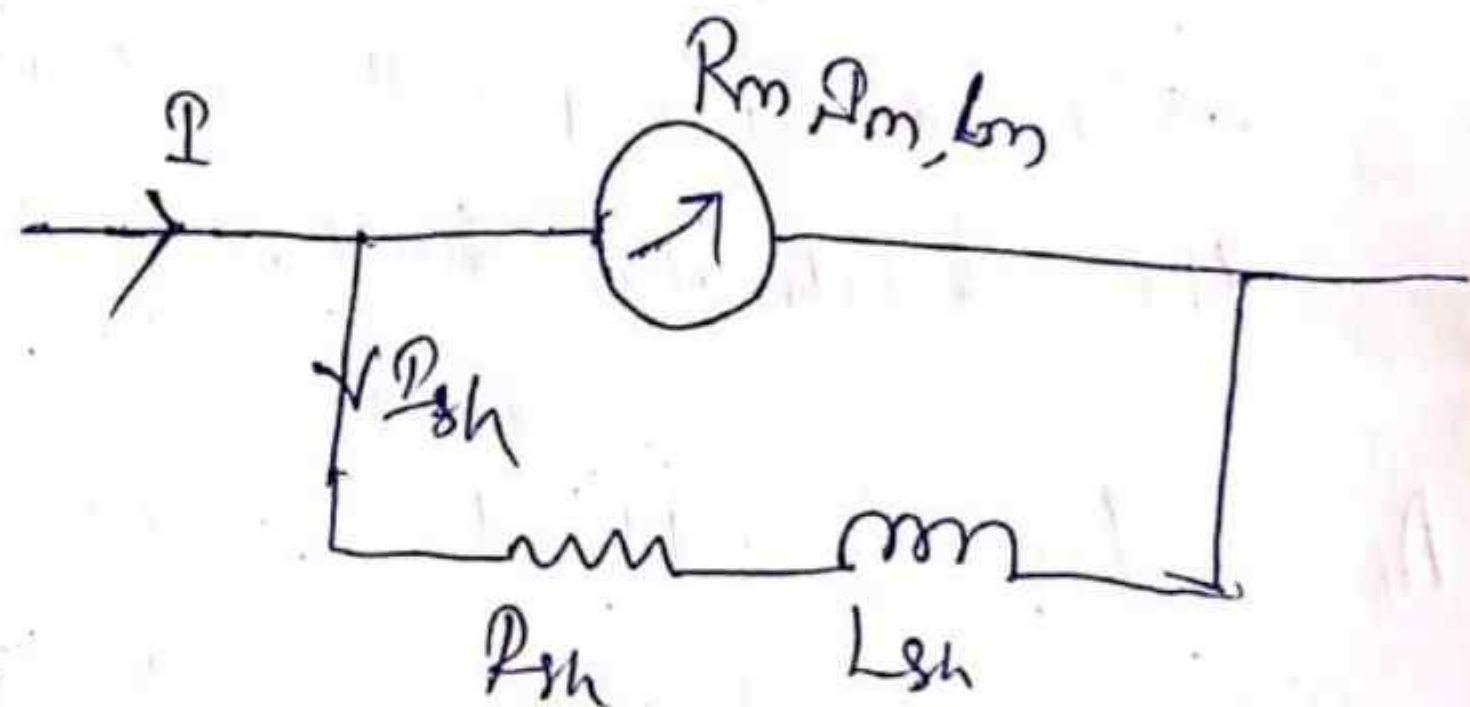
- (i) These instruments are cheap, ~~Robust~~ and simple in construction.
- (ii) These instruments can be used on both AC and DC.
- (iii) These instruments are reasonably accurate.
- (iv) MI Instruments possesses high operating torque.

Disadvantages:-

- ① M.I. Instruments have non uniform scale.
- ② These Instruments are not very sensitive.
- ③ Power consumption is quite high.

④ Errors are introduced due to change in frequency in case of AC measurement.

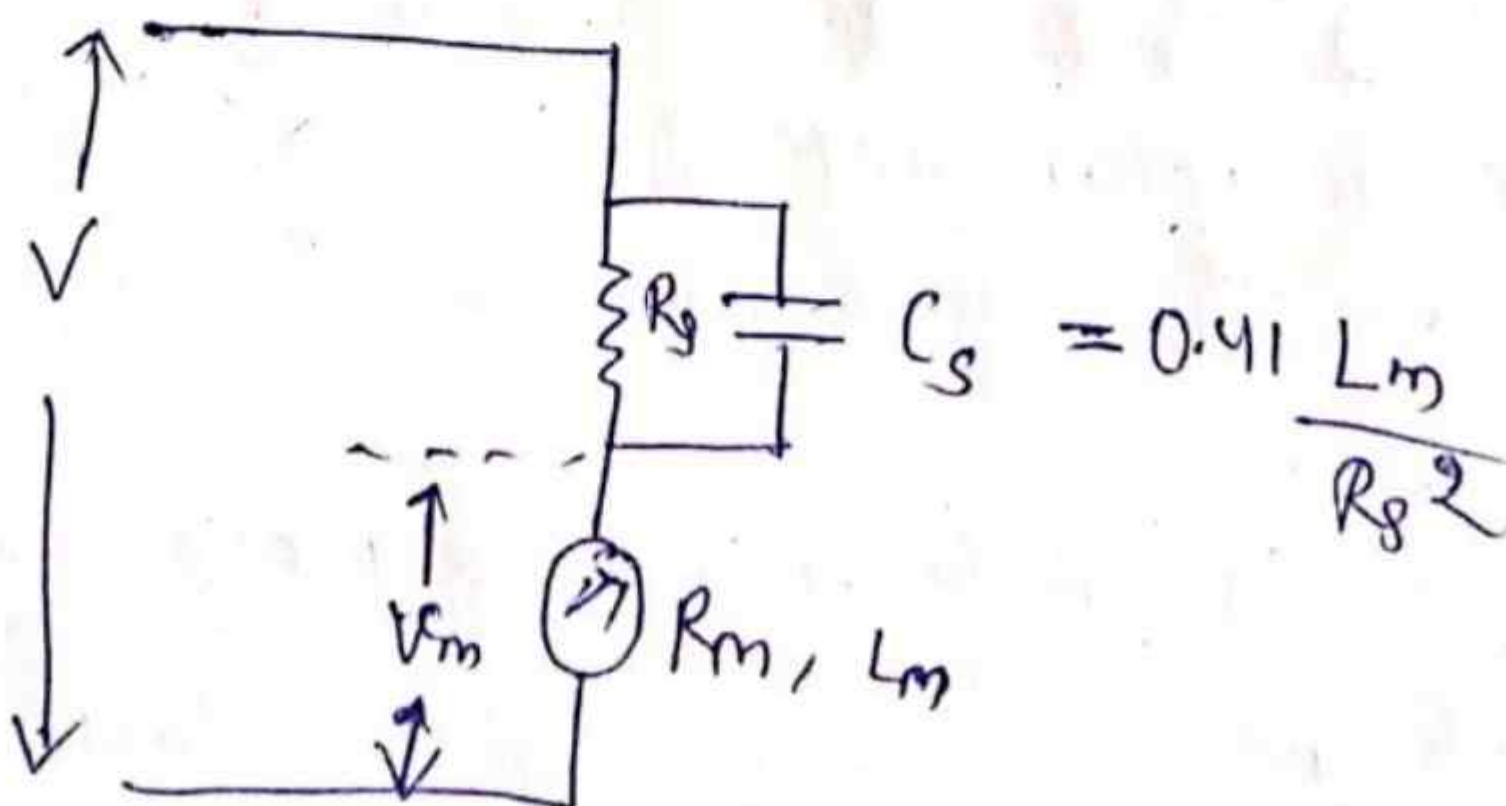
M.I. Instruments as ammeter:-



$$Z_1 = Z_2$$

$$\Rightarrow \frac{I_{sh}}{I_m} = \frac{L_m}{R_m} \quad (\text{Time constant})$$

M.I. Instrument as voltmeter:-



Error in MI instruments :-

There are two types of error which occur in moving iron instruments.

① Errors with both A.C. and D.C. work:

(a) Hysteresis error.

~~(b) Stray magnetic field error.~~

(c) Temperature error.

(d) Friction error.

② Errors with A.C. work only :-

(a) Frequency error

(b) Error due to reactance of instrument coil.

(c) Error due to eddy current.

~~(d) Error due to wave form.~~

(a) Hysteresis error :- It is a serious type of error in MI instruments when used on D.C. circuits. The effect of this error is that the readings are higher when current increases than when it decreases.

This error can be reduced by employing vanes of Mumetal (i.e. Mumetal is magnetic material having low hysteresis loss and high permeability) and by working it over a low range of flux densities.

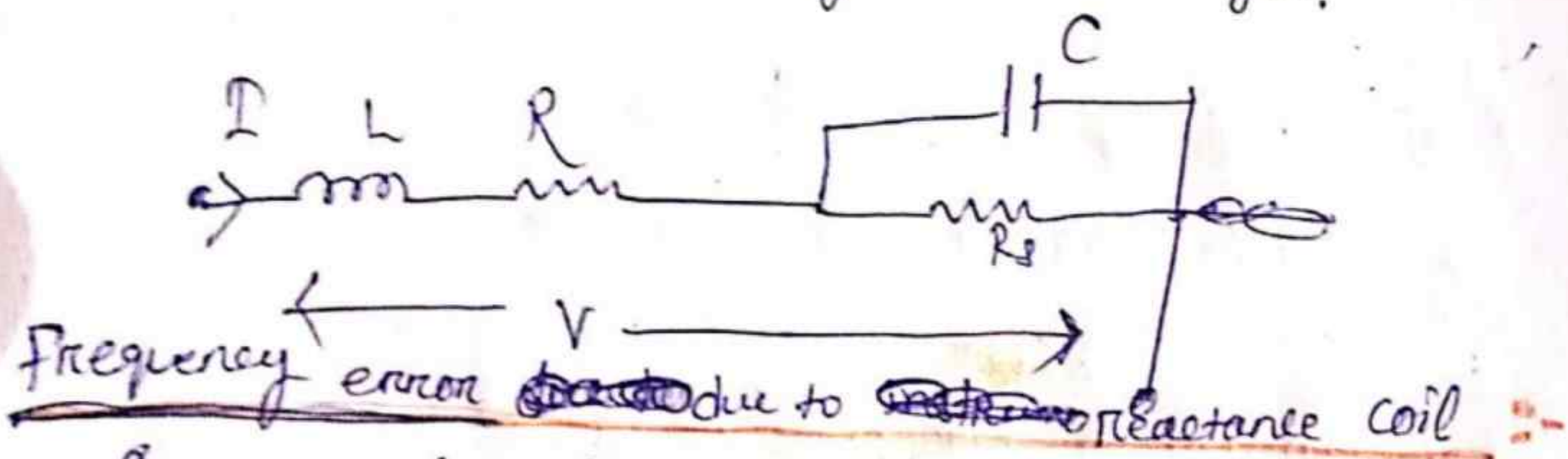
(b) Temperature error is due to change of temperature that affects the instrument resistance and stiffness of the control spring.

(c) Friction error is due to the friction of moving parts this can be avoided by making torque-weight ratio high.

③ Frequency errors - change in frequency may be cause errors due to change of reactance of the operating coil and also to the changes in magnitude of eddy current set up in the metal parts of instrument near the operating coil.

④ error due to the instrument coil the change in instrument coil reactance owing to change in frequency causes serious error in case of volt meters.

⑤ Eddy current error affects both ammeters and volt meters equally. the frequency error may be compensated for by connecting a suitable capacitor 'C' in the parallel with swamping resistance R_s ($C = L/R^2$, if frequency is not too high).



In case of volt meter a series resistance is connected with the coil, where I is the instrument current, ' V ' is the applied voltage.

as we know that, $I = \frac{V}{Z}$

$$Z = (R + R_s) + j\omega L$$

$$\Rightarrow I = \frac{V}{\sqrt{(R + R_s)^2 + (\omega L)^2}}$$

$$\rightarrow I = \frac{V}{\sqrt{(R+R_s)^2 + \omega^2 L^2}}$$

$$\Rightarrow T_d \propto I \propto \frac{1}{\omega}$$

From this relation we know that T_d depends on the current through the coil and current is inversely proportional to the frequency, so for given voltage deflecting torque is less at high frequency than low frequency.

This can be compensated by connecting a capacitor 'C' across the series resistance 'R_s'.

Frequency error due to change in magnitude of eddy current setup in metallic ~~inductor~~ part.

This error is caused by the eddy current induced in the iron part of the instrument.

hence there will be change in main magnetic field due to induced field.

→ This can affect the operating current and also frequency.

→ This can be minimized by ~~reducing~~ ^{minimizing} the metallic part of the instrument.

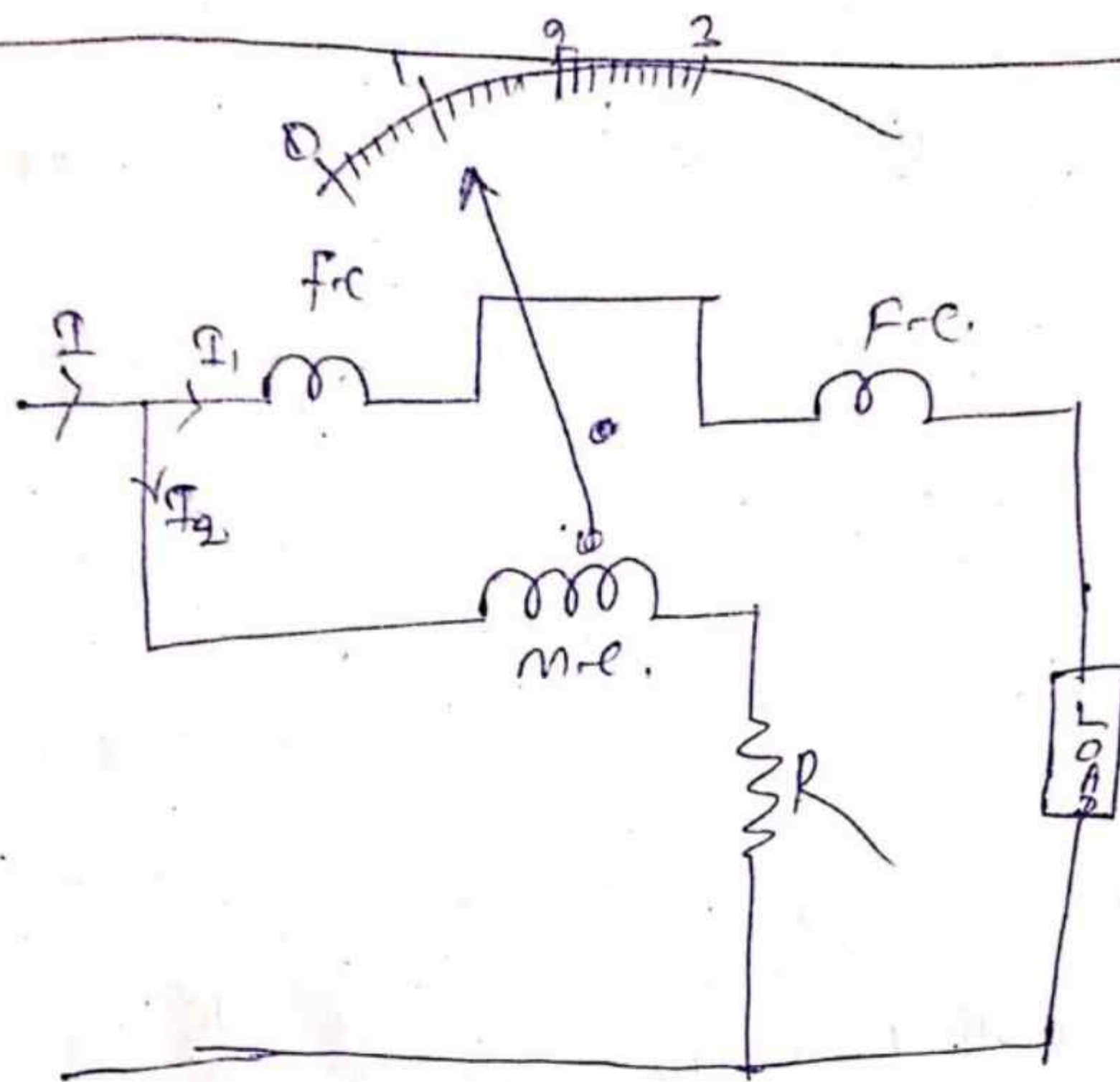
Electrodynamometer type instrument

Construction :-

- It consists of a fixed coil, which is split into two parts and placed parallel to each other.
- The fixed coils are cone to eliminate the hysteresis loss.
- A moving coil is placed in betⁿ the fixed coils.
- The moving coil is attached on the spindle with spring and pointer (or) moving system.
- A high resistance is connected in series with the moving coil to ~~limit~~ limit the current.
- The connection of fixed coil and moving coil are different by their uses as an ammeter, voltmeter & wattmeter.
- The control torque is provided by spring control mechanism and Damping torque is provided by air friction damping.

Principle :-

When a current carrying ^{moving coil} ~~conductor~~ is placed in the magnetic field. ~~force~~ of produced by current carrying fixed coil. Then a force is exerted on the coil sides of the ^{moving coil} ~~and deflection~~ and deflection takes place.



~~as~~ The fixed coil are connected in series with the load. and the moving coil is connected in parallel with the load.

Operation :-

when the load is connected to the instrument and supply is given to the instrument then current starts flowing through both the coil.

Let, I_1 = current flowing through F.C.

I_2 = current " " M.C.

$I_1 \propto I_{load}$ and $I_2 \propto V_{load}$.

Both the coil produced magnetic field around them, the operating field (F_m) is produced by the fixed coil, and another magnetic field (F_R) is produced by the moving coil.

Then both the field interact with each other ~~and~~ and the magnetic field produced by moving coil tries to come in line with operating magnetic field, due to which moving coil gets deflected and by which pointer deflects;

The deflecting torque produced can be estimated as

$$T_d \propto I_1 I_2$$

$$T_d = \frac{dM}{d\theta} I_1 I_2 \quad (\text{for DC})$$

where M = mutual inductance betⁿ fixed coil;

and $\frac{dM}{d\theta}$ = It is the rate of change of mutual inductance w.r.t θ ^{angle of deflection}.

~~Result~~

For AC

T_d can be estimated as

$$T_d = I_1 I_2 \cos \phi \frac{dM}{d\theta}$$

where $I_1, I_2 \rightarrow$ RMS value

Controlling torque is-

As control torque is provided by spring
Control T_c can be represented by

$$T_c = K\theta$$

The pointer remains steady position when both the torques are equal i.e. $T_c = T_d$

① For dc

$$T_d = T_c$$

$$\Rightarrow I_1 I_2 \frac{dm}{d\theta} = K\theta$$

$$\Rightarrow \boxed{\theta = \frac{1}{K} I_1 I_2 \frac{dm}{d\theta}}$$

② For Ac

$$T_d = T_c$$

$$\Rightarrow I_1 I_2 \frac{dm}{d\theta} \cos\theta = K\theta$$

$$\Rightarrow \boxed{\theta = \frac{1}{K} I_1 I_2 \cos\theta \frac{dm}{d\theta}}$$

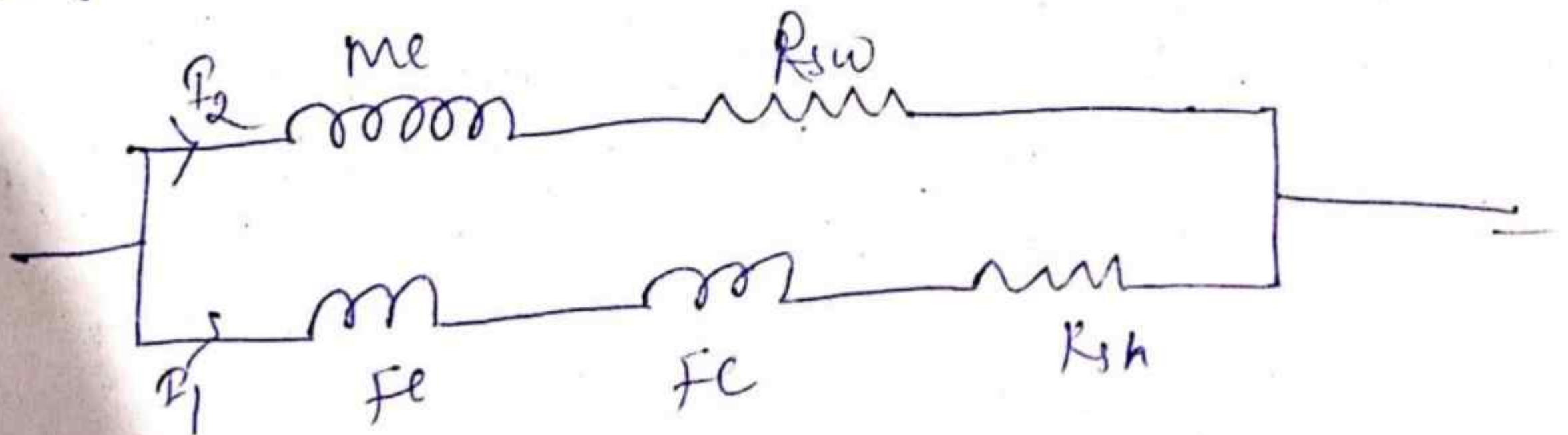
Application:-

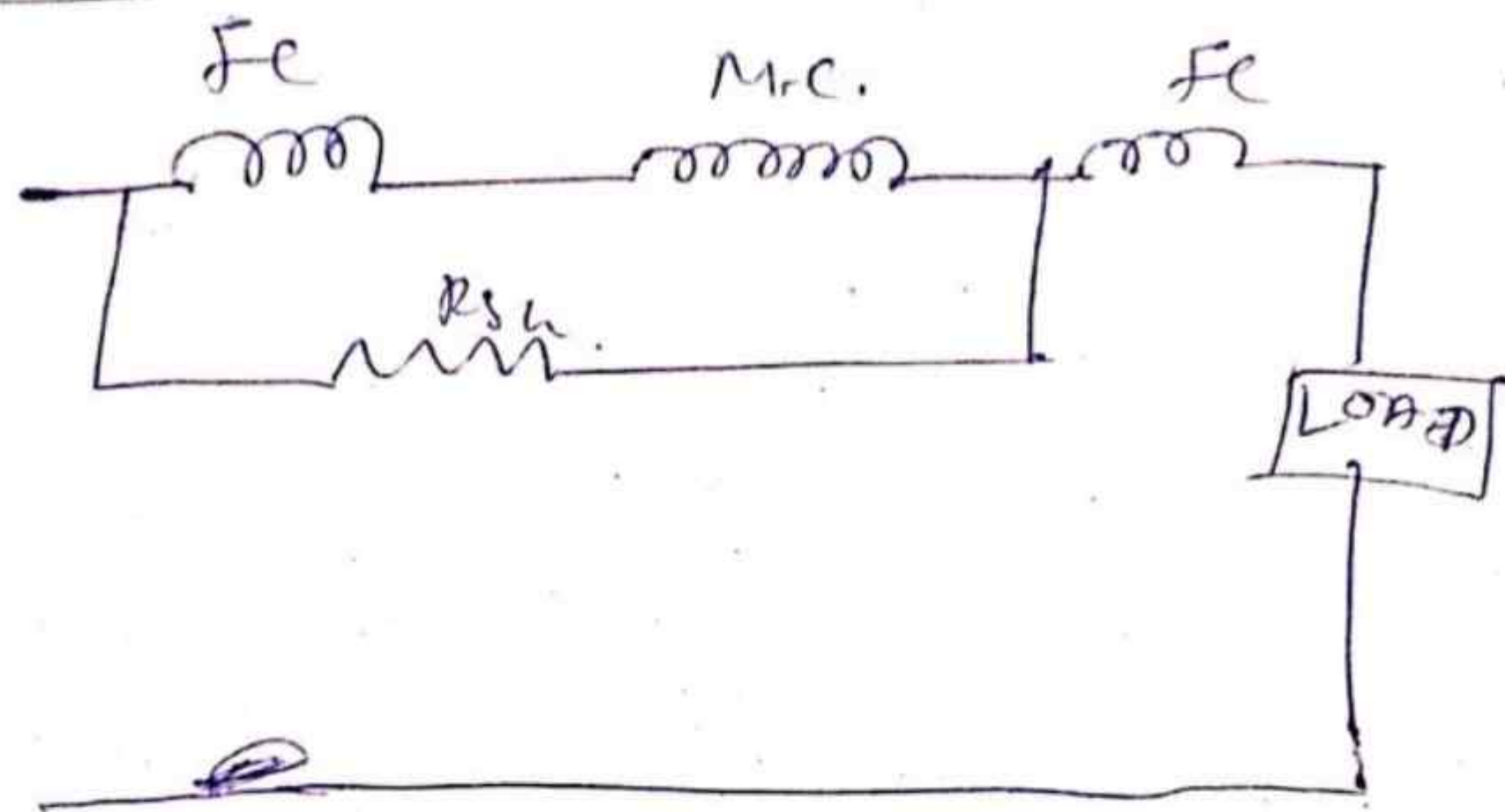
→ ^{meter} ~~Dynamometer~~ type instruments can be used as ammeter, voltmeter, wattmeter.

→ These are used in both Ac and dc measurement.

→ This instruments is known as transfer instruments, because ~~if it~~ ^{if it} is calibrated on DC ~~it~~ can be used in ac.

Dynamometer type instrument as an ammeter :-





For measurement of current the resistance of instrument kept low so that a shunt resistance is connected in the fixed coil branch, which is shown in the figure. here the relation betⁿ deflection and current,

→ This type of connection is adapted for currents $> 100\text{mA}$.

For operating current less than 100mA fixed coil and ~~fixed~~ moving coil are connected in series.

Dynamo meter type instrument as voltmeter.

The sensitivity of voltmeter ^{can be} increased by increasing the

so that both the coils are connected in series

which are shown in the figure.

Relation betⁿ angle of deflection and current is as

$$\theta = \frac{1}{K} I_1 I_2 \frac{dm}{d\theta}$$

$$\text{here, } I_1 = I_2 = I = \frac{V}{Z}$$

where V = load voltage

Z = impedance of the ckt.

So putting this value in above eqⁿ we found that,

$$\Rightarrow \theta = \frac{1}{K} I^2 \frac{dm}{d\theta}$$

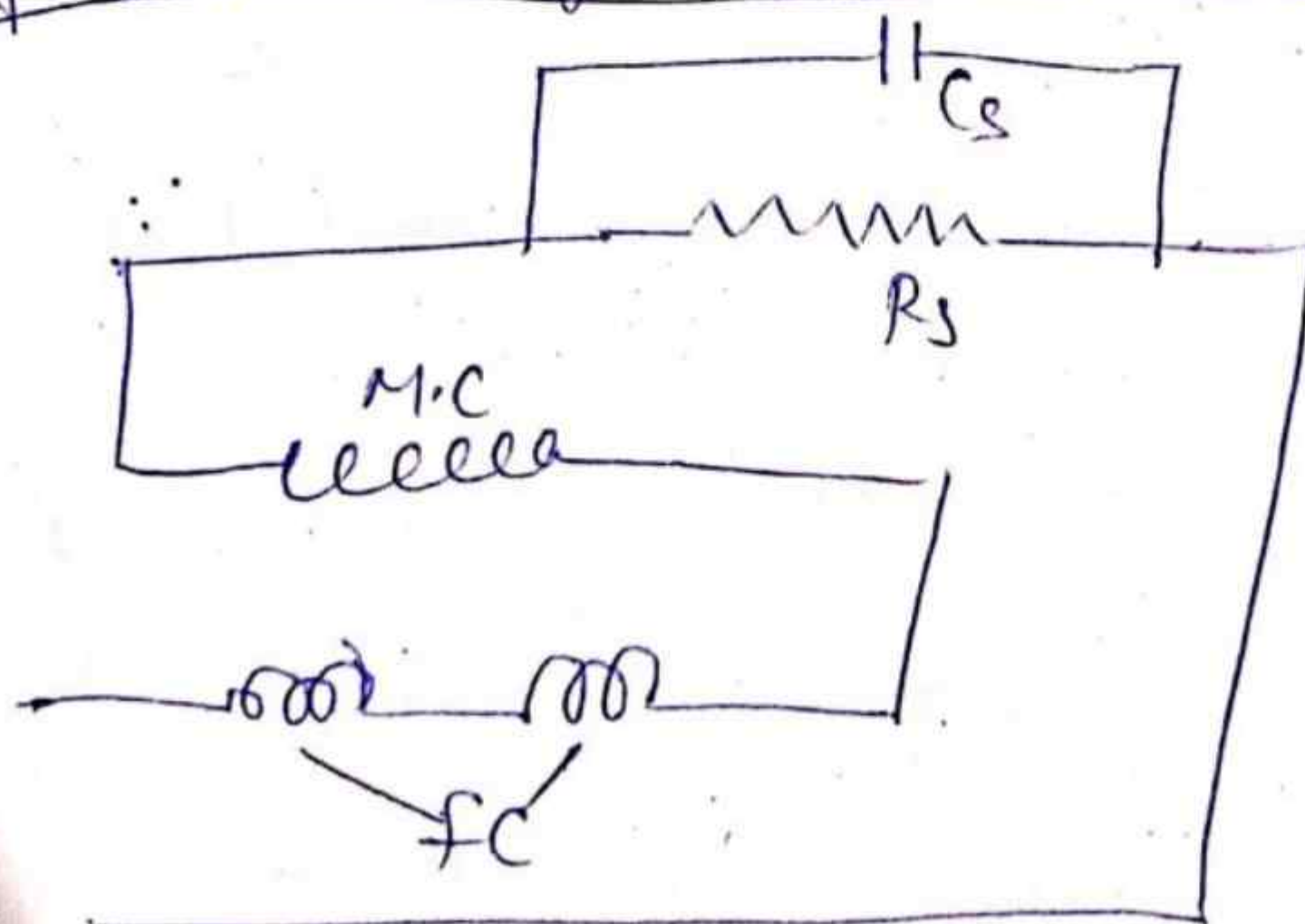
$$\Rightarrow \theta = \frac{1}{K} \frac{V^2}{Z^2} \frac{dm}{d\theta}$$

~~we find~~ from this we found that,

$$\theta \propto V^2$$

So in this instrument the scale is non uniform.

~~By using meter type instrument as an example~~



Error in dynamometer type instrument :-

① Frictional error :- here the coils are air core so the magnetic field produced is small. Therefore it requires large no. of ampere turns to create necessary deflecting torque. This results heavy moving system. So it has small torque by weight ratio.

Due to heavy moving system frictional error (or) losses in this instrument is large as compare to other instruments.

here hysteresis loss is also zero, as the coils are ~~air~~ air core.

② Temp. error :-

This instrument considerable amount of power so self heating in this instrument is appreciable. To compensate this swamping resistance made up of manganin are used.

③ Error due to stray magnetic field :-

Since the operating field produced by fixed coil is weaker in comparison to other instruments this is more sensitive to stray magnetic field.

④ Frequency error :-

A change in frequency causes error.

① due to change in reactance of the operating coil.

- ⑪ due to change in magnitude of eddy current set up in the metallic part of the instrument.

Advantages :-

- ① This Instruments can be used on both AC and DC.
- ② It is free from hysteresis and eddy current errors.
- ③ It follows square law calibration.
- ④ Ammeter upto 10 amp and voltmeter upto 600V can be constructed with Precision grade accuracy.
- ⑤ Because of precision grade accuracy and same calibration for dc and Ac measurement this instrument used as transfer instruments.

Disadvantages :-

- ① It has non uniform scale.
- ② small torque by weight ratio.
- ③ Large Frictional error.
- ④ Costly as compare to pmmc and MI Instruments.
- ⑤ Easily affected by stray magnetic field.
- ⑥ Sensitivity of instrument is very low due to poor deflecting torque.

Induction type instrument :-

In this instrument the deflecting torque is produced by the principle of induction. hence the name. ~~and~~
this instrument is only used for AC measurement.

Working principle :-

When a disc of conducting material is placed in a rotating magnetic field (or) magnetic field produced by electromagnet with some phase difference then eddy currents are induced in it.

→ The reaction betⁿ rotating field and eddy current creates torque which rotates the disc. by which pointer gets deflected.

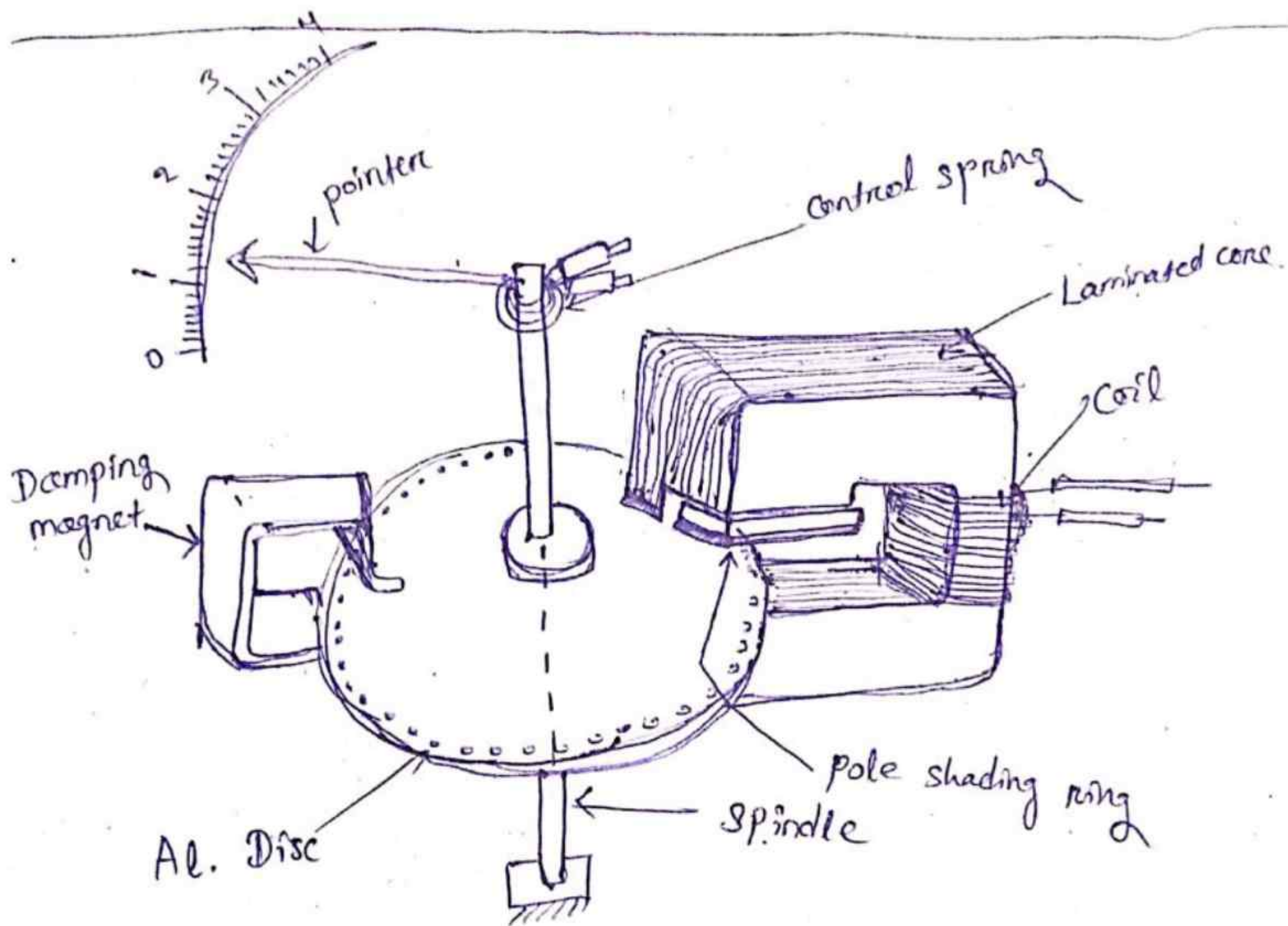
Induction type instrument is of two types,

- (i) Shaded pole type.
- (ii) split phase type.

(i) Shaded pole type :-

Construction:- It consists of electromagnet which is ~~shaded in~~ shaded in one part to provide phase difference betⁿ the fluxes.

The shape of the core is same as transformer in betⁿ the poles. A disc is placed which is attached in the spindle. The moving system i.e. pointer & the control system is also attached to the spindle, and a



damping magnet (break magnet) is provided in other end of the disc.

Working:-

When the supply is given to the coil of electromagnet it draws two different current i.e. I_1 and I_2 due to different resistance ~~and~~ (or) reluctances.

Due to this two fluxes are set up that is ϕ_1 and ϕ_2 . This ϕ_1 and ϕ_2 have some phase difference betⁿ them. So a rotating magnetic field is set up.

As this magnetic links with aluminium disc. Then emf is induced in the disc by which eddy current are set up in the disc.

Let the eddy currents are I_{e1} and I_{e2} due to the interaction of ϕ_1 and I_{e2} and ϕ_2 and I_{e1} .

The torques are produced in the disc. Let the torque

Let the torque are, $T_1 \propto \phi_1 I_{e2}$

$$\Rightarrow T_1 = K \phi_1 I_{e2} \cos(90 + \beta)$$

$$\Rightarrow \boxed{T_1 = -K \phi_1 I_{e2} \sin \beta}$$

$$T_2 \propto \phi_2 I_{e1}$$

$$\Rightarrow T_2 = K \phi_2 I_{e1} \cos(90 - \beta)$$

$$\Rightarrow \boxed{T_2 = K \phi_2 I_{e1} \sin \beta}$$

$$\therefore T_d = T_2 - T_1 \text{ (or) } T_1 - T_2$$

$$\Rightarrow T_d = T_2 - T_1 = 2K \phi_1 \phi_2 \sin \beta$$

$$\Rightarrow T_d \propto \phi_1 \phi_2$$

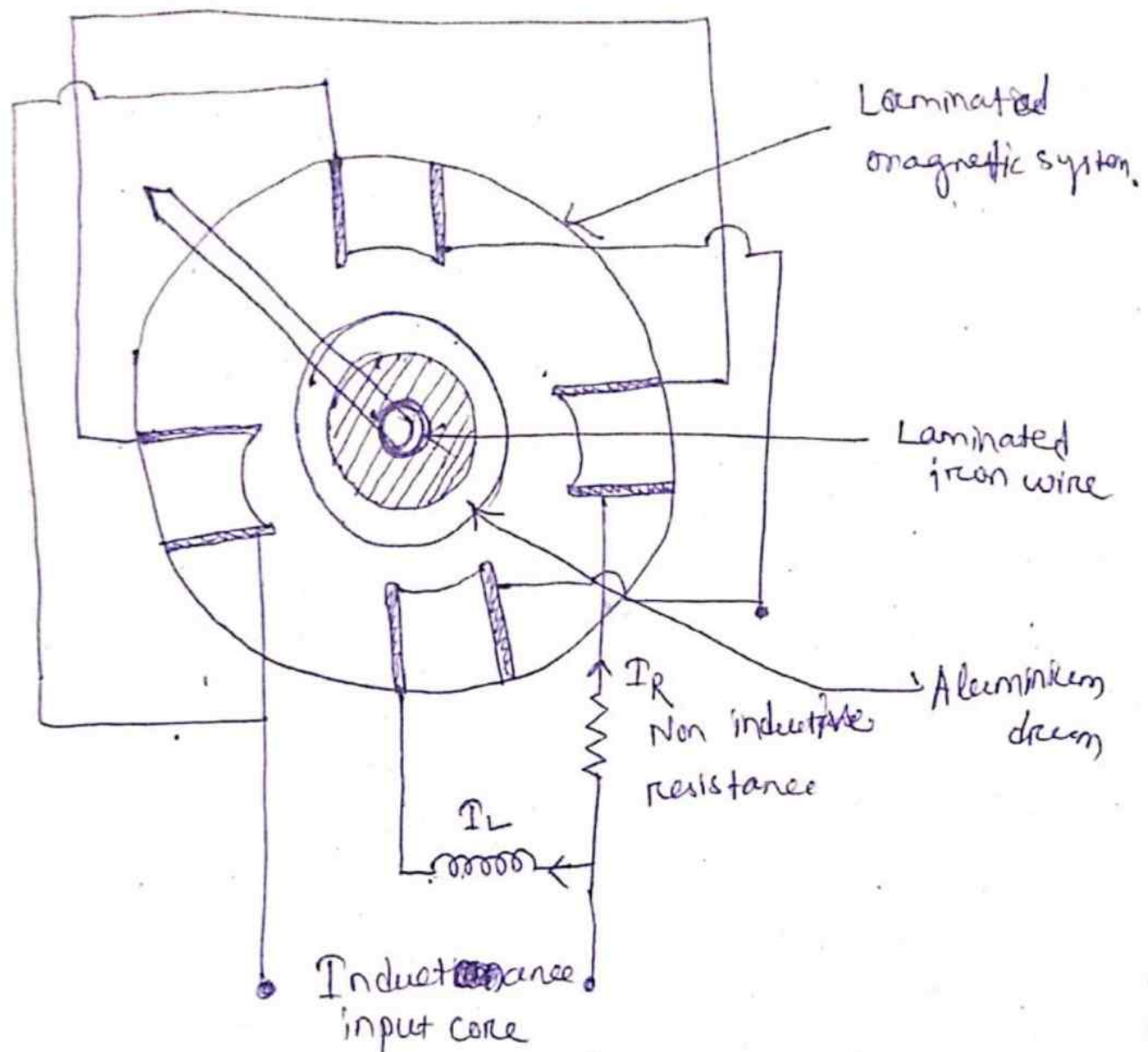
$$\Rightarrow T_d \propto I^2$$

Then the ~~deflecting~~ deflecting torque can be estimated by the resultant of T_1 and T_2 .

$$\text{So } T_d = T_2 - T_1 \quad (\beta = \text{phase difference bet}^n \phi_1 \text{ and } \phi_2)$$

$$(I = \text{operating current} / \text{supply current})$$

here the control spring is provided by spring control mechanism and damping is by break magnet.
more the phase split more be the phase difference.

Split phase type :-Construction :-

It consists of a laminated magnet with the pairs of ^{are} poles at right angle to each other. coils ^{are} wound on the poles and opposite poles are connected in series and the coils ~~are~~ on the the 2 pairs of poles are connected in parallel,

one set of coil is connected through an inductance and another with a high resistance to create a phase difference of 90° .

The input to both coils is the current to be measured.

on the center of the yoke ~~and~~ in coil and aluminium drum is placed.

Working :-

When the instrument is connected to the AC a rotating magnetic field is set up due to this eddy currents are induced in the drum, and the torques are produced by the interaction of eddy current and opposite flux.

The deflecting torque is resultant of 2 torques, here also control torque is provided by spring.

Advantages :-

- ① Efficient damping
- ② High torque by weight ratio.
- ③ cheap as compare to MP Instrument.
- ④ Accuracy. scale is high.



Disadvantages

- ① Non uniform scale
- ② Large power consumption
- ② exclusively used for AC measurement,

Measurement of Resistance, Inductance & Capacitance

Measurement of Resistance :-

According to range resistance is divided in 3 parts,

- ① Low resistance ($R < 1$)
- ② Medium resistance ($R (1-100\text{ k}\Omega)$)
- ③ High resistance ($R > 100\text{ k}\Omega$)

① Low resistance :-

The resistance ~~below~~ below one ohm are considered as low resistance. For measuring this we use,

- ① Kelvin's double bridge method
- ② Potentiometer method.

② Medium resistance :-

The resistance betⁿ $1\Omega - 100\text{ k}\Omega$ are considered as medium resistances, all household and commercial appliances resistances are in this range.

These are generally measured by,

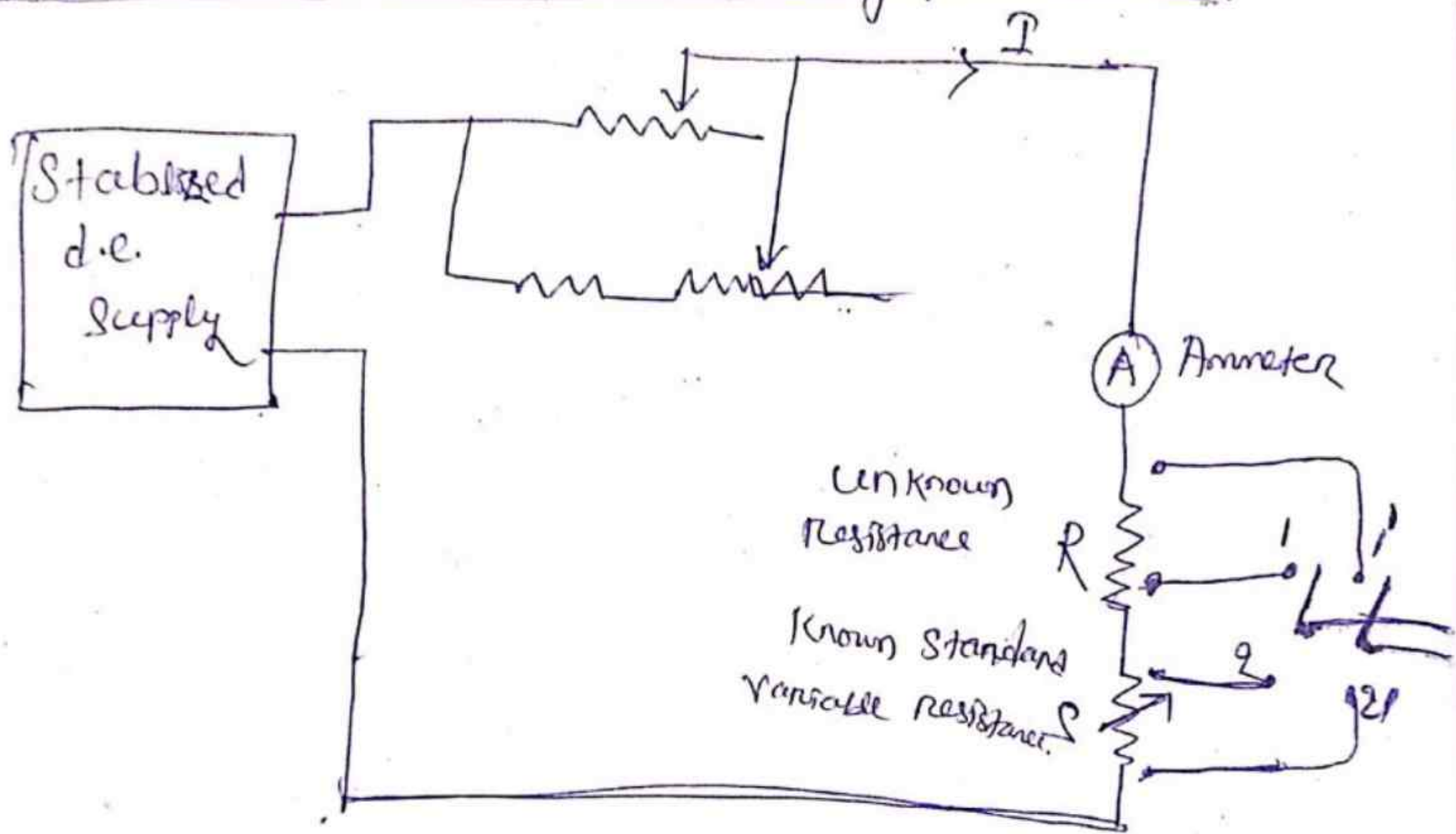
- ① Substitution method
- ② Wheat stone bridge method.

③ High resistance :-

The resistances of value of greater than $100\text{ k}\Omega$ are considered as high resistances.

Usually insulation resistances are in this range.
 For measuring this MS meter (or) megger is use.

Measurement of low resistance by potentiometer



Explanation

This method is used for measuring unknown low resistance. This can be done by comparing the unknown resistance with standard resistance.

here the voltage drop across known and unknown resistance is measured by potentiometer.

here the $R \rightarrow$ unknown value whose value is to be measured.

$S \rightarrow$ standard known resistance.

Rheostat

It is used for controlling the magnitude of current in the ckt.

Ammeter - used for measuring the ckt current.

DPDT switch - This is used for connecting the resistances to potentiometer,

operation - when the switch is in position 1-1' the unknown resistances R_x is connected to the potentiometer,

Let the voltage be ' V_R ' and from dc supply let the current is ' I '.

As R and S are connected in series the same current I is flowing through them, potentiometer,

from this we can write that $V_R = IR$ — (1)

when the switch is in position 2-2', S is connected to the potentiometer,

Let the voltage is V_S ,

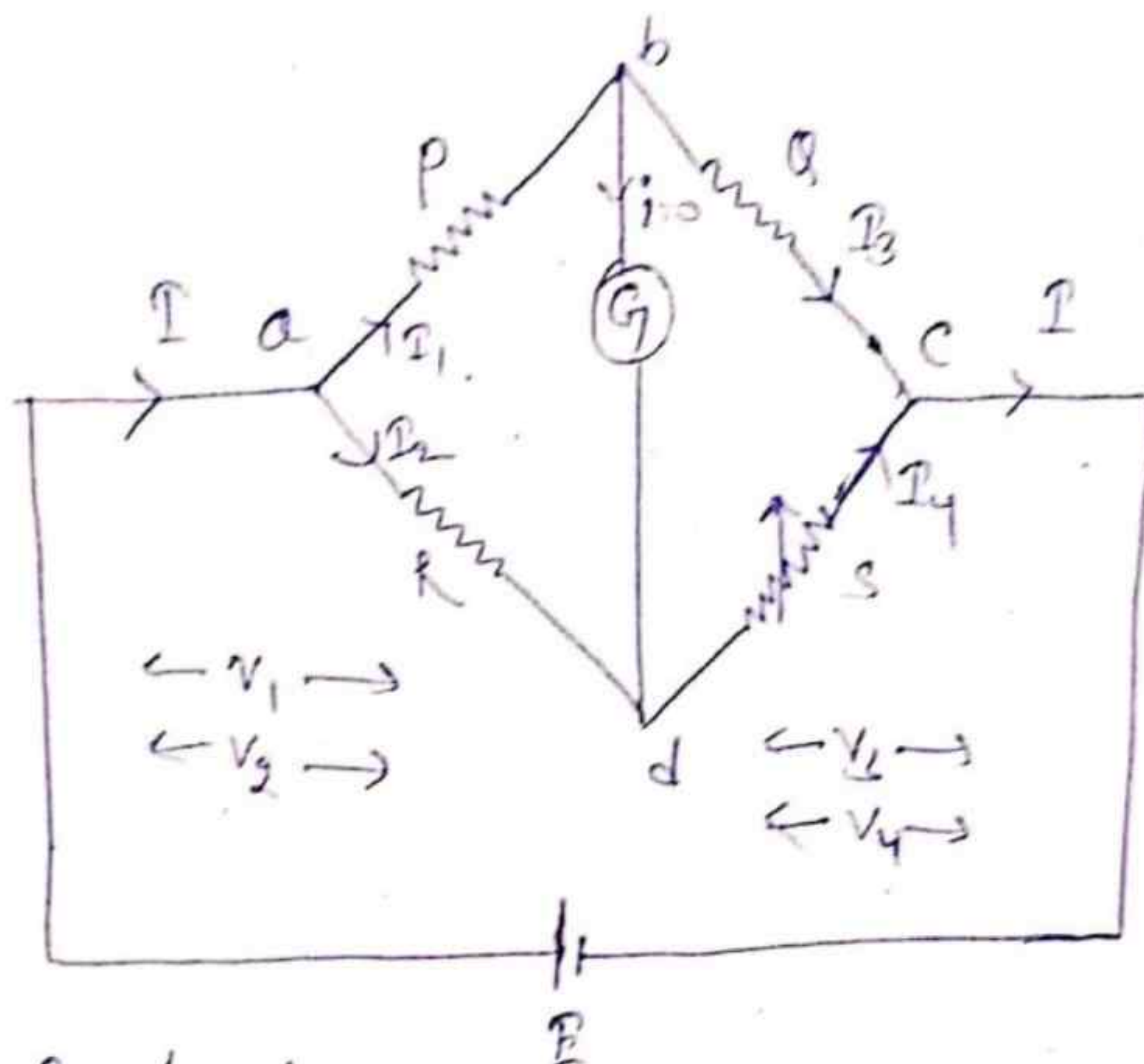
$$V_S = IS \quad (2)$$

By diving eqn (1) by (2) we get,

$$\frac{V_R}{V_S} = \frac{IR}{IS}$$

$$\Rightarrow \frac{V_R}{V_S} \cdot S = R$$

Measurement of medium resistance by Wheatstone bridge method.



Construction:

Wheatstone bridge is used for measurement of medium resistance. This bridge ~~works~~ on the principle of null deflection (or) balance bridge condition. The construction of bridge is as follows.

→ It consists of 4 arms in which the unknown resistances whose value is to be measured. ~~are kept~~ ~~are kept~~ in first arm.

→ here two resistances are known that is (Q & R). ~~kept and are kept~~ in 2nd and 3rd arm and the standard variable known resistance S is kept in 4th branch.

→ And a Galvanometer is connected betⁿ the point d and c as shown in the figure and a battery

or emf is connected betⁿ a and b,

The bridge works on the principle of the null deflection
i.e. when the current through galvanometer is zero.

Balancing condition is the condition to study or ~~analyze~~ analyze
the bridge. ~~at~~ at balanced condition ' i_g ' = 0.

$V_1 \rightarrow$ Voltage across point ad,

$V_2 \rightarrow$ Voltage across point bc

$V_3 \rightarrow$ Voltage across point db.

$V_4 \rightarrow$ Voltage across point cb.

$$\left. \begin{array}{l} I_1 = I_3 \quad P/P+Q \\ I_2 = I_4 \quad E/R+S \end{array} \right\} \text{--- ①}$$

As the potential betⁿ d and b are same in balanced
condition then $V_1 = V_2$ and $V_3 = V_4$ ②

$$\Rightarrow I_1 P = I_3 R$$

From eqn ① and ②

$$\frac{E}{P+Q} \cdot P = \frac{E}{R+S} \cdot R$$

$$\Rightarrow P(R+S) = R(P+Q)$$

$$\Rightarrow PR + PS = RP + RQ$$

$$\Rightarrow PS = RQ$$

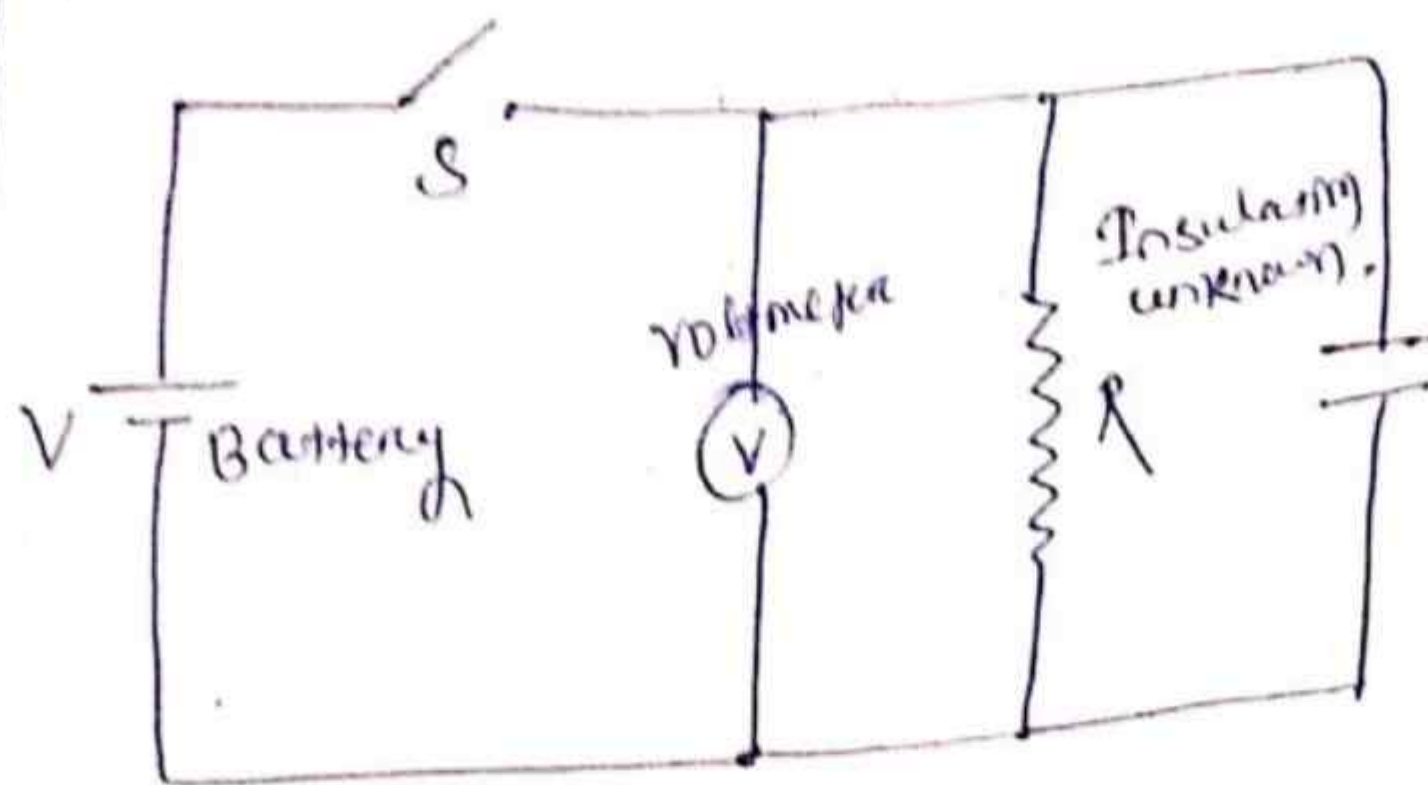
$$\Rightarrow \boxed{R = \frac{PS}{Q}}$$

This is the expression for

Unknown resistance in terms of known resistances.

Here the balancing condition is obtained by varying
the S = standard variable known resistance.

Measurement of high resistance by using loss of charge method.



$$V_0 = V_0 e^{-t/\tau}$$

$$V_t = V_0 e^{-t/RC}$$

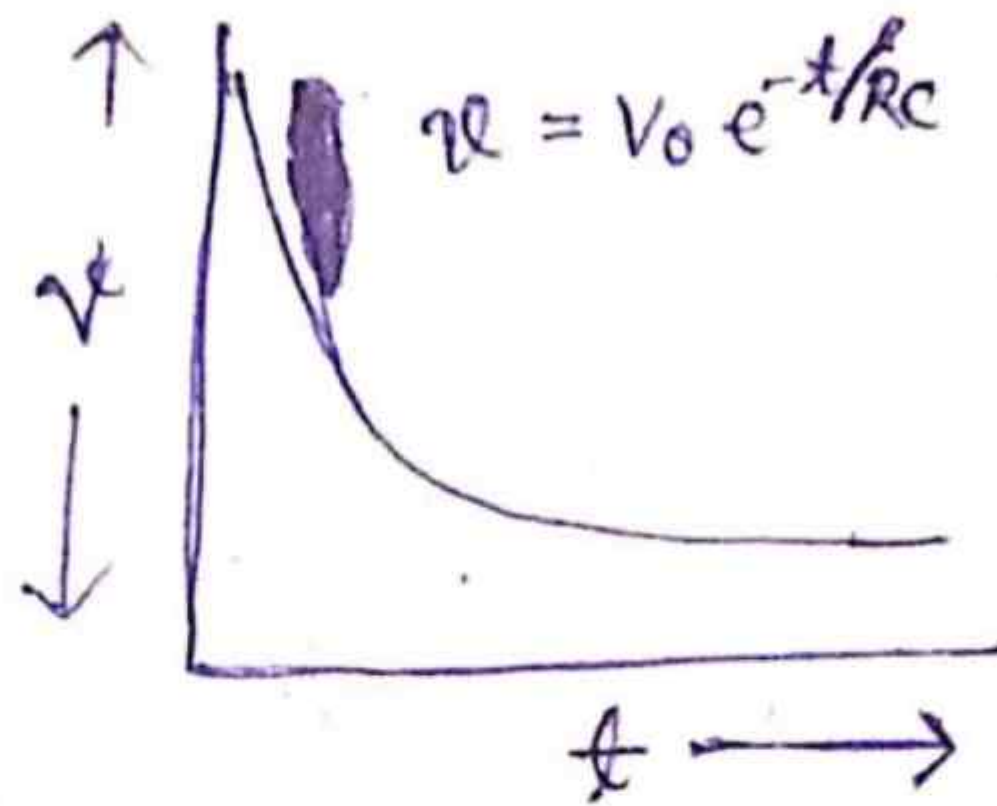
$$\frac{V_t}{V_0} = e^{-t/RC}$$

$$\Rightarrow \log \frac{V_t}{V_0} = \frac{-t}{RC}$$

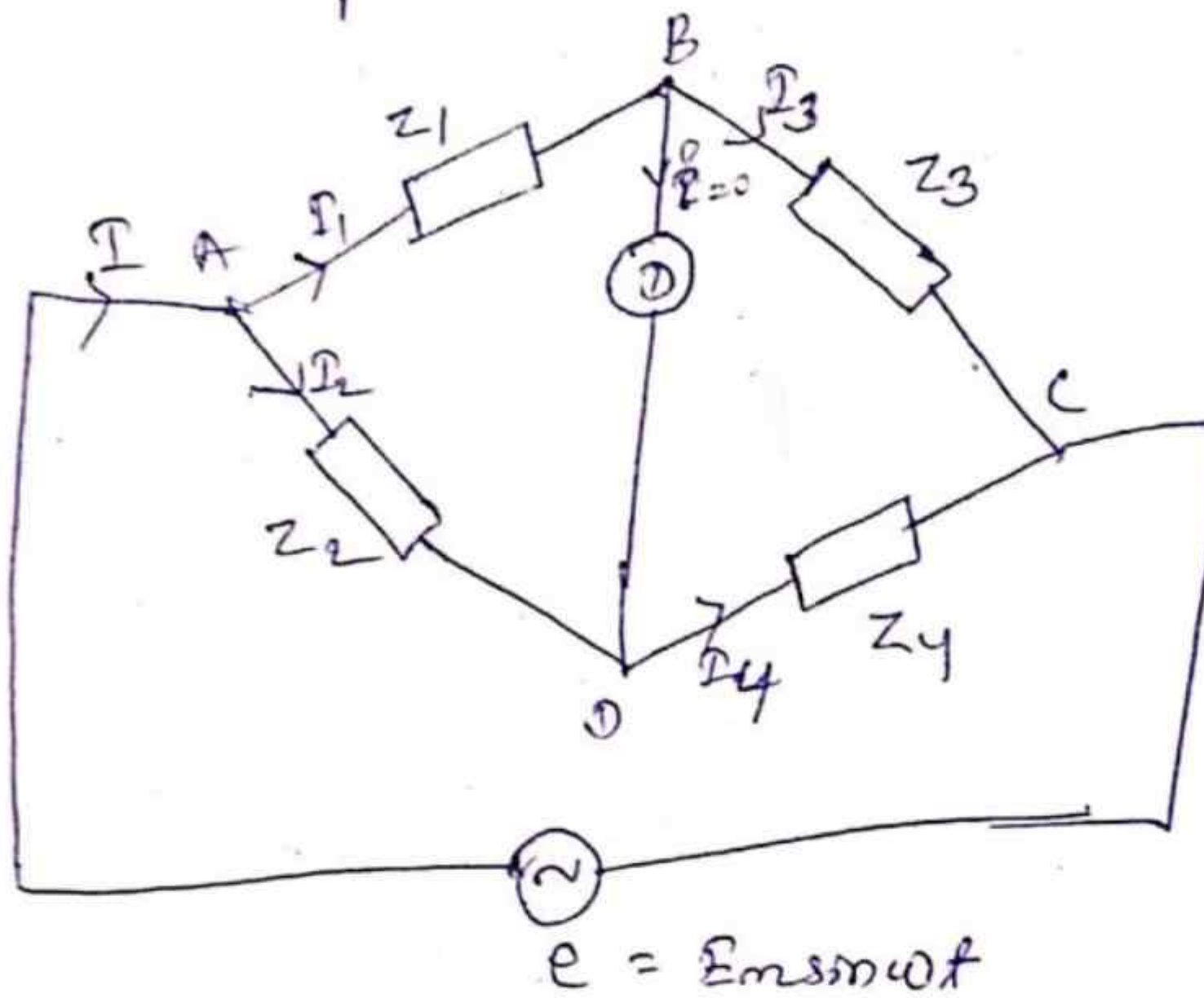
$$R = \frac{t}{\log \left(\frac{V_t}{V_0} \right)} = \frac{0.4343 t}{C \log \frac{V_t}{V_0}}$$

- In this method the insulation resistance (R) to be measured is connected in parallel with a capacitor (C) and an electrostatic voltmeter.
- The capacitor is charged to some suitable voltage by means of battery having voltage (V) and is then allowed to discharge through the resistance. The terminal voltage is observed over considerable period of time during discharge.
- The voltage across the capacitor at any instant (t) after the application of voltage is -

~~Q. If V_i , V_0 , C & t are known. then the value ' R ' can be computed.~~



Balancing Condition for AC Bridge:-



At Balance condition $I_D = 0$

$$\text{i.e. } I_1 = I_3, \quad I_2 = I_4$$

$$E_1 = E_2$$

$$E_3 = E_4$$

$$\Rightarrow I_1 Z_1 = I_2 Z_2 \quad \text{--- (i)}$$

$$\Rightarrow I_3 Z_3 = I_4 Z_4 \quad \text{--- (ii)}$$

from eqⁿ (i) and (ii)

$$\Rightarrow \frac{I_1}{I_2} = \frac{Z_2}{Z_1} \quad \Rightarrow \frac{I_1}{I_2} = \frac{Z_4}{Z_3}$$

$$\Rightarrow \frac{Z_2}{Z_1} = \frac{Z_4}{Z_3}$$

$$\Rightarrow Z_2 Z_3 = Z_1 Z_4$$

$$\Rightarrow Z_1 Z_4 = Z_2 Z_3$$

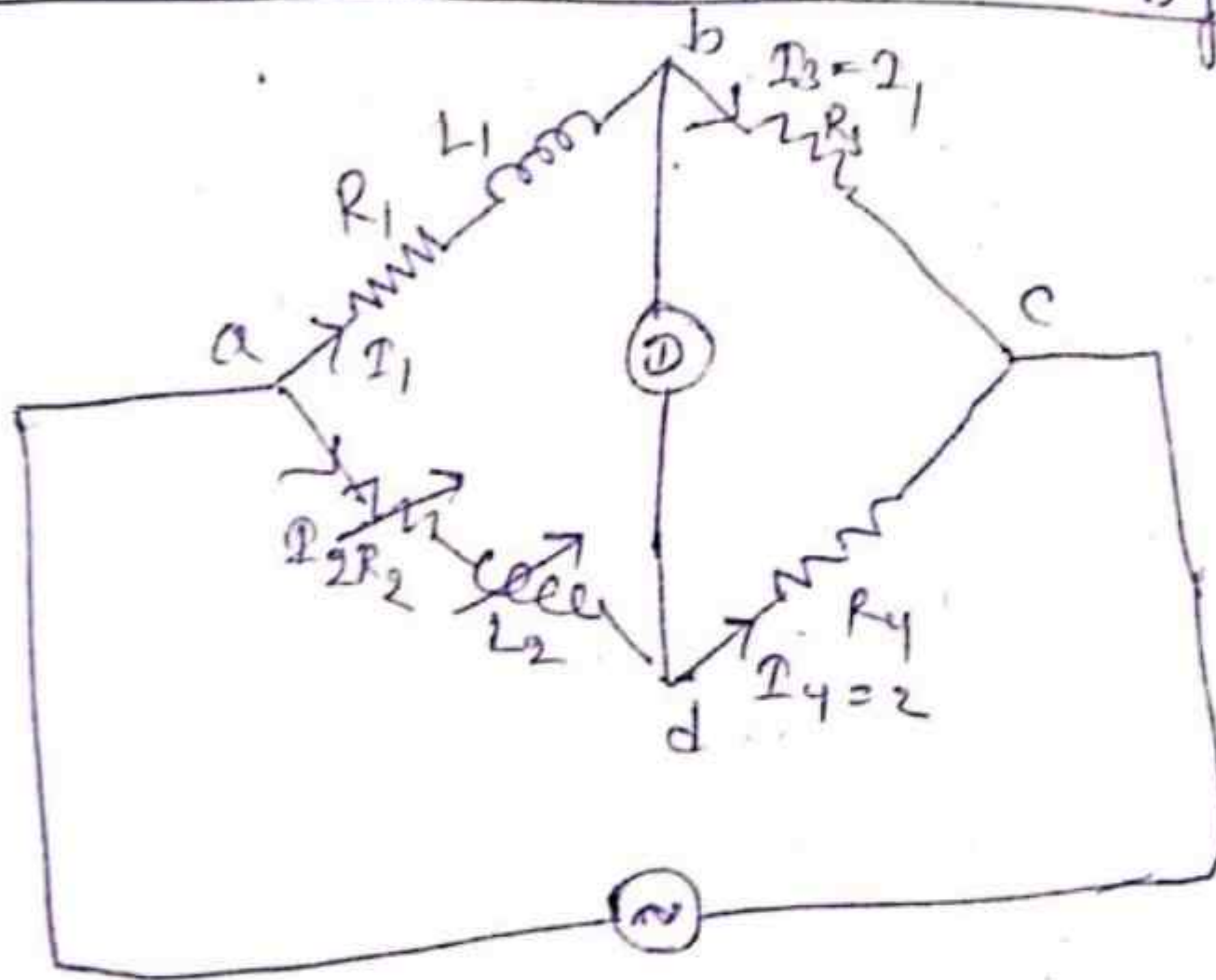
$$\Rightarrow |Z_1| < 0, |Z_4| < 0_4 = |Z_2| < 0_2 \neq |Z_3| < 0_3$$

$$\Rightarrow |Z_1| |Z_4| \angle \theta_1 + \theta_4 = |Z_2| |Z_3| \angle \theta_2 + \theta_3$$

$$\Rightarrow |Z_1| |Z_4| = |Z_2| |Z_3|$$

$$\angle \theta_1 + \angle \theta_4 = \angle \theta_2 + \angle \theta_3$$

① Measurement of Inductance by Maxwell bridge



It is the first formulated bridge for measurement of inductance, in this bridge the unknown value of inductance L_1 is calibrated in terms of known value of inductance L_2 .

The bridge is as shown in the figure.

where $L_1 \rightarrow$ unknown inductance of resistance R_1

$L_2 \rightarrow$ variable inductance.

$R_2 \rightarrow$ variable resistance connected in series with L_2 .

$R_3, R_4 \rightarrow$ known non-inductive resistance.

The bridge is balanced by adjusting the value of $L_2 R_2$.

at balance condition, current through the detector $(i) = 0$.

$$Z_1 Z_4 = Z_2 Z_3$$

$$\Rightarrow |Z_1| |Z_4| \angle \theta_1 + \theta_4 = |Z_2| |Z_3| \angle \theta_2 + \theta_3$$

$$\Rightarrow (R_1 + j\omega L_1) R_4 = (R_2 + j\omega L_2) R_3$$

$$\Rightarrow R_1 R_4 + j\omega L_1 R_4 = R_2 R_3 + j\omega L_2 R_3$$

By Equating real part we get,

$$\therefore R_1 R_4 = R_2 R_3$$

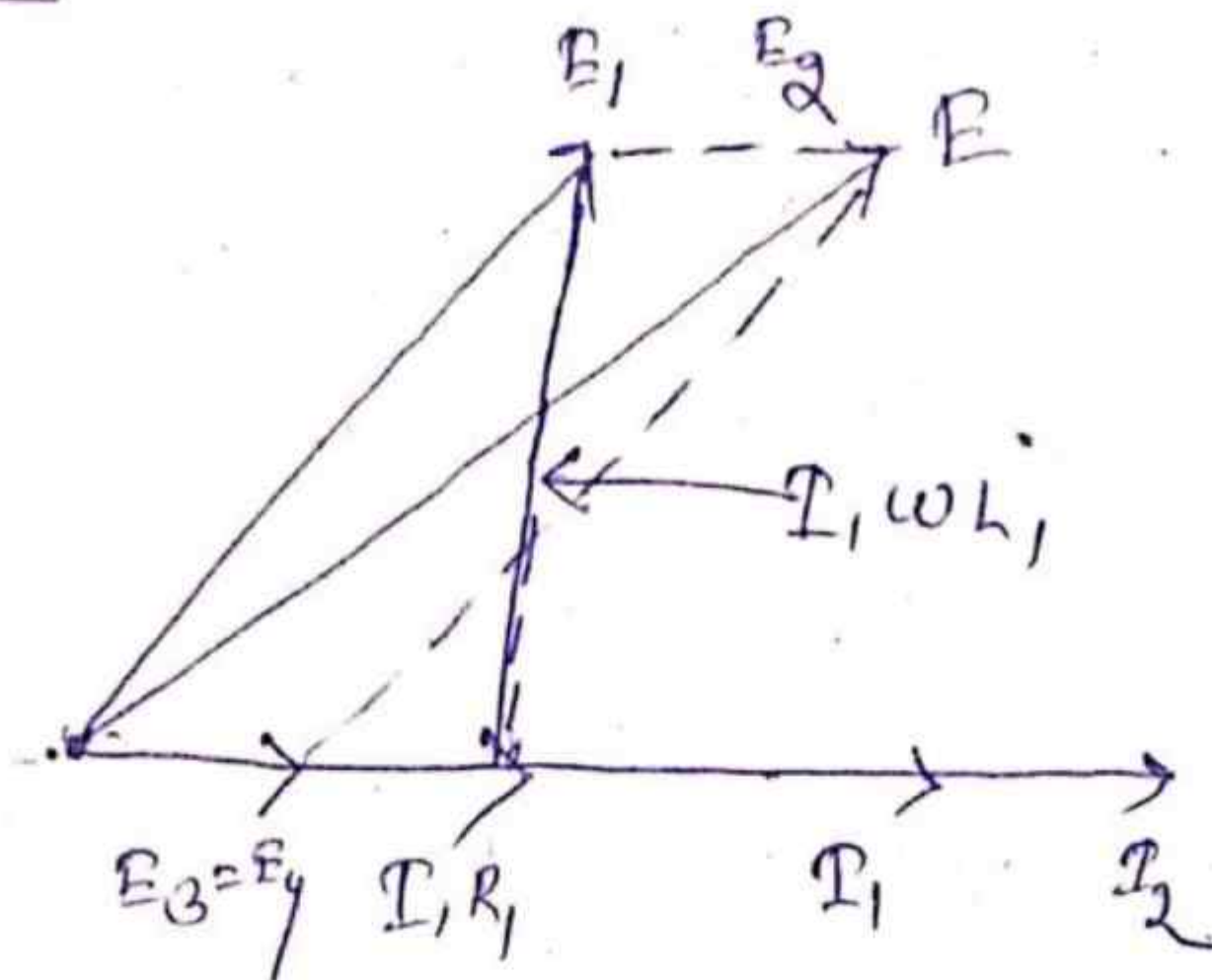
$$\therefore \boxed{R_1 = \frac{R_2 R_3}{R_4}}$$

By equating Imaginary part, we get,

$$j\omega L_1 R_4 = j\omega L_2 R_3$$

$$\Rightarrow L_1 R_4 = L_2 R_3 \Rightarrow \boxed{L_1 = \frac{L_2 R_3}{R_4}}$$

Phasor diagram :-



Advantages :-

- ① Expression for R_1, L_1 are simple ② They do not depend on frequency.
- ③ R_1, L_1 are independent of each other.

Disadvantages :-

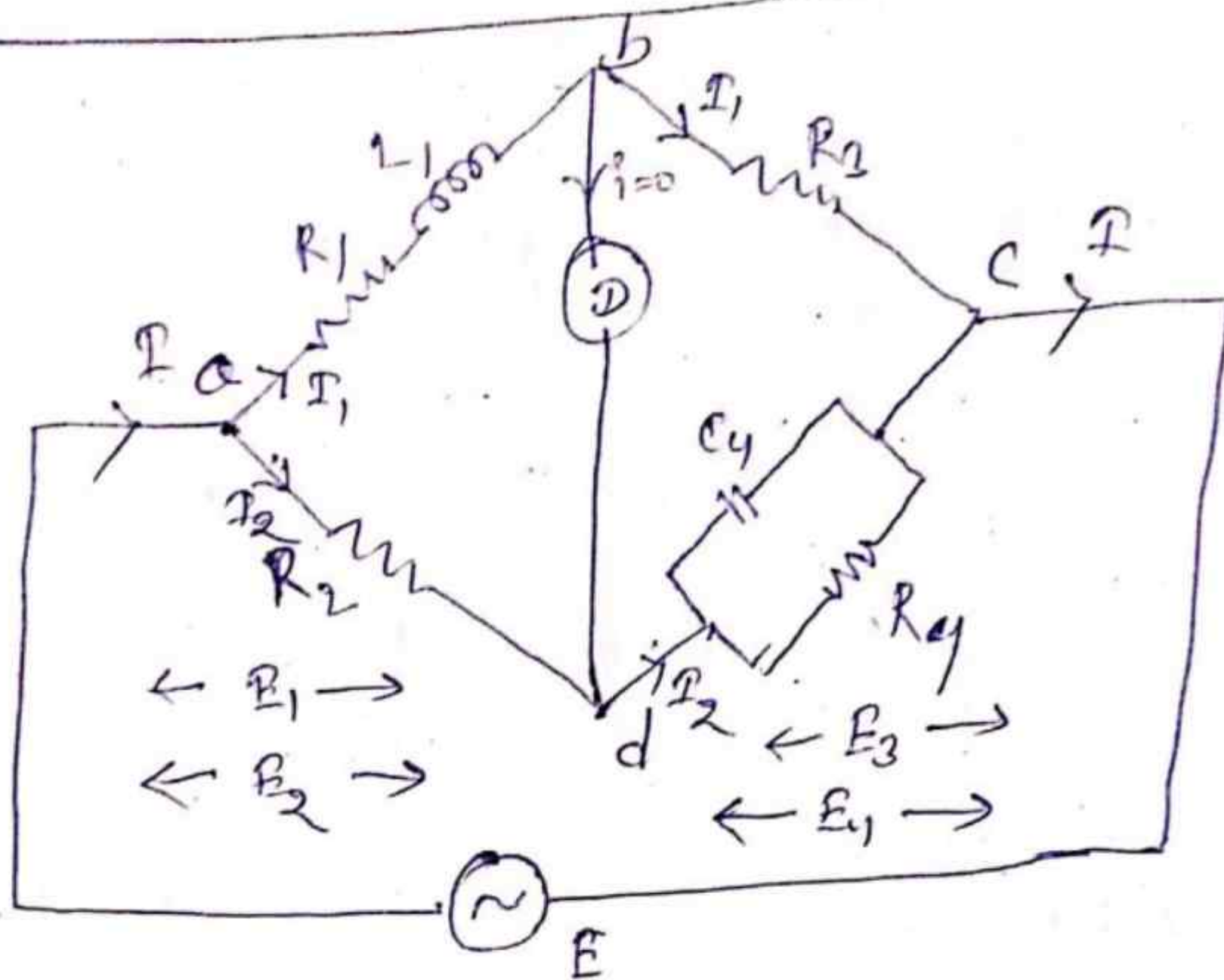
- ① Variable inductance used is costly bulky.

Date - 13/02/2020

Maxwell's L-C bridge

In this bridge the unknown inductance is measured in terms of known variable capacitance.

→ The variable capacitance is used to adjust ~~the~~ and get the condition of null deflection.



$L_1 \rightarrow$ unknown inductance

$R_1 \rightarrow$ effective resistance of L_1

$R_2, R_3, R_4 \rightarrow$ known non-inductive resistance

$C_4 \rightarrow$ variable standard capacitor.

The bridge is analysed when it is in the balance condition i.e. at balance condition,

$$Z_1 Z_4 = Z_2 Z_3$$

$$Z_1 = R_1 + j\omega L_1$$

$$Z_3 = R_3$$

$$Z_2 = R_2$$

$$Z_4 = \frac{R_4 \cdot \frac{1}{j\omega C_4}}{R_4 + \frac{1}{j\omega C_4}}$$

$$\Rightarrow \frac{\frac{R_4}{j\omega C_4}}{R_4 + \frac{1}{j\omega C_4}} = Z_4 \Rightarrow Z_4 = \frac{R_4}{1 + R_4 j\omega C_4}$$

$$Z_1 Z_4 = Z_2 Z_3$$

$$= (R_1 + j\omega L_1) \frac{R_4}{1 + R_4 j\omega C_4} = R_2 R_3$$

$$\Rightarrow R_1 R_4 + j\omega L_1 R_4 = R_2 R_3 (1 + R_4 j\omega C_4)$$

$$\Rightarrow R_1 R_4 + j\omega L_1 R_4 = R_2 R_3 + R_2 R_3 R_4 j\omega C_4$$

By equating Real part -

$$R_1 R_4 = R_2 R_3 \Rightarrow R_1 = \frac{R_2 R_3}{R_4}$$

By equating Imaginary part -

$$j\omega L_1 R_4 = R_2 R_3 R_4 j\omega C_4$$

$$\Rightarrow L_1 R_4 = R_2 R_3 C_4$$

$$\text{The quality factor (Q)} = \frac{\omega L_1}{R_1} = \frac{\omega R_2 R_3 R_4}{\frac{R_2 R_3}{R_4}}$$

$$\Rightarrow \frac{\omega L_1}{R_1} = \omega R_4 C_4$$

uses:-

This bridge is used for measurement of inductance over wide range at high power factor and best used for measurement of low quality factor, i.e. $Q < 10$.

Advantages:-
The value of L_1 and R_1 are independent of frequency.

frequency.

→ The value of L_1 and R_1 are independent if we choose R_2 and C_2 variable.

~~31-13~~

* Scheering Bridge :-

It is the most general form of bridge for measurement capacitance over wide range.

→ this uses a variable capacitor for balancing.

→ A static capacitor is also connected in 1st arm;



$C_1 \rightarrow$ unknown capacitor whose capacitance is to be measured

$R_1 \rightarrow$ series resistance connected with capacitor ' C_1 '.

$C_2 \rightarrow$ A standard capacitor.

$R_3 \rightarrow$ non inductive resistance.

$C_4 \rightarrow$ variable capacitor

$R_4 \rightarrow$ variable non inductive resistance connected

in parallel with C_4 .

At balance condition,

$$Z_1 Z_4 = Z_2 Z_3$$

$$Z_1 = R_1 + \frac{1}{j\omega C_1} \quad \therefore \quad Z_2 = \frac{1}{j\omega C_2} \quad Z_3 = R_3$$

$$Z_4 = \frac{R_4}{1 + R_4 j\omega C_4}$$

$$\therefore Z_1 Z_4 = Z_2 Z_3$$

$$\Rightarrow R_1 + \frac{1}{j\omega C_1} \times \frac{R_4}{1 + R_4 j\omega C_4} = \frac{1}{j\omega C_2} \times R_3$$

$$\Rightarrow \frac{j\omega C_1 R_1 + 1}{j\omega C_1} \times \frac{R_4}{1 + R_4 j\omega C_4} = \frac{R_3}{j\omega C_2}$$

$$\Rightarrow \frac{R_4 j\omega C_1 R_1 + R_4}{\cancel{j\omega C_1} + C_1 R_4 j\omega C_4} = \frac{R_3}{C_2}$$

$$\Rightarrow R_4 j\omega C_1 R_1 + R_4 = \frac{R_3 C_1 + R_3 C_1 R_4 j\omega C_4}{C_2}$$

$$\Rightarrow R_4 j\omega C_1 R_1 + R_4 = \frac{R_3 C_1}{C_2} + \frac{R_3 C_1 R_4 j\omega C_4}{C_2}$$

By equating ^{Imaginary} ~~Real~~ part

$$\Rightarrow R_1 \omega C_1 = \frac{R_3 \omega C_2}{R_4 \omega C_2}$$

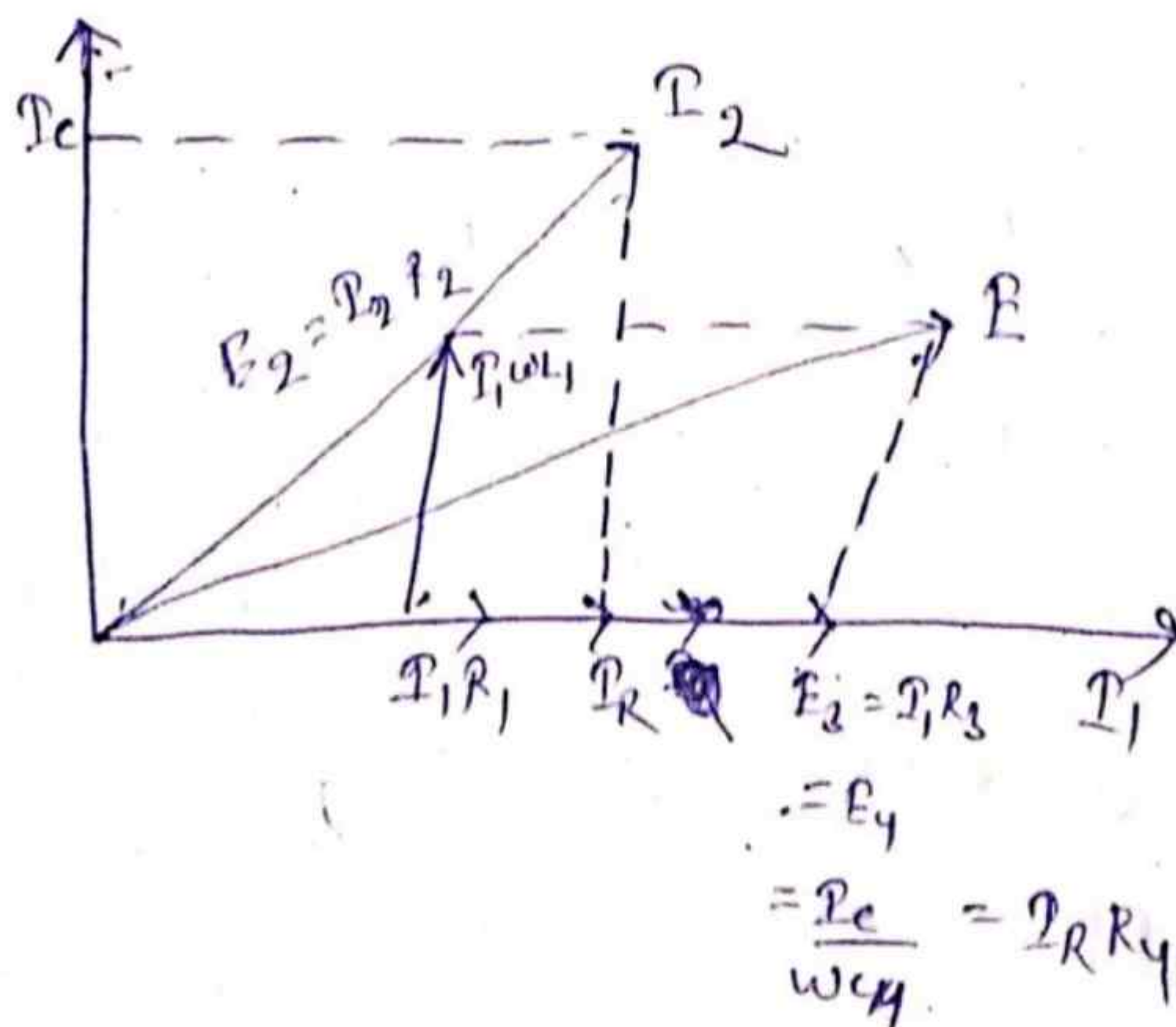
$$\Rightarrow R_1 = \frac{R_3 C_2}{C_1}$$

By equating ^{real part,} ~~Imaginary part~~

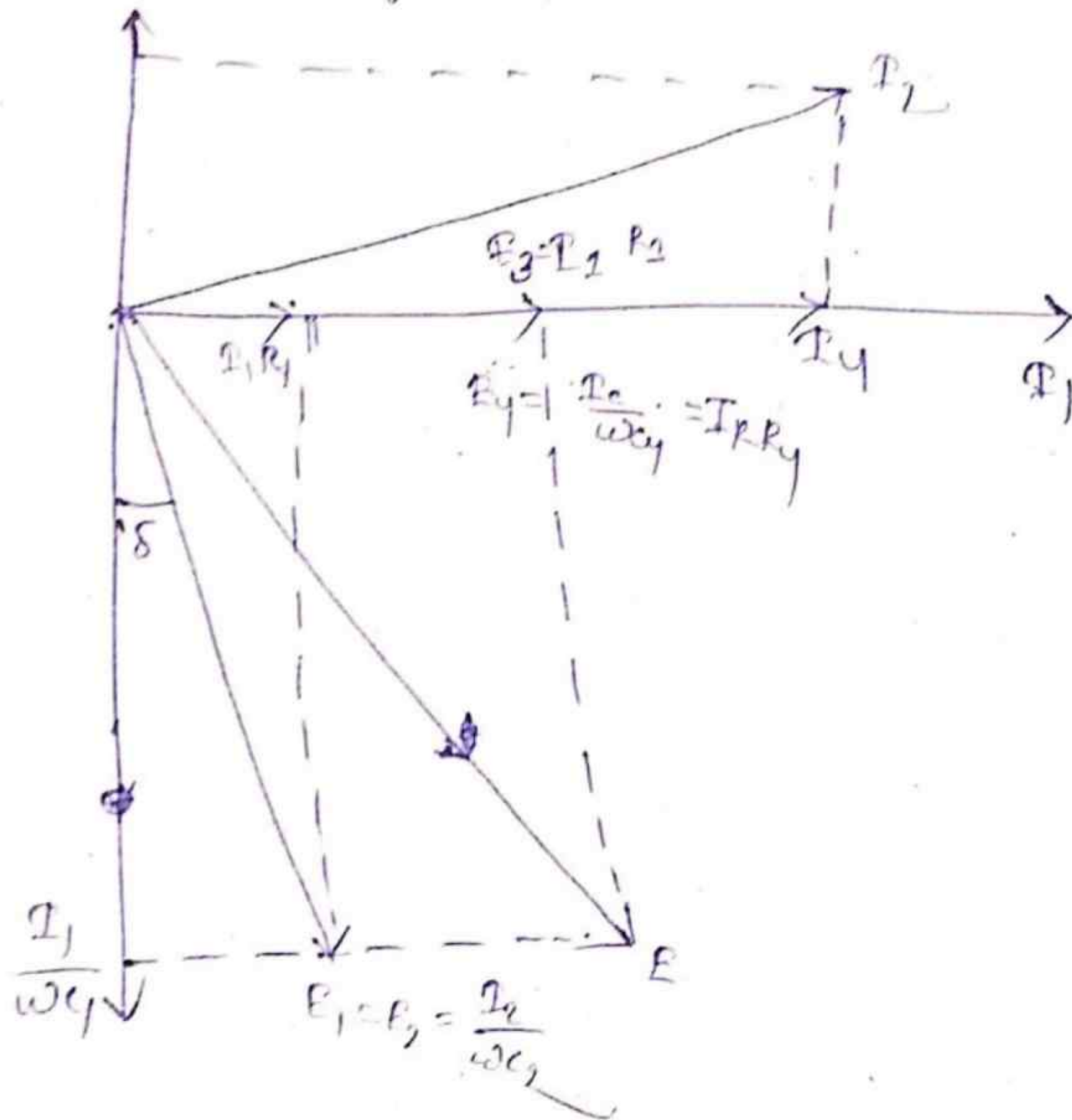
$$R_4 = \frac{R_3 C_1}{C_2}$$

$$\Rightarrow C_1 = \frac{R_4 C_2}{R_3}$$

Phasor diagram of Maxwell's L-C bridge



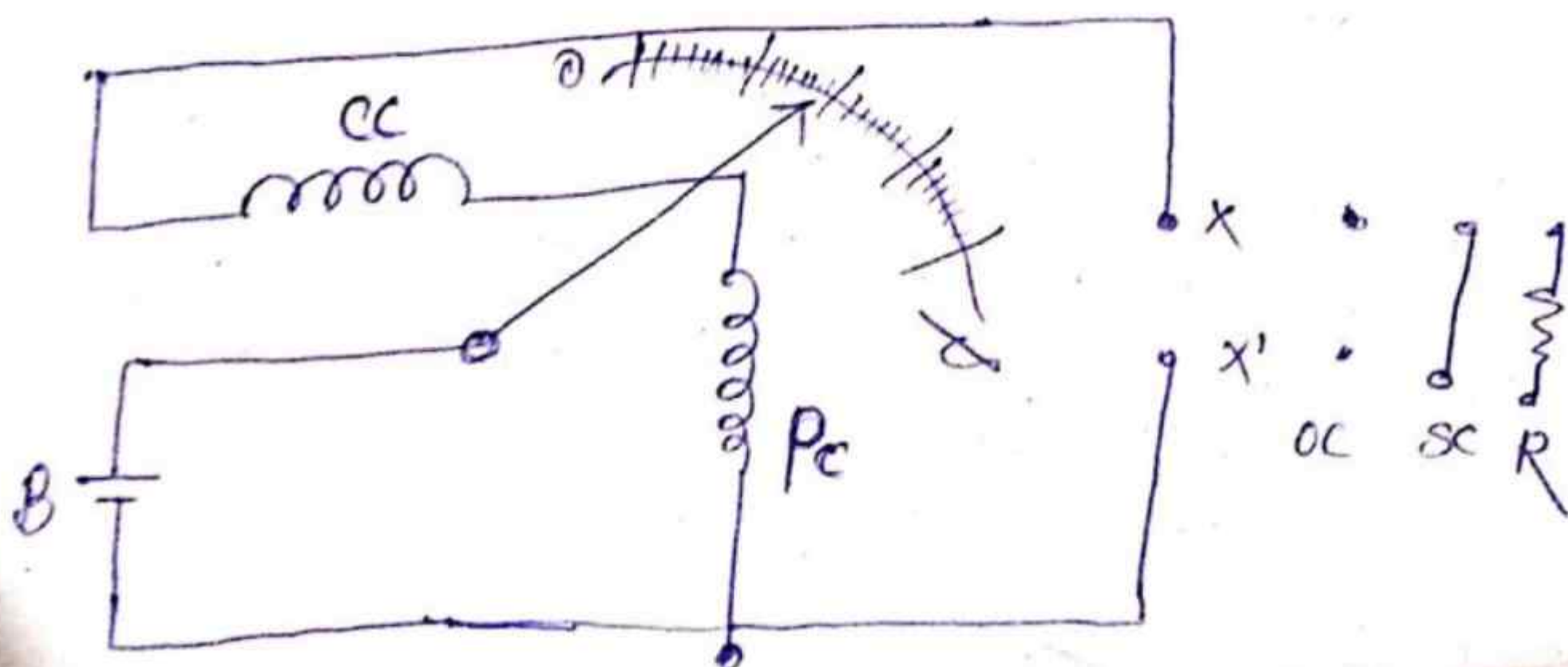
phase diagram of shearing bridge



Date-15/02/2020

Ohm-meter

gm-meter
gm is used for the measurement of medium resistance even though the instrument scale is calibrated for infinite. Its accuracy can be maintained up to 100%.



Operation

The operation of this instrument, can be explain in three steps.

The value of resistance whose value is to be measured is connected across the terminal

$X-X'$,

is connected

- ① when no resistance ^{is connected} in betⁿ $X-X'$ it is considered as open circuit.

on this case pointer gives maximum deflection i.e. ∞ .

- ② when $X-X'$ is short circuited, on this case the meter indication should be zero because in short circuit $R=0$.

on this case the current flowing through current coil is maximum, so it will exhaust maximum magnetic pole.

- ③ Any intermediate value of resistance is connected betⁿ $X-X'$. on this case both the coils will share the current proportionally and ~~share~~ exhaust proportional magnetic pole on the pointer. Thereby pointer stands at a particular position on the scale corresponding to value of R .

Megger :-

Megger is portable measurement which is used to measure high resistance i.e. insulation resistance of electrical machinery or system.

It can be battery operated or mechanically operated, and keeps a direct reading in ohms.

Megger comes in the range of 50, 500, 1000, 2500,

5000 volt etc.

① Electronic type (Battery operated)

In this case battery is used to provide d.c. voltage. It is also known as electrical megger. The important parts of this megger are

- ① Digital display ~~connected to~~
- ② Testing wire
- ③ Selection switches
- ④ Indicator

Digital display :-

Used to show the insulation resistance value in digital.

Testing wire :- Two wire leads for connecting megger with an external electrical system for testing.

Selection switches :-

It is used to select different parameter range provided in the megger.

Indicator :- ④ Different indicators are incorporated into the instrument to give a visual and audible

Indication when the instrument is on,
for a warning parameter status

Date - 17/2/20

Advantages

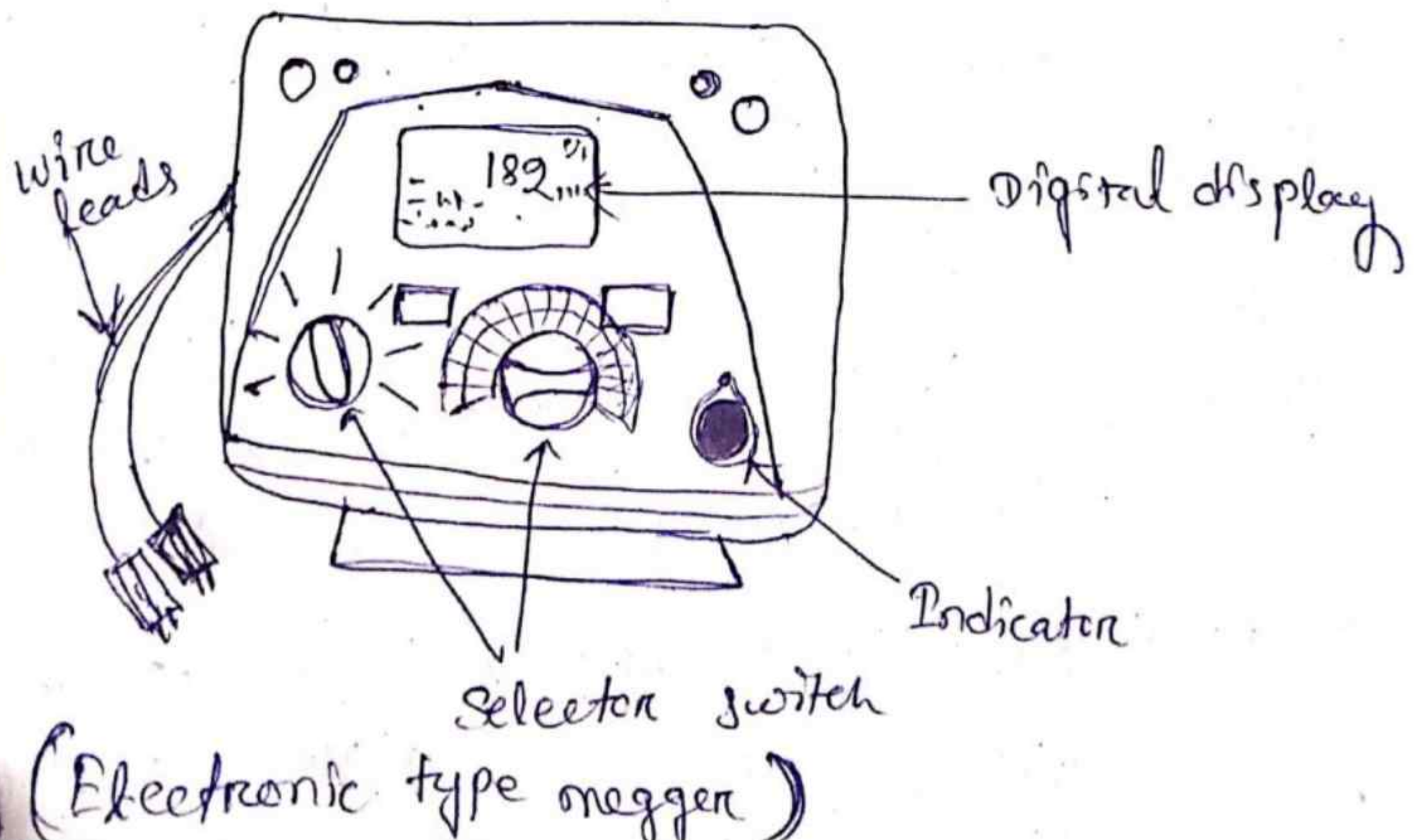
- (i) High accuracy.
- (ii) Easy to operate.
- (iii) Digital display makes it easy to read the insulation resistance value.
- (iv) Robust and safe to use.
- (v) Less maintenance as compare to other type.
- (vi) Handy and compact to carry.
- (vii) Less time consuming operation.

Disadvantages :-

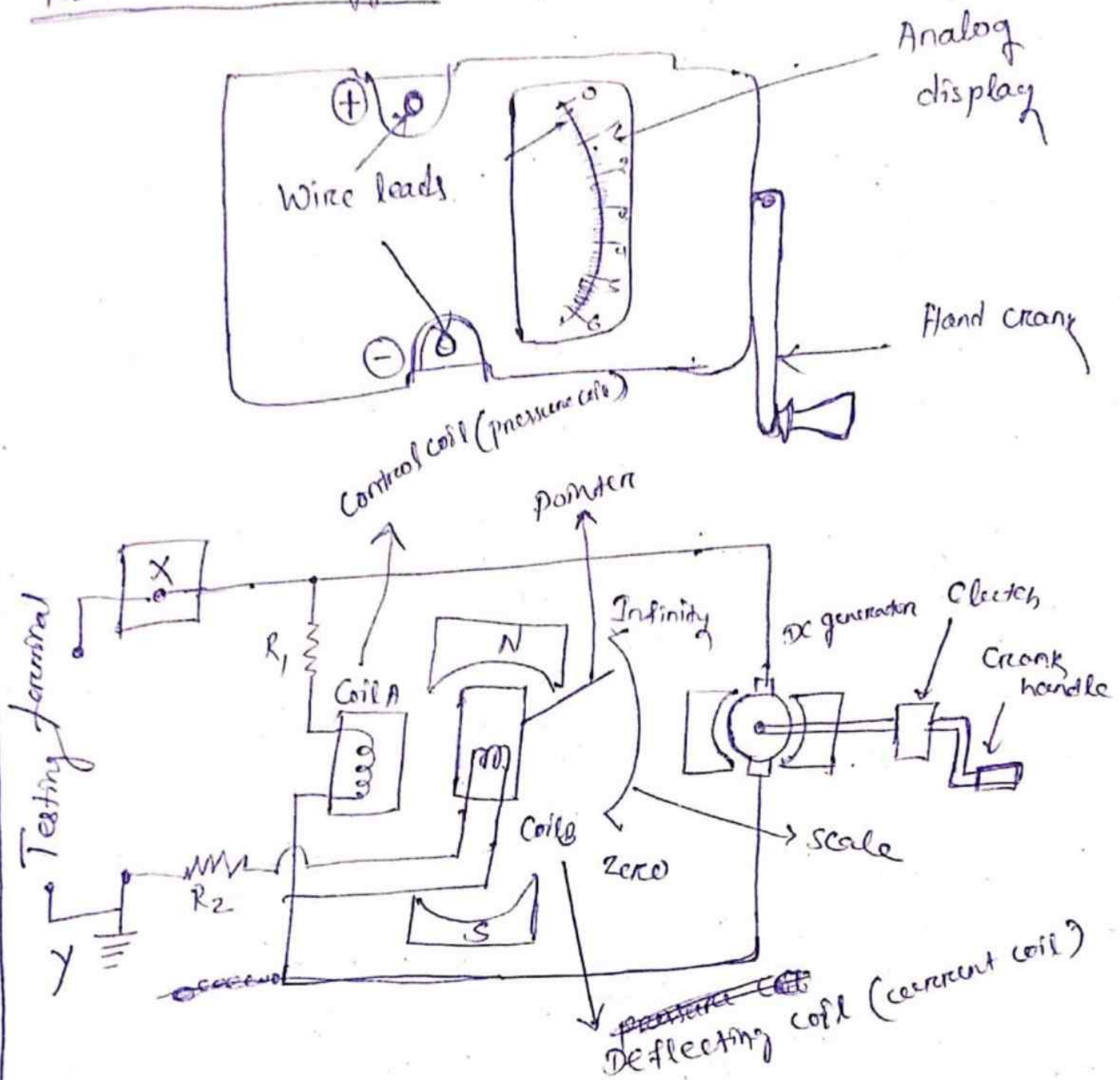
- (i) It requires an external source of energy i.e. dry shape or battery.
- (ii) High initial cost.



Hand held megger :-



Hand held megger :-



Construction :-

- (i) Analog display :- Used for ~~provide~~ displaying insulation resistance value by pointer, ~~etc etc~~
- (ii) Hand crank :- A hand crank is provided which can be rotated to generate the required voltage.
- (iii) Wire leads :- These are provided to connect the megger with electrical system or testing material.
- (iv) Control and deflecting coil :- These are normally mounted at right angle to each other and connected to the d.c. generator.

(V) Permanent magnet & Used to produce magnetic field.
In Ohmmeter and dc generator.

(VI) Pointer & Scale & A pointer is attached to the coil and end of the pointer float on a scale which is in the range from zero to infinity.

(VII) DC Generation & In this megger the testing voltage is supplied by DC motor generator.

(VIII) P.P.C.R & C.C.R & These are the resistance are connected in series with pressure coil and current coil respectively. These are used to limit the current flowing through them.

→ These are also used for preventing the damage.

Working principle & Earth tester Date: 19/2/20

It works on the principle of motor i.e. whenever a current carrying conductor is placed inside a magnetic field then the EMF is induced in the conductor. The reading of the megger is resistance which is directly proportional to the voltage and inversely proportional to the current.

Operation:-

When the electrical circuit is being tested (x, y) is opened the current is only flowing through the control coil hence the torque is only due to control coil. This torque is directly proportional to the voltage.

hence this is maximum, and the pointer shows infinity, that means ~~no~~ shorting through out the ckt and has minimum resistance within the ckt under test.

(ii) If there is short circuit betⁿ X-Y then all the ~~current~~ current will be passing through the deflecting coil.

In this case the torque due to current coil is maximum and torque due to control ~~torque~~ ^{coil} is zero, hence the

reading of the instrument is zero, that means no resistance is in the path.

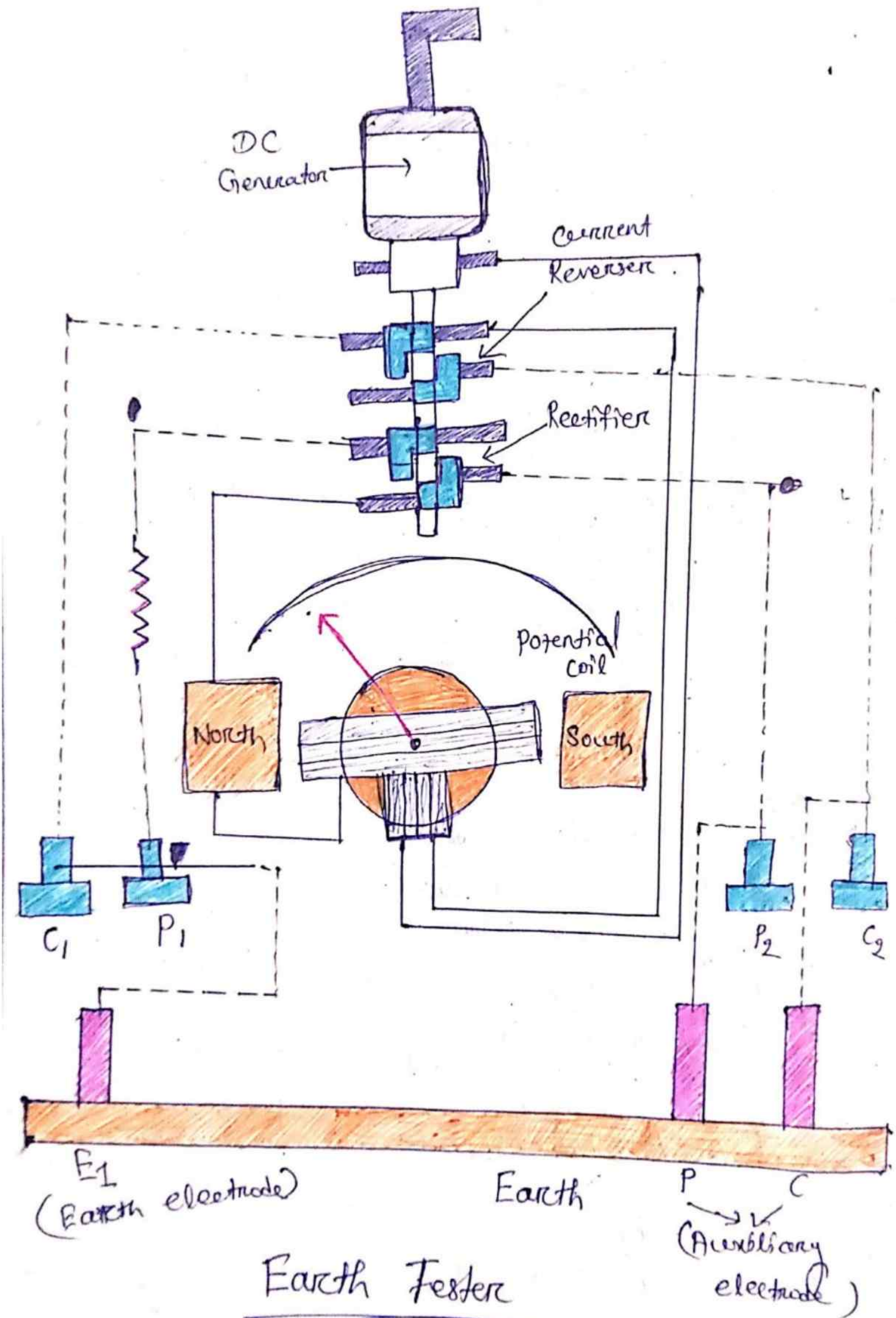
(iii) If there is an intermediate betⁿ X-Y then current flows through both the coil and the torque is due to both coil. The resultant torque of them is acted on the pointer and due to this pointer remains betⁿ zero to infinity.

Date-20/2/20

The instrument used for measurement of earth resistance is known as earth tester. It is a special type of megger which gives AC through earth and DC through measuring in addition to that it has a rectifier and a rotating current reversal, these are mounted on the shaft of DC generator.

It has two pair of pressure coil and current coil
i.e. P_1, C_1 and P_2, C_2 .

P_1, C_1 are shorted to form a ~~common~~ common point which is connected to earth electrode under test i.e. E.



→ The current to the earth is sent by this electrode. The other two terminal C_1 & P_2 are connected to auxiliary electrode C and P . The value of earth resistance is indicated by the instrument directly when it's handled is rotated ~~uniform~~ ^{at} speed, in uniform speed.

→ The earth resistance =
$$\frac{\text{Voltage drop bet}^n E \& P}{\text{Current through earth path,}}$$

→ hence a potential coil is directly connected to DC generator, and the pointer is also attached to the potential coil.

Requirement of earth tester :-

All the equipment of power system is connected to the ~~earth~~ ^{earth} through the earth electrode. The earth protects the equipment and ~~the~~ personnel from the fault current. The fault current through the earth electrode passes to the earth thus protects the ~~the~~ system from damage.

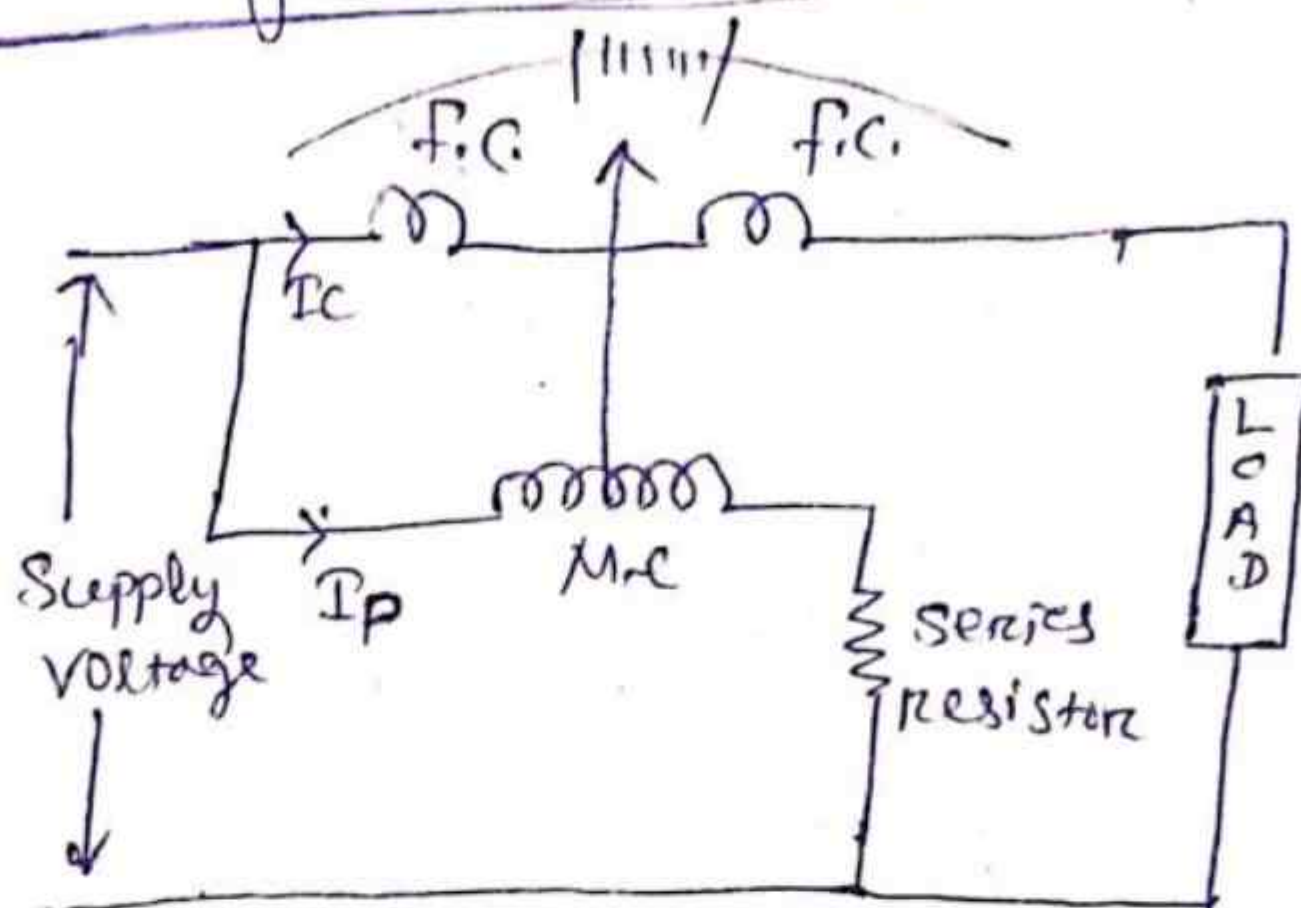
→ The earth tester is use to test OR find the low resistance ground to provide earth electrode.

→ The earth resistance should be less than 1Ω for power station, and should be less than 5Ω for sub station.

Construction - measuring instrument used for measurement of power
Electrodynamometer type ~~is called~~ Wattmeter :-

Principle :-

The instrument whose working depends on the reaction betⁿ the magnetic field of moving coil and fixed coil



is known as electro-dynamometer type wattmeter.

- here the operating field is produced by fixed coil.
- it is used for measurement of power in both AC and DC ckt.

Construction :-

① fixed coil (F.C. or CC)

→ Fixed coil is split into two ^{equal} parts & these are placed 11el to each other.

→ Fixed coil is used to produce operating magnetic field in the instrument.

→ fixed coil is connected in series with the load that's why considered as current coil.

→ It carries the current proportional to the load current.

$$(I_C \propto I_L)$$

→ fixed coil is designed to carry current of approximate ly to carry 20 Amp.

→ Fixed coils are air core to avoid hysteresis loss.

② Moving coil & (MC or) PC

→ The moving coil is considered as pressure coil of the instrument. It connects with the supply voltage.

→ The current flows through it is directly proportional to the supply voltage.

→ The moving coil is placed between two fixed coils and the pointer is mounted on the moving coil.

→ A high value of resistance is connected in series with the moving coil to limit its current.

③ Control system &

Here the control torque is provided by spring control mechanism.

④ Damping system & Here air friction damping is used.

⑤ Scale & pointer & A pointer is attached on the moving coil which graduates over the calibrated scale.

Working principle &

When a current carrying moving coil is placed in the magnetic field produced by current carrying fixed coil then a force is exerted on the coil sides of the moving coil and deflection takes place.

When the power is to be measured in the ckt the wattmeter is connected in the ckt. then current flows through both the coil.

→ The current coil carries the current ' I_c ' proportional to the load current and the pressure coil carries the current ' I_p ' which is proportional to the supply voltage.

→ Then the fixed coil produces field ' F_m ' and moving coil produces field ' F_n '. Now ~~the~~ both the fields interact with each other and the field ' F_n ' tries to come in line with main magnetic field ' F_m ', which produces a deflecting torque in moving coil.

→ Thus the pointer attached to the spindle gets deflected.

The deflecting torque is estimated as,

$$\therefore T_d = I_p I_c \frac{dm}{d\theta} \text{ (for dc)}$$

$$\therefore T_d = I_p I_c \cos \phi \frac{dm}{d\theta} \text{ (for Ac.)}$$

Control torque i.e. Spring control is used the control

torque is given by.

$$T_c = K\theta$$

The pointer will remain stop at equilibrium position that is when $T_c = T_d$.

$$\Rightarrow I_p I_c \frac{dm}{d\theta} = K\theta \quad (\text{for dc})$$

$$\Rightarrow \theta = \frac{1}{K} I_p I_c \frac{dm}{d\theta}$$

$$\Rightarrow I_p I_c \cos\phi \frac{dm}{d\theta} = K\theta \quad (\text{for ac})$$

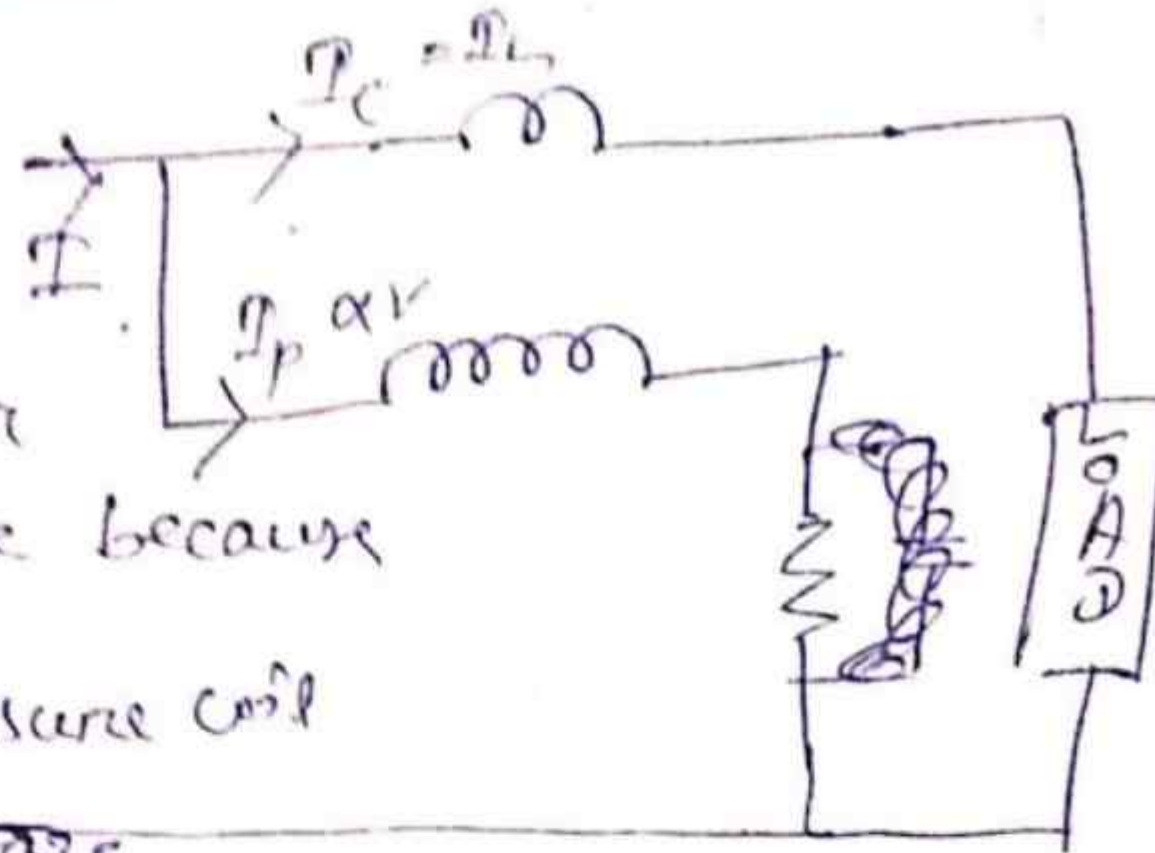
$$\theta = \frac{1}{K} I_p I_c \cos\phi \frac{dm}{d\theta}$$

Errors in dynamometer type wattmeter :-

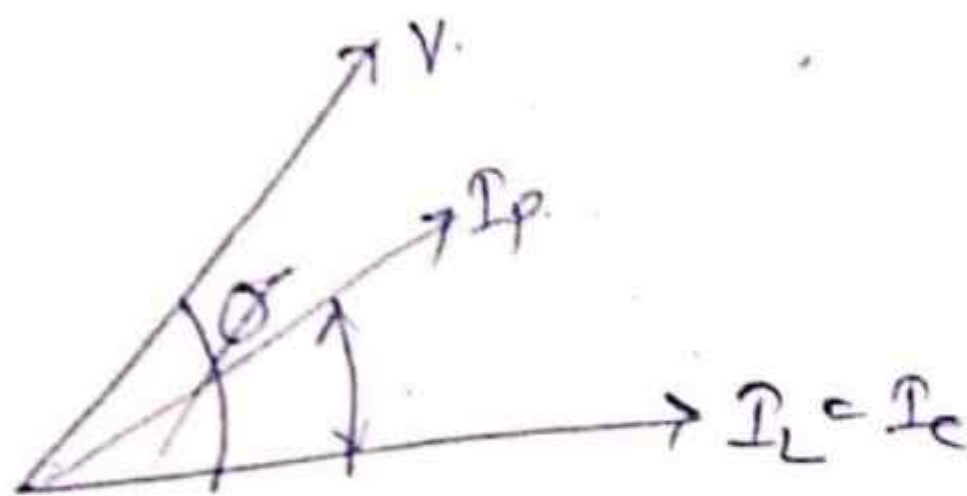
- (i) Error due to PC inductance.
- (ii) Error " PC capacitance
- (iii) " due to connection
- (iv) " " mutual inductance effect.
- (v) Eddy current error
- (vi) Error due to stray magnetic field.
- (vii) Temperature error

① Error due to PC inductance :-

The pressure coil of electro dynamometer type wattmeter has some inductance because of ~~some~~ ^{this} inductance the current of pressure coil lags behind the voltage.

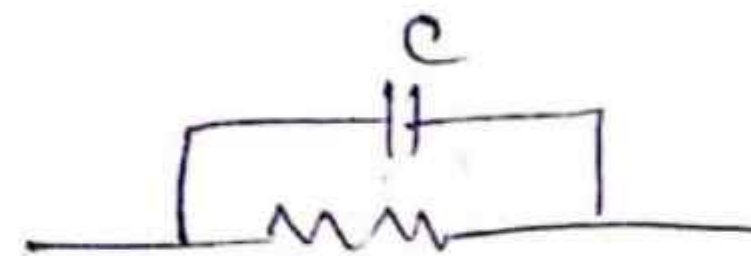


thus the power factor of the wattmeter becomes lagging & the meter reads high value in lagging P.F. & low in leading P.F. this arises error in the instrument



$$T_d = I_p I_c \cos \phi$$

To compensate this a capacitor is connected in parallel with a portion of series resistance.



② Error due to PC capacitance :-

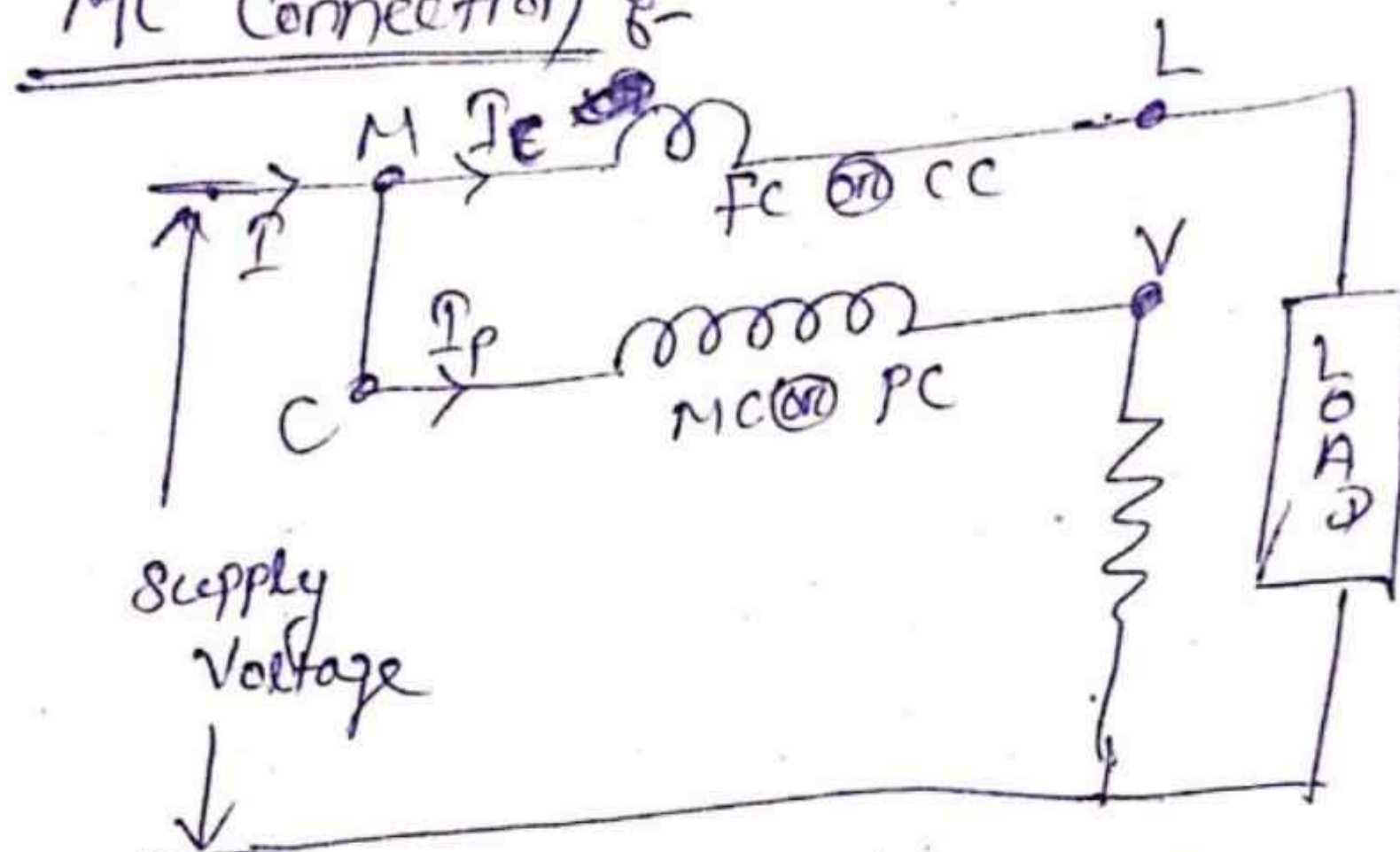
→ The PC has capacitance along with inductance. This capacitance is mainly due to inter term capacitance of series resistance. The capacitance increases the P.F. of instrument hence causes error.

(Or) it has ~~alternate~~ ^{opposite} effect of inductance.

To avoid this error capacitance value is adjusted to suitable value.

III Error due to connection :-
There are two alternating methods of connecting wattmeter

MC Connection :-



M → main C → Common
L → Line V → voltage of selectivity.

here in this connection P_C is connected on supply side
hence 'V' applied to the P_C is voltage across the
load + voltage ^{drop} across the fixed coil.

$$V_{PC} = V_L + V_{FC}$$

$$WMR = I_L \cdot V_L + I_L \cdot V_{FC}$$

The power indicated by the instrument = power
consumed by the load + power loss in F_C .

$$\begin{aligned} WMR &= I_L V_L + I_L \cdot V_{FC} \\ &= I_L \cdot I_L R_{FC} \\ &= I_L^2 R_{FC} \\ &= I_C^2 R_{FC} \end{aligned}$$

From this eqⁿ we can say that wattmeter absorbs
more power than power absorbs by the load.

The excessive power is treated as error, i.e.

$$\text{Error} = I_L \cdot V_{FC} = I_L^2 R_{FC} = I_C^2 R_{FC}$$

here the error is due to moving coil absorbs in excess voltage than load voltage. The excess voltage is required by ~~V_{co}~~ F.C.

④ Error due to mutual inductance &

Error cause due to mutual inductance betⁿ P_c & C_c . This error is quite low at power frequency but increases as frequency increases.

To compensate this P_c and C_c are so arranged that they have zero position of mutual inductance.

⑤ Error due to Eddy current &-

The eddy currents are induced in the metallic parts of the instruments this creates its own magnetic field. This affects the main ~~current~~ magnetic field which causes error in instrument.

To compensate this metallic part may be reduced (or) shielded or standard conductor should be used in ~~CC~~ C_c .

⑥ Error due to Stray magnetic field &-

We already know that dynamometer type wattmeter has weak operating field therefore it is ~~at~~ easily affected by stray magnetic field which affects main magnetic field.

To compensate this instrument should be shielded.

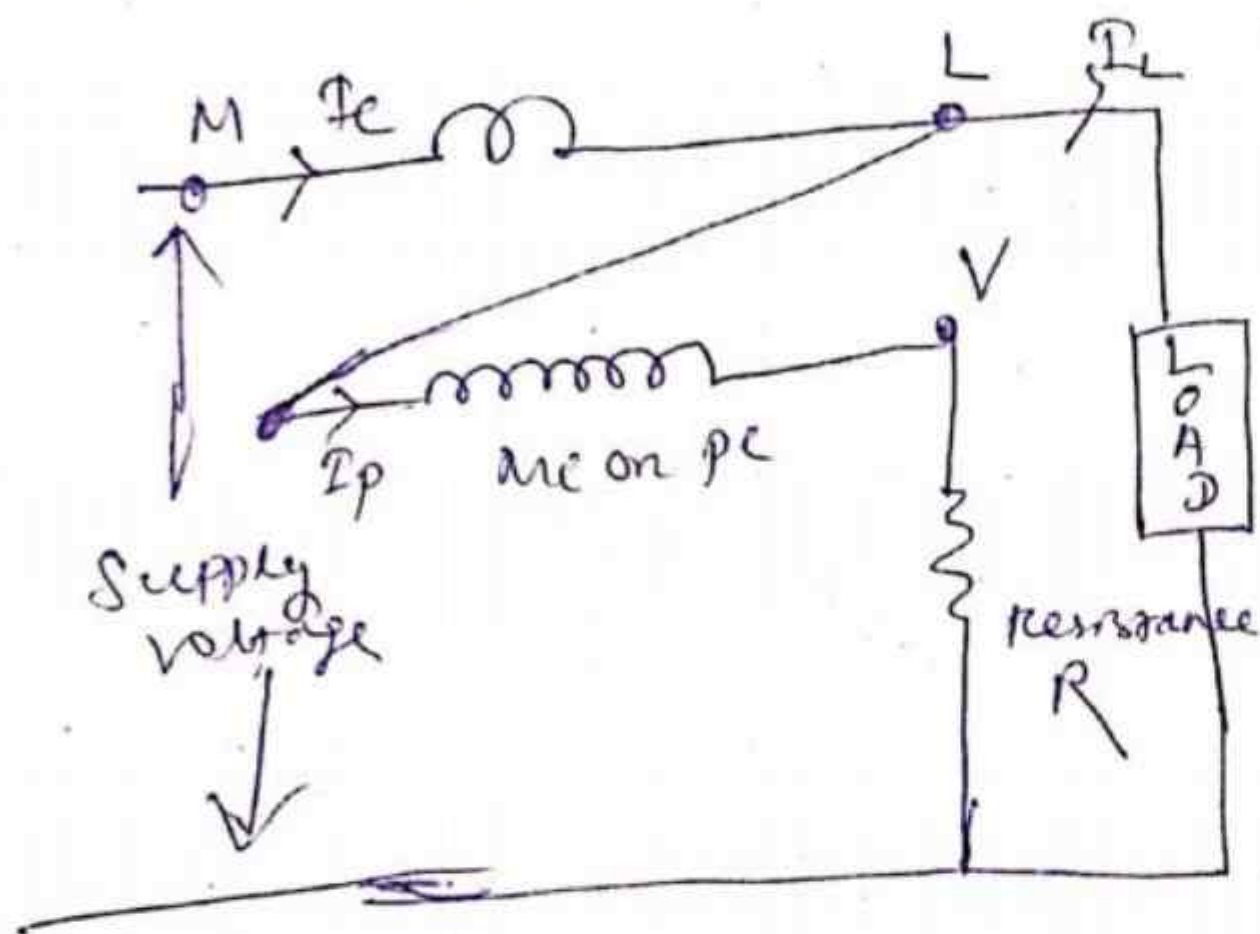
⑦ Temperature error &-

The variation of temp will change the resistance of P_c coil and stiffness of spring.

To compensate this pc should be made up of alloy of Cu and Mn.

Date - 27/02/20

L-C Connection :-



For this connection the current coil is on supply side therefore it carries pc current + Load current, hence the wattmeter reads the power consumed in the load + loss in pressure coil,

$$WMR = I_c \cdot V_{pc}$$

$$= (I_L + I_p) \cdot V_{pc}$$

$$= V_{pc} \cdot I_L + V_{pc} \cdot I_p$$

$$= V_L \cdot I_L + V_{pc} \cdot I_p$$

here, the current coil carries excess current than the current absorbed by the load. this current is for pressure coil. hence the error arises. here the error is $V_{pc} \cdot I_p$.

LPF type wattmeter (Low power factor)

This wattmeter is used for measurement of power with low power factor because an ordinary dynamometer type wattmeter can't measure power with ~~low~~ LPF, due to some reasons.

① The deflecting ~~ing~~ moving system is small, ~~in~~ low power factor ~~even~~ even when ~~both~~ PC and VC are fully excited.

② Error is introduced because of inductance of PC coil be large at LPF.

There are some special features incorporated in ordinary dynamometer type wattmeter to make it LPF wattmeter.

① PC current :- The PC ckt is design to have low value ^{of} resistance so that, current flowing through it increases by which ~~the~~ T_d increases.

② Compensation for PC current :- The power being measured in LPF ckt is small and current is high ~~on~~ on account of LPF.

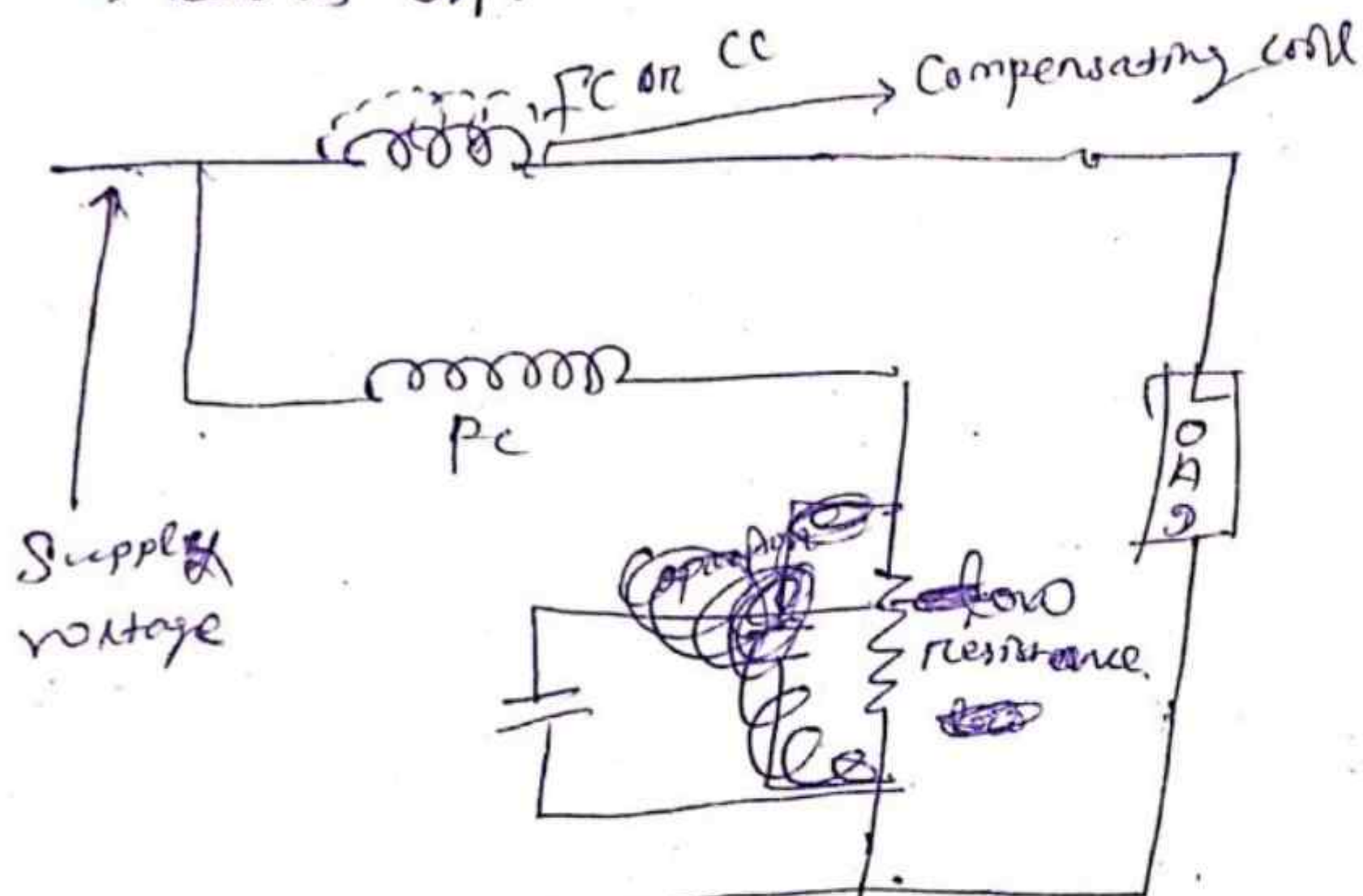
This error arises in ^{both} the connecting so we have to compensate it.

③ Compensation for inductance of PC :-

This error is caused by P_c inductance. This is compensated by connecting a capacitor across a part of series resistance in P_c ckt.

Small Control torque

L_{PF} wattmeter are design small control torque so that they can give full scale deflection for power factor as low as 0.1.



here the compensating coil is connected in series with the P_c . It is made as nearly as possible identical and coincident with series current coil.

It is so connected that, it opposes the field of current coil, hence the resultant field is due to the load current.

Induction type watt meter

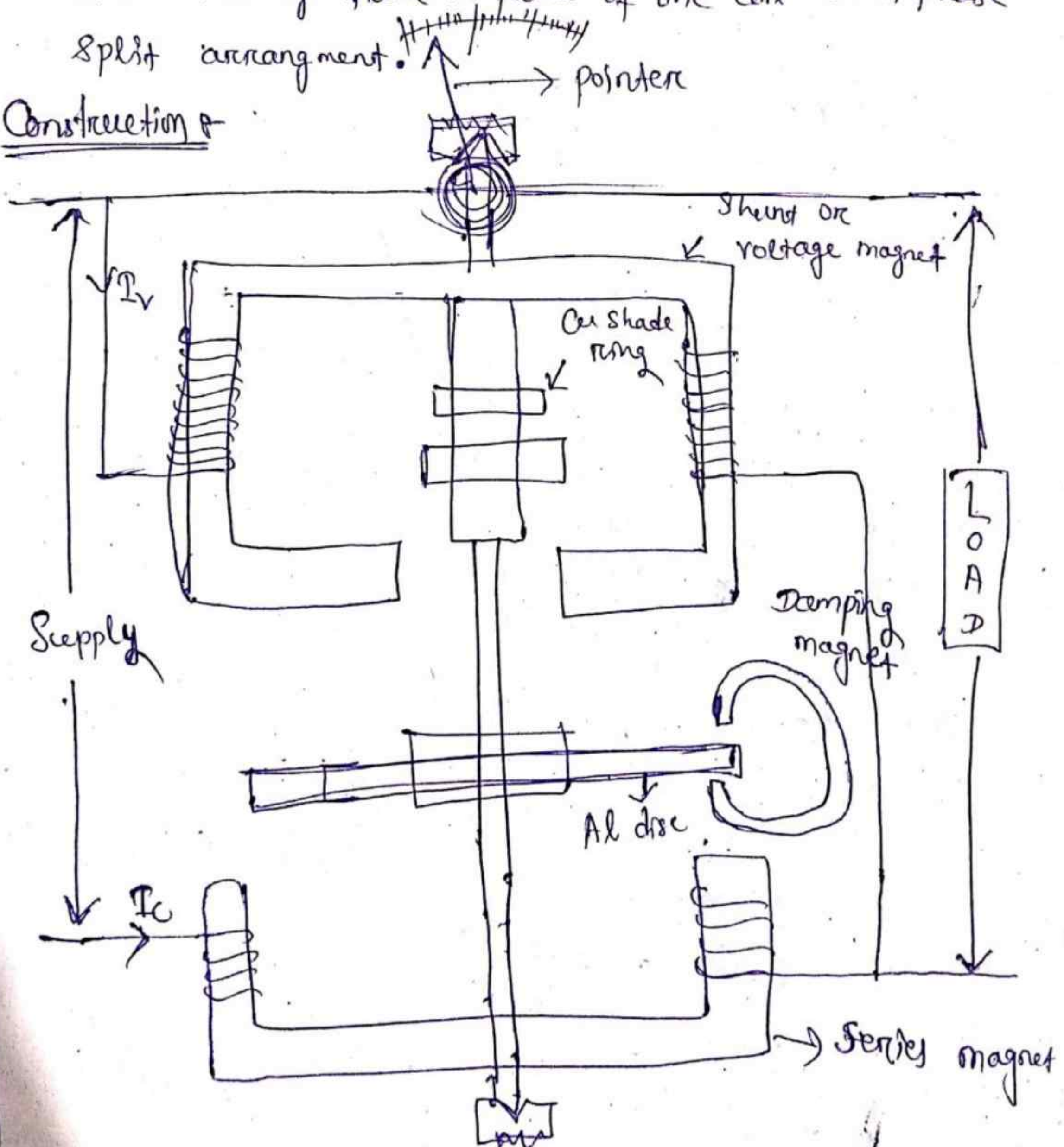
Date - 27/2/20

The induction type watt meter is used to measure ac power only.

Principle :-

The principle of operation of induction wattmeter is same as that of induction ammeter & Voltmeter however, it differs from induction ammeter & voltmeter in so far that separate two coils are used to produce the rotating flux in place of one coil with phase split arrangement.

Construction :-



It consists of two laminated electromagnet. one is called shunt magnet is connected across the supply & carries current ~~proportional~~ proportional to applied voltage this coil of this magnet is made highly inductive so that the current in it lags behind the supply voltage by an angle 90° .

→ The other magnet is called series magnet which is connected in series with supply & carries load current.

The coil of this magnet is made highly non-inductive.

→ A thin Aluminium disc is mounted on the spindle is placed betⁿ two magnet so that it cuts fluxes of both the magnets.

The pointer is attached to the spindle which moves over the calibrated scale.

Control system:-

Spring control mechanism is used here.

Damping system:-

C shaped braking magnet is used here.

Working:-

When the wattmeter is connected to measure AC power, the Shunt magnet carries current proportional to supply voltage i.e. $(I_{sh} \propto V)$ & Series magnet carries the load current $(I_{sh} \propto I)$. Due to this two fluxes ϕ_{sh} & ϕ_{se} are created & two eddy currents are developed these are I_{esh} & I_{esc} . The ~~interaction~~ interaction betⁿ eddy currents & opposite fluxes produce the deflecting torque on the disc.

$V =$ supply voltage

$$T_1 = K I_{se} \phi_{sh} \cos \theta$$

$$T_2 = K I_{esh} \phi_{se} \cos (180^\circ - \theta)$$

$$T_d = T_1 - T_2$$

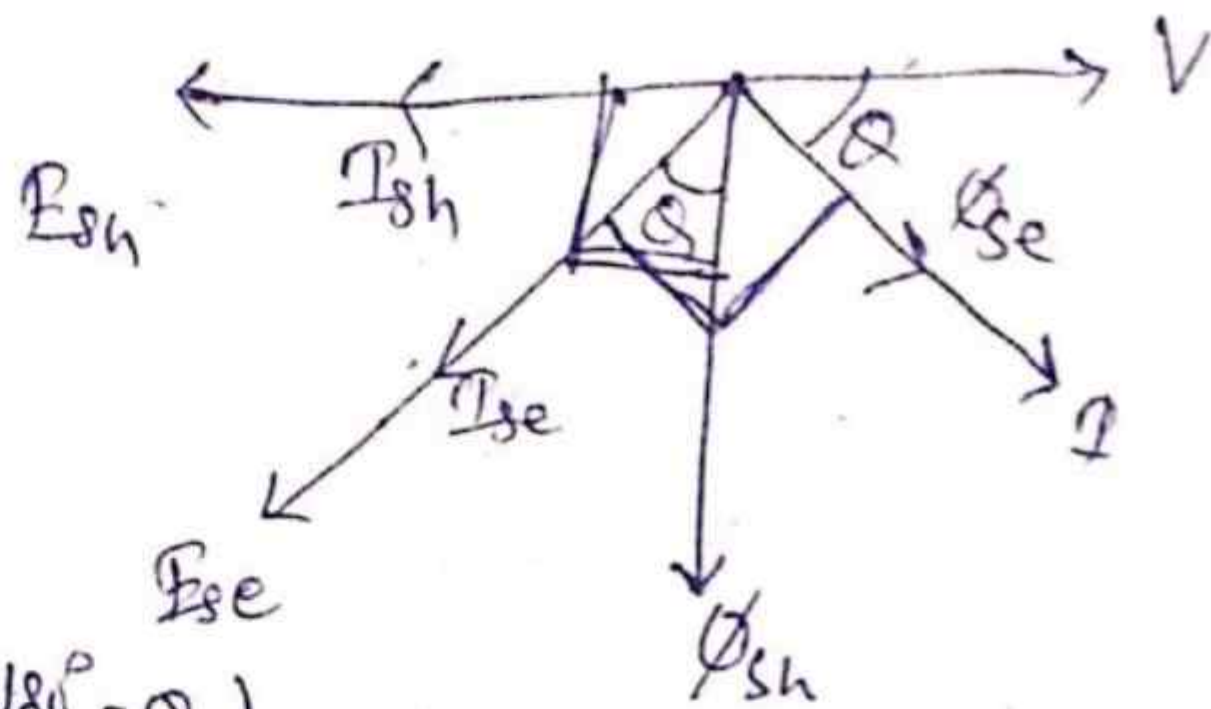
$$= K I_{se} \phi_{sh} \cos \theta - K I_{esh} \phi_{se} \cos (180^\circ - \theta)$$

$$= K [I_{se} \phi_{sh} \cos \theta + I_{esh} \phi_{se} \cos \theta]$$

$$= K [K_1 I V \cos \theta + K_2 V I \cos \theta]$$

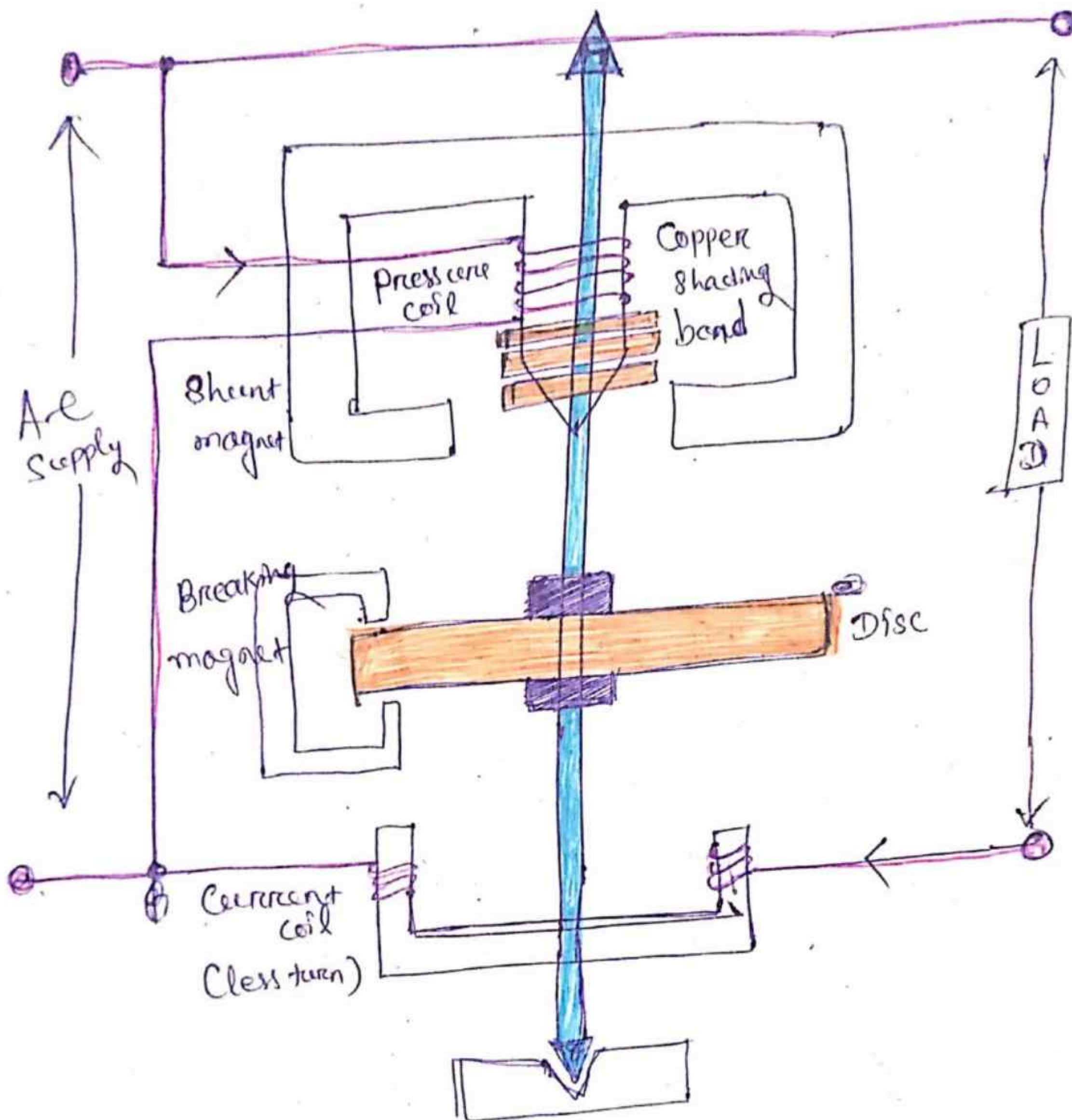
$$= K V I \cos \theta [K_1 + K_2]$$

$$T_d \propto V I \cos \theta$$



Date - 29/2/20

Induction type Energy meter



Errors

Q. Single phase induction type energy meter the errors may be caused by driving system or braking s/s. The driving s/s may cause error due to incorrect magnitude of fluxes, incorrect phase angles (produced by in proper lag adjustment, abnormal frequency, variation in resistance with temp etc.).

and lack of symmetry in magnet CKT, which makes the meters to creep.

- (ii) In correct magnitude of fluxes are produced by abnormal values of current, voltage or frequency or variation in coil resistance.
- (iii) The breaking S/S may cause error due to ~~mag~~ change in break magnet strength, change in disc resistance. (or) abnormal friction of moving parts.

④ Compensation and adjustment :-

① For low lagging power factor

We know that the meter will reads correctly at any power factor only when ϕ_{sh} lags supply voltage by 90° , but because the meter potential coil is not purely inductive hence the lagging angle is less than 90° , however

PC then can be made to lag supply voltage exactly 90° , by introducing a magnetic shunt CKT that allows the ϕ_{sh} to by pass the gap in which the disc is located. The required mmf is obtained from lag coil located on the central lense of the shunt magnet close to the disc gap so that it may link with the flux that cuts the disc.

For proper adjustment the shading band is connected to the central line of shunt magnet.

n) For friction on light load &

Despite every care in the design the pivot bearing which forms a lower bearing for the spindle when sample slip in type of bearing at the top of ~~the~~ the spindle frictional errors are liable to be serious specially at light load. So in order to insure a meter response to very light load small compensating torque particularly independent of load on the meter to overcome the friction of bearing and resisting mechanism.

This is usually attained by placing a small shading loop also termed as load plate in the air gap of shunt magnet. So that it produces a lag in the time phase of part of pressure coil flux.

(iii) For creeping &

It is the error caused in the energy meter due to rotation of disc without load. ~~a slight~~

A slight torque developed by the light load ~~adjustment~~ may cause the disc to rotate slowly in PC are excited ~~with~~ but with no load current flowing. This effect is known as creeping and it is prevented cutting two holes or slots in the disc, at the opposite side of spindle.

The disc tends to remain stationary when one of the poles comes under one of the poles of shunt magnet.

In some cases a small piece of iron wire is attached to the edge of the disc.

This adjustment to avoid creeping is called provisioning or light load adjustment.

For full load

There may be an error in the resistance and such an error is evident when meter is checked at rated voltage and rated current at unity power factor. Hence the adjustment is carried out either by varying the position of magnet shunt to control the amount of flux by breaking magnet.

The moment of break magnet is to reduce the speed of rotation of disc by moving the break magnet with respect to disc. The meter can resist correctly within the required limit of error.

Frictional errors

Date-3/03/20

Frictional forces at the rotor bearing and registering mechanism caused notable error at light loads. At the light loads the torque due to friction is considerable to the braking torque on the disc of rotor. Since friction torque is not proportional to the speed but is roughly constant and

can cause considerable error,

Adjustment :-

This error can be reduced by making the ratio of ϕ_{sh} and ϕ_{se} large with the help of shading band.

Temperature error :-

Temperature error due to variation of temp is very small because various effects tends to neutralize one another,

The resistance of coil and characteristics of magnetic ckt and strength of permanent magnet are affected by changes in temp.

Frequency variation :-

The meter is designed to give minimum error at a particular frequency. If the supply frequency changes the reactance of coil changes resulting small error.

Error due to voltage variation :-

This error is very small i.e. $(0.2 - 0.3)\%$

This can be eliminated by the proper design by proper magnetic ckt. of shunt magnet.

⑤ Frequency meter

Frequency meter is two types.

- ① Electrical resonance type.
- ② Mechanical resonance type.

Again electrical resonance ~~is~~ ~~resonance~~ is two types.

- ① Ferrodynamic type.
- ② Electrodynamometer type.

Frequency meter

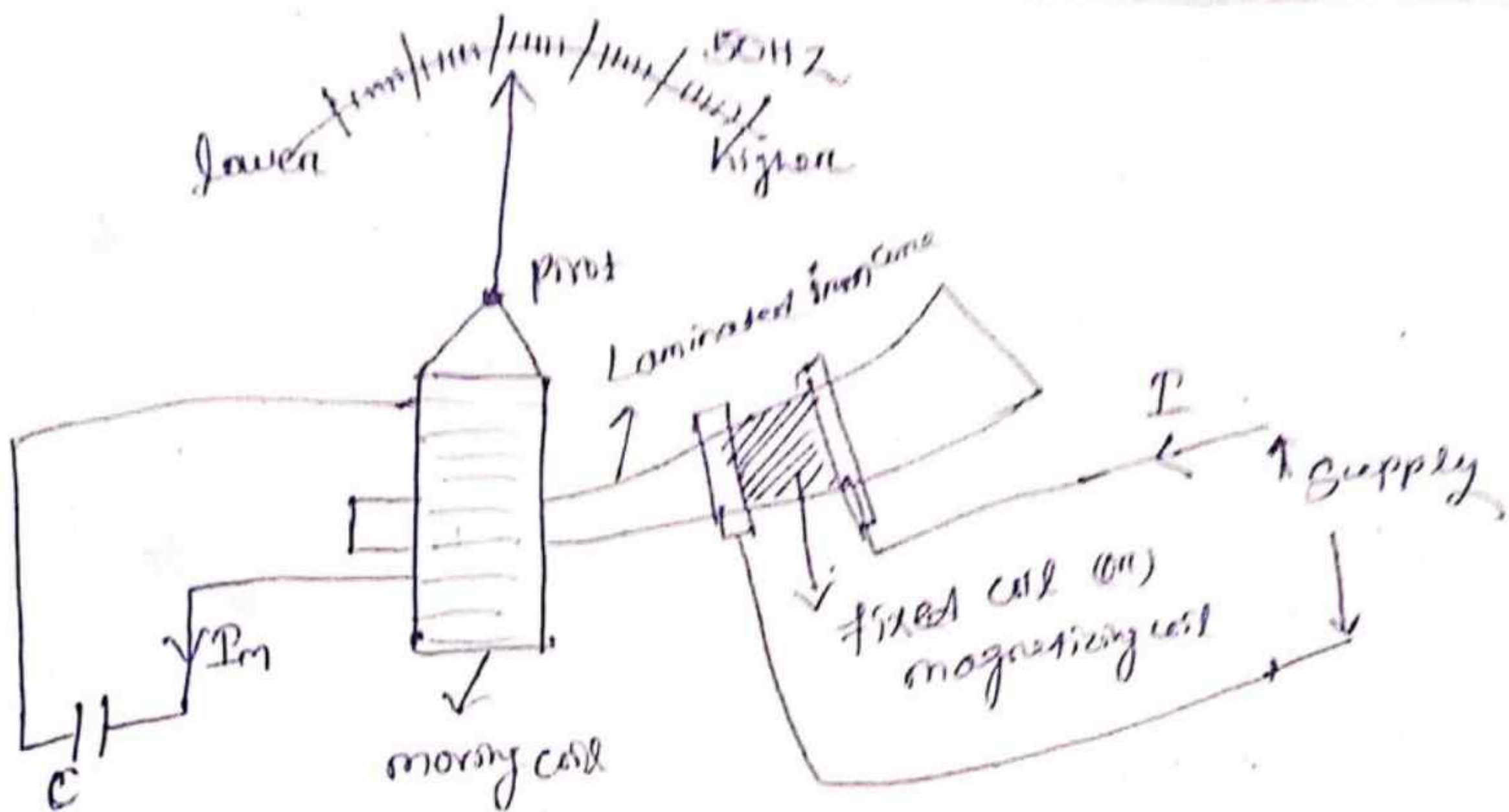
It is the measuring instrument which is used to measure frequency of A.C. supply.

There are various types of frequency meter present,

- ① electrical resonance type.
- ② mechanical resonance type.
- ③ Weston frequency meter.
- ④ Ratio meter.
- ⑤ Saturable core type frequency meter.

① Electrical Resonance type

* Ferrodynamic type frequency meter &



It consists of two electromagnet (or) coil. The fixed coil is mounted on ~~the~~ one end of the laminated iron cone. The supply is given to the fixed coil. The iron cone used here is variable cross section and laminated. Its cross sectional area varies gradually over length. It is being maximum over ~~one~~ end where fixed coil is mounted and minimum over other end.

A moving coil is pivoted over the iron cone. A pointer is attached to the moving coil - the terminals of moving coil are connected to the capacitor of suitable value.

Working principle:-

This instrument is designed in such a way that the pointer moment stops at the occurrence of electrical resonance. electrical resonance can be observed by the condition of $X_L = X_C$.

when the supply is given to the magnetizing coil, current I flows through it and it produces flux Φ .

This flux is alternating in nature and in phase with I , when it links to the moving coil then emf is induced in the moving coil, 'E' by which a current is flowing in the moving coil. let it be I_m .

For the moving coil a self inductance L is developed. The value of L depends upon the nearness or position of moving coil on the ϕ iron core.

If it is more nearer to the fixed coil 'L' will be more.

~~also~~ The value of capacitor is slow chosen that for normal operating frequency (50 Hz) the resonance by default occurs. and the coils at initial position indicating frequency 50 Hz .

Operation :-

Case-1 - If $f > 50\text{ Hz}$, $X_L > X_C$ with this condition the moving coil rotates in clockwise direction there by pointer gradually starts towards the scale $> 50\text{ Hz}$. on this moment the moving coil is going away from magnetizing coil there by 'L' decreases.

with this continuous moment at some position $X_L = X_C$ obtained at that position pointer stops indicating appropriate value of frequency.

Case-2 If $f < 50\text{Hz}$ i.e. $X_L < X_C$

In this case moving coil makes deflection in anticlockwise direction with this it reaches nearer to magnetizing coil there by I increases. at some point $\odot X_L = X_C$ occurs, and the pointer stops and indicates the frequency.

Case-3 If $f = 50\text{Hz}$ i.e. $X_L = X_C$

In this position the deflecting torque of moving coil is zero, hence ~~it stops~~ it remains at its initial position.

Electrodynamometer ~~type~~ type
frequency meter

Date - 4/2/20

Construction:-

